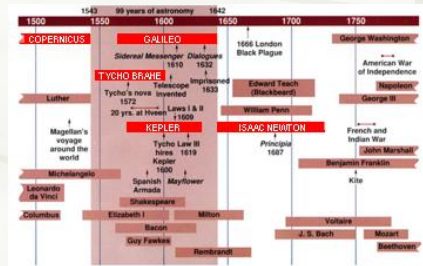


# Lecture 3: Cosmology of the Scientific Revolution

- ◆ Tycho Brahe
- ◆ Kepler
- ◆ Galileo
- ◆ Newton



<http://www.physics.fsu.edu/users/Lind/AST1002/>

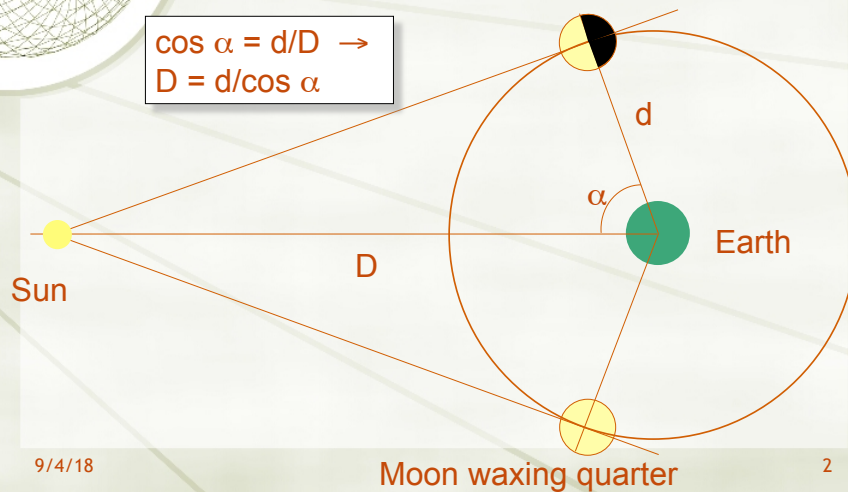
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1

## Aristarchus Earth-Sun distance

Moon waning quarter

$$\cos \alpha = d/D \rightarrow D = d/\cos \alpha$$



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2



## Heliocentric model of Aristarchus

- ★ Observations implied Sun is much larger than Earth
- ★ Therefore proposed the first **heliocentric** model
  - ★ Sun is the center of the Universe
  - ★ Everything goes around the Sun
- ★ Never accepted by others of his time
  - ★ inconsistent with *apparent* perception of stationary Earth
  - ★ No *apparent* shift in stellar positions could be observed over course of seasons
  - ★ Prevailing culture was uncomfortable with the idea that Earth was not central to the Cosmos

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3



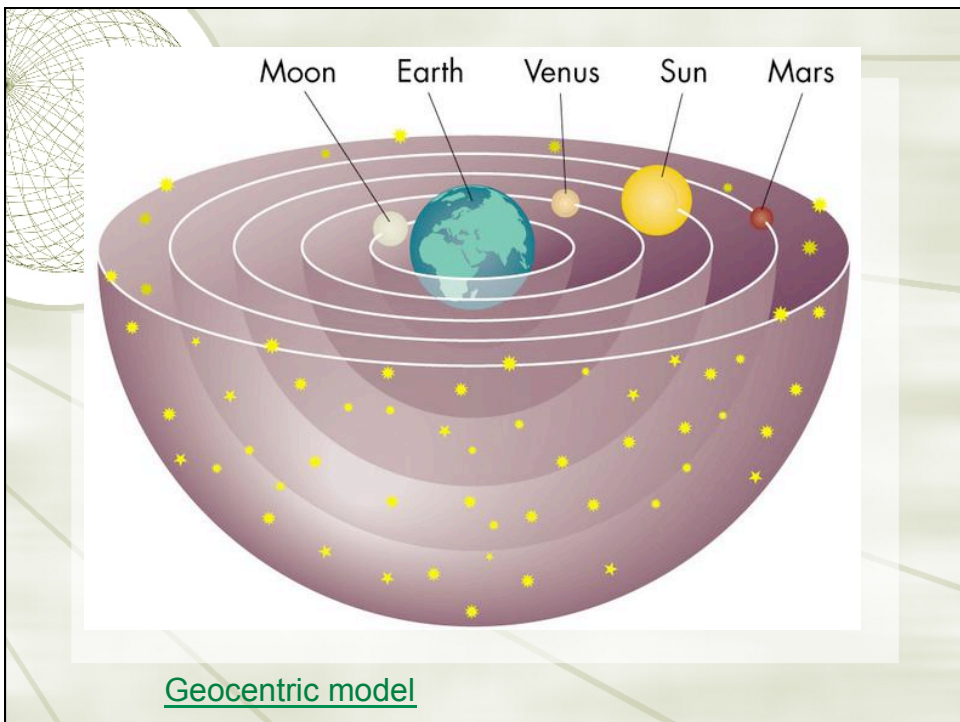
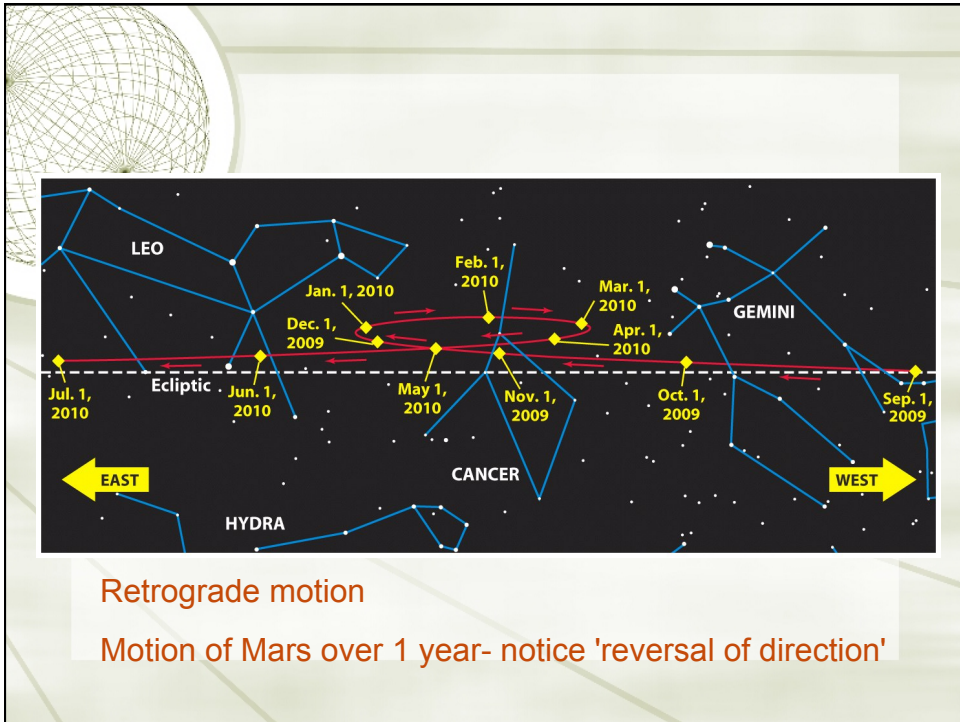
## Ptolemy (100-170 A.D.)

- ★ Worked at observatory in Alexandria, both as observer and theorist
- ★ Developed theory to accommodate detailed planetary observations:
  - ★ Variations in brightness over months
  - ★ Retrograde motions
  - ★ Variations in observed orbital speed
- ★ Theory involved motion along small circles superposed on top of motion along large circles (think Spirograph!)
- ★ Successors added additional “epicycles” to model to improve agreement with observations
  - ★ Very complex!
  - ★ No underlying law; no predictive power for new planets



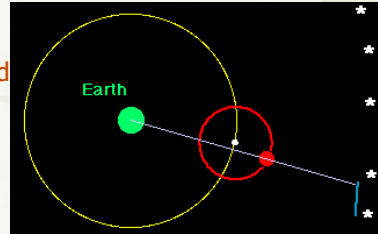
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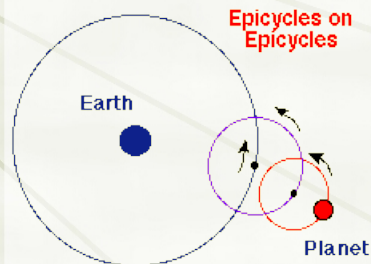


## Ptolemy's epicycles

- ✦ Ptolemy's original "epicycles"
  - ✦ Larger circle ("deferent") not centered on the Earth
  - ✦ Motion appeared uniform from "equant" (offset from Earth and from center of "deferent")



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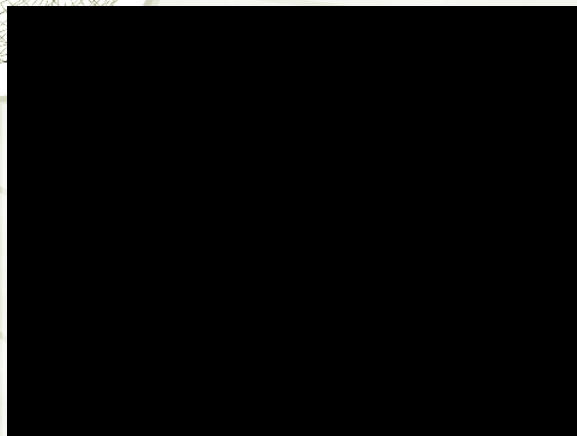


Needed more and more epicycles to fit observed angular motion

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## Ptolemy and Homer



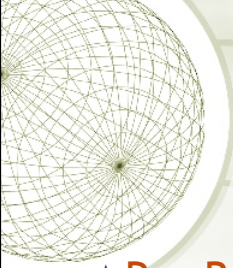
Carman & Serra,  
from YouTube

- This particular "orbit" required 1000 epicycles
- What do you think this translates to in terms of falsifying the theory?

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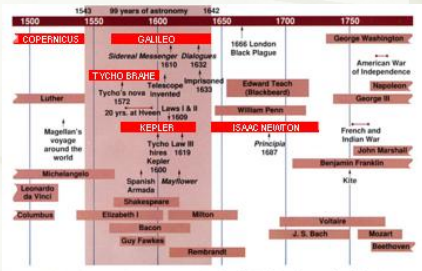
8





## Renaissance cosmology

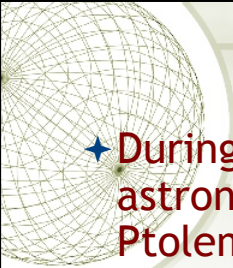
- ◆ Pre-Renaissance
- ◆ Copernicus
- ◆ Tycho



The transition from ancient astronomy to the birth of modern scientific astronomy

<http://www.physics.fsu.edu/users/Lind/AST1002/>

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## Before the Renaissance

- ◆ During European “dark ages,” Arab astronomers preserved and extended Ptolemy’s work
- ◆ Aristotelian/Ptolemaic view prevailed in Europe, through 1400’s
  - ◆ Geocentric model
  - ◆ Creation at finite time in past, for consistency with Christian theology
  - ◆ Earth known to be round (Columbus battling against “flat Earth”ers is myth!)

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## Copernicus (1473-1543)

- ✦ Nicholas Copernicus was modern founder of the heliocentric (Sun centered) model for the solar system
- ✦ Copernicus was born in Poland; studied in Krakow, Bologna, Padua, Ferrara
  - ✦ canon law, medicine, mathematics, astronomy
  - ✦ Worked as church canon, physician
- ✦ Rejected Ptolemy's geocentric model because it was too complicated
- ✦ Preferred heliocentric model with perfect circular motions
- ✦ **The Copernican Principle : The Earth is not at a special location in the Universe.**
- ✦ Later, we will come across the **Generalized Copernican Principle: There is no special place in the universe, i.e., the universe has no center.**

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## Copernicus's first work

- ✦ Wrote and distributed to friends the *Little Commentary* (1514)  
Axioms:
  1. *There is no one center in the universe.*
  2. *The Earth's center is not the center of the universe.*
  3. *The Earth and planets revolve around the Sun.*
  4. *The distance from the Earth to the Sun is imperceptible compared with the distance to the stars.*
  5. *The rotation of the Earth accounts for the apparent daily rotation of the stars.*
  6. *The apparent annual cycle of movements of the Sun is caused by the Earth revolving round it.*
  7. *The apparent retrograde motion of the planets is caused by the motion of the Earth from which one observes.*

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Portrait from 1597  
by Teothor de Bry

## Copernicus' *de Revolutionibus*

- ✦ Full title: *De Revolutionibus Orbium Coelestium*
- ✦ Printed Nuremberg, 1543, in last year of life
- ✦ Spelled out, using observations and mathematics, evidence for his heliocentric model
  - ✦ Simple and natural explanation for retrograde motion of planets
  - ✦ Included accurate relative spacings of planetary orbits
  - ✦ Showed that planetary speeds decrease outward from Sun
  - ✦ Still had to include some epicycles to improve agreement with observations
- ✦ Book was widely read and appreciated by 16th C. astronomers
  - ✦ some believed in Copernicus' heliocentric physical model
  - ✦ others considered Copernicus' approach superior for calculating orbits, but believed in geocentric Universe
- ✦ No official position by Catholic church up to 1600

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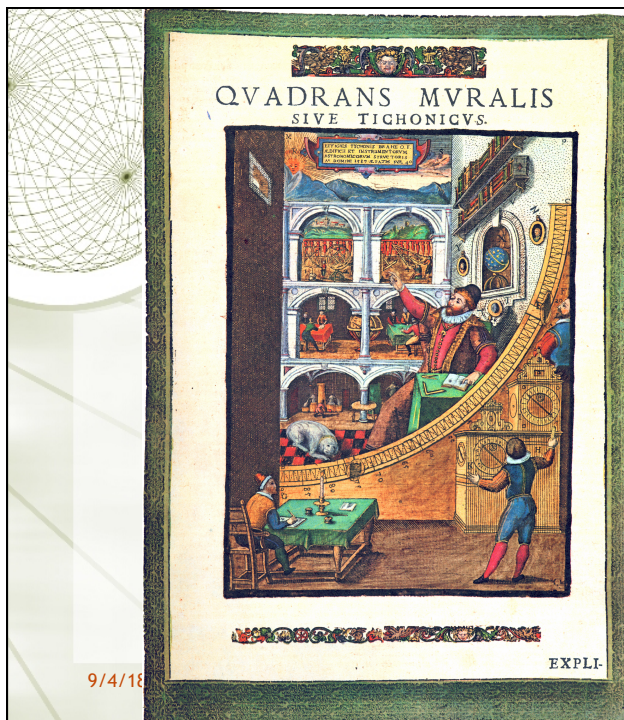




## Tycho Brahe (1546-1601)

- Flamboyant and tyrannical aristocrat, but devoted to science
- Lived and observed on an island (Ven) off the coast of Denmark
- Last of the great “naked eye” observers
- Made planetary observations much more accurate than any previous
- Observed “new star” (Tycho’s supernova) in 1572
- Demonstrated that a comet was beyond Moon’s orbit
- From parallax observations of new star, comet:
  - knew they were not in Earth’s atmosphere
  - evidence that heavens were not immutable

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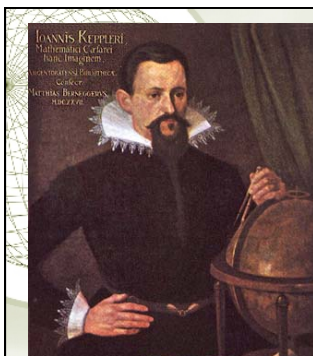
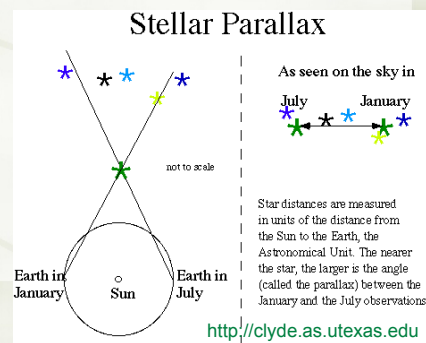
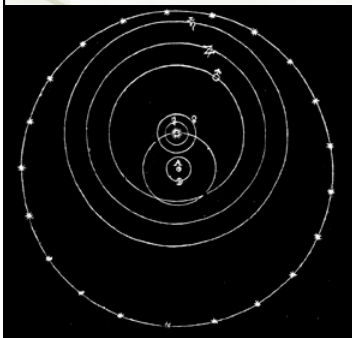
## Large quadrant at Uraniborg

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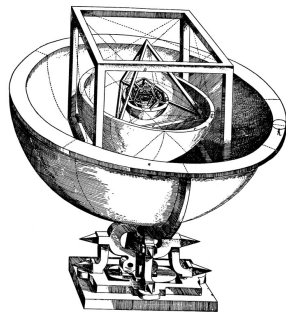
## Tycho's cosmological model

- ✦ Tycho used parallax observations to explore heliocentric model:
  - ✦ If Earth moves, then parallax of stars *should* be observable
  - ✦ Tycho could not detect any significant parallax; he concluded Earth is stationary
  - ✦ In fact, stellar parallax is 100× too small for naked-eye observation to measure; largest values are about 1 arcsecond= $(1/3600)^\circ$
- ✦ Tycho settled on combined geo/helio-centric model
  - ✦ Sun orbits Earth; all other planets orbit Sun



## Johannes Kepler (1571-1630)

- ✦ Born in Germany; originally planned to be ordained as Lutheran minister
- ✦ Convinced God made the Universe according to a mathematical plan; saw his Christian duty as understanding works God had created
- ✦ Studied mathematics; published in 1596 his *Mystery of the Cosmos* proposing that planetary orbits lie in spheres nested within a series of the Platonic solids (wrong!)
- ✦ Was hired as Tycho Brahe's assistant in Prague; his job was to make sense of Brahe's extremely accurate observations of Mars
- ✦ Kepler became Imperial Mathematician after Brahe's death (1601)
- ✦ Kepler's "war with Mars" amounted to a thousand sheets of arithmetic; resulted in publishing Kepler's "First Law" and "Second Law" in 1609 as part of his *New Astronomy*
- ✦ Kepler's "Third Law" was published in 1619 as part of his *Harmony of the World*



The Polyhedra inscribed into the planetary orbits. Kepler's drawing is a pure geometrical fancy, but it is meant to correspond to the actual relation between the radii of the planetary orbits. Most important here is the cube, fitted into the outermost sphere of Saturn.

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## Kepler's first law

★ Planets move around the Sun in ellipses, with the Sun at one focus.

The diagram shows an elliptical orbit with the Sun at the left focus (yellow dot) and Mars at a point on the orbit (red dot). The right focus is marked with a blue dot and a question mark. The distance from the Sun to Mars is labeled  $d_1$ , and the distance from the right focus to Mars is labeled  $d_2$ . The equation  $d_1 + d_2 = \text{constant}$  is written to the right. The leftmost point of the orbit is labeled 'perihelion' and the rightmost point is labeled 'aphelion'. A dashed horizontal line represents the major axis. An arrow on the orbit indicates the direction of motion.

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## Kepler's first law

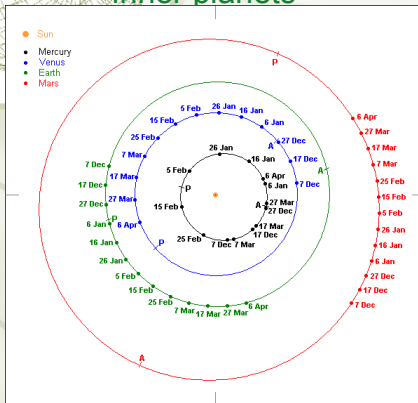
Drawing an ellipse is easy: use two tacks for the foci and a string

The image shows a hand holding a white marker, drawing an ellipse on a piece of paper. Two tacks, one green and one yellow, are pinned to the paper as foci. A string is looped around both tacks and held together by the hand. The string is being used to trace the path of an ellipse.

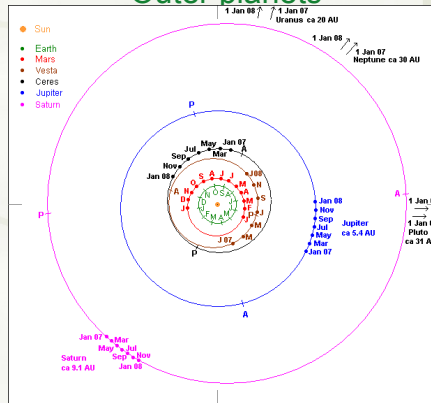
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# Solar system orbits

## Inner planets



## Outer planets +



<http://www.rasnz.org.nz/SolarSys/Orbits07.htm>

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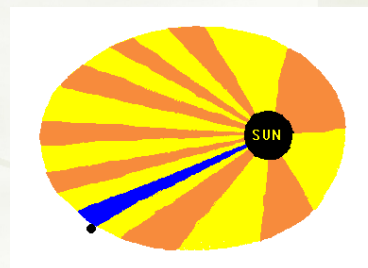
*Note the low eccentricities!*

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# Kepler's second law

★ The line connecting the Sun and a given planet sweeps out equal areas in equal times.

- ★ Therefore, planets move faster when they are nearer the Sun
- ★ Consequence of angular momentum conservation.



<http://home.cvc.org/science/kepler.gif>

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Kepler's second law with high- and low- eccentricity orbits

The diagram shows a central yellow star with two elliptical orbits. The inner orbit is highly eccentric, while the outer orbit is nearly circular. Two cyan arrows originate from the star, pointing to the same point on each orbit. The arrow pointing to the point on the highly eccentric orbit is significantly longer than the arrow pointing to the point on the circular orbit, demonstrating that the area swept out by the longer radius vector is equal to the area swept out by the shorter radius vector in the same time interval.

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*Time-lapse movies of orbits*  
Stars around the Galactic center's black hole

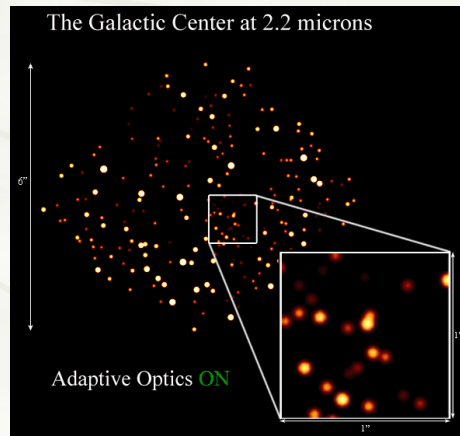
The image shows a 3D model of a star with a bright blue core and a grey, flattened accretion disk. The star is positioned in the center of the frame, representing its orbit around the Galactic center's black hole.

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<http://www.galacticcenter.astro.ucla.edu/animations.html>



## Time-lapse movies of orbits

Stars around the Galactic center's black hole



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<http://www.galacticcenter.astro.ucla.edu/animations.html>

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## Kepler's third law

- ★ The square of the period  $P$  of the orbit is proportional to the cube of the semi-major axis  $R$
- ★ Period ( $P$ ) = time it takes for planet to complete one orbit
- ★ Semi-major axis ( $R$ ) = half of the length of the "long" (i.e. major) axis of the ellipse.

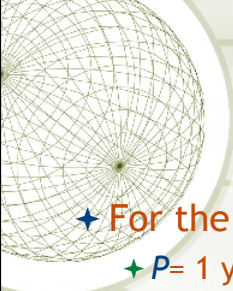
$$P^2 = \text{constant} \times R^3$$

$$P^2 = 4\pi^2 / G(M+m) \times R^3$$

(Newton)

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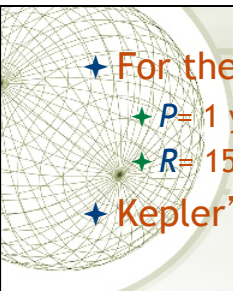
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- ★ For the Earth, we know that:
  - ★  $P = 1 \text{ year} = 3 \times 10^7 \text{ seconds}$
  - ★  $R = 150 \text{ million km (1 Astronomical Unit, A.U.)}$
- ★ Kepler's 3<sup>rd</sup> law says that, for other planets,

$$\left( \frac{P}{\text{yr}} \right)^2 = \left( \frac{R}{\text{AU}} \right)^3$$

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- ★ For the Earth, we know that:
  - ★  $P = 1 \text{ year} = 3 \times 10^7 \text{ seconds}$
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- ★ Kepler's 3<sup>rd</sup> law says that, for other planets,

$$\left( \frac{P}{\text{yr}} \right)^2 = \left( \frac{R}{\text{AU}} \right)^3$$

- ★ Newton will show (lect# 5) that in general

$$P^2 = \frac{4\pi^2}{GM_{\text{sun}}} R^3$$

Where  $G$  is the "gravitational constant"

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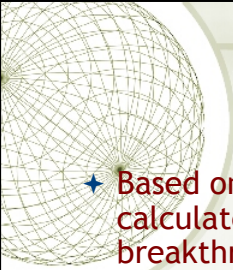


## An imprecise version of Kepler's laws

- ✦ Orbits are not circular
- ✦ A planet's speed changes during its orbit
- ✦ There is a definite relationship between orbital period and the distance from the star

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## Kepler in perspective

- ✦ Based on Tycho Brahe's accurate observations, Kepler calculated and thought his way to a major breakthrough in cosmology
- ✦ Kepler's three laws of planetary motion
  - ✦ Represented a very simple (and correct!) model of the solar system
  - ✦ Swept away thousands of years of prejudice - and his own previous pet theory!
  - ✦ Were driven fundamentally by the **data**, including Tycho's error estimates
- ✦ Unlike previous models which quantified only what was observed already, Kepler's Laws had **predictive power**, consistent with modern idea of a meaningful scientific theory

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*This is what we mean by “predictive power”*

- ★ Line is Kepler’s third law
- ★ Boxes are planets in the solar system

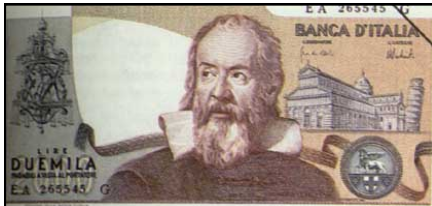
Period (yrs)	Distance (AU)
0.1	0.1
1	1
10	10
100	100

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*Exoplanets discovered by the Kepler observatory*

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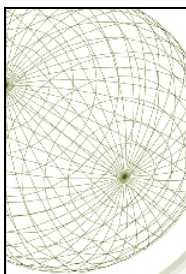


## Galileo Galilei (1564-1642)

- ✦ Born in Pisa; worked as professor of mathematics
- ✦ Built one of the first telescopes in 1609
- ✦ Published *"The Starry Messenger"* with first telescopic discoveries in 1610
- ✦ Telescopic observations:
  - ✦ Saw craters and mountains on the Moon
  - ✦ Realized sunspots were on surface, not foreground; rotated with Sun
  - ✦ Identified four satellites of Jupiter ("Galilean moons")
  - ✦ Saw rings of Saturn
  - ✦ Resolved the diffuse Milky Way into many faint stars
  - ✦ Observed phases of Venus including gibbous and full

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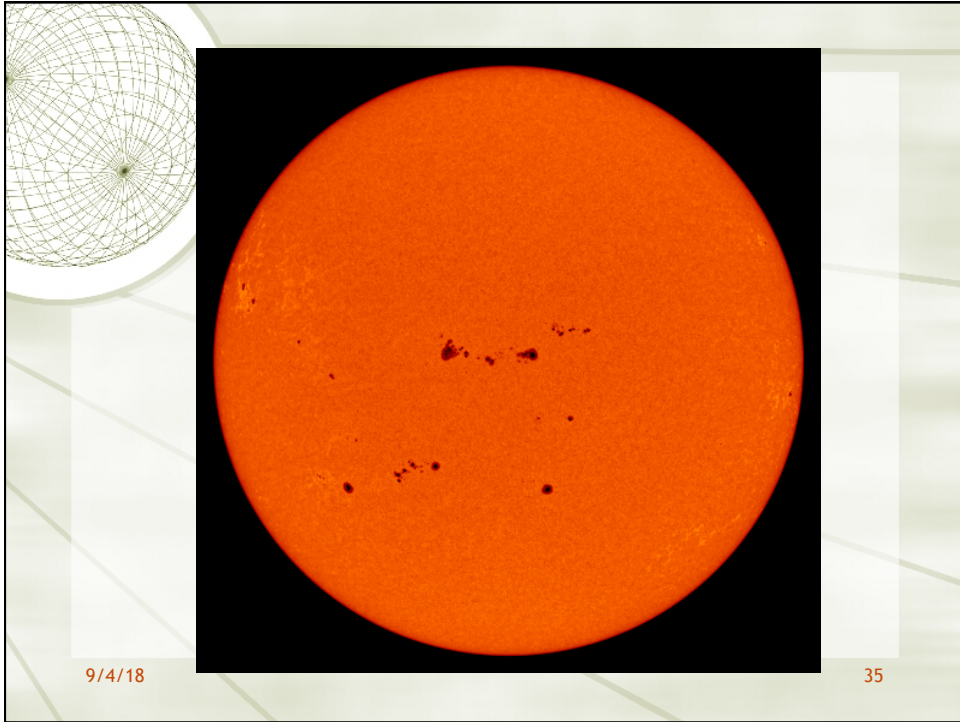
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<http://www.astromax.org>

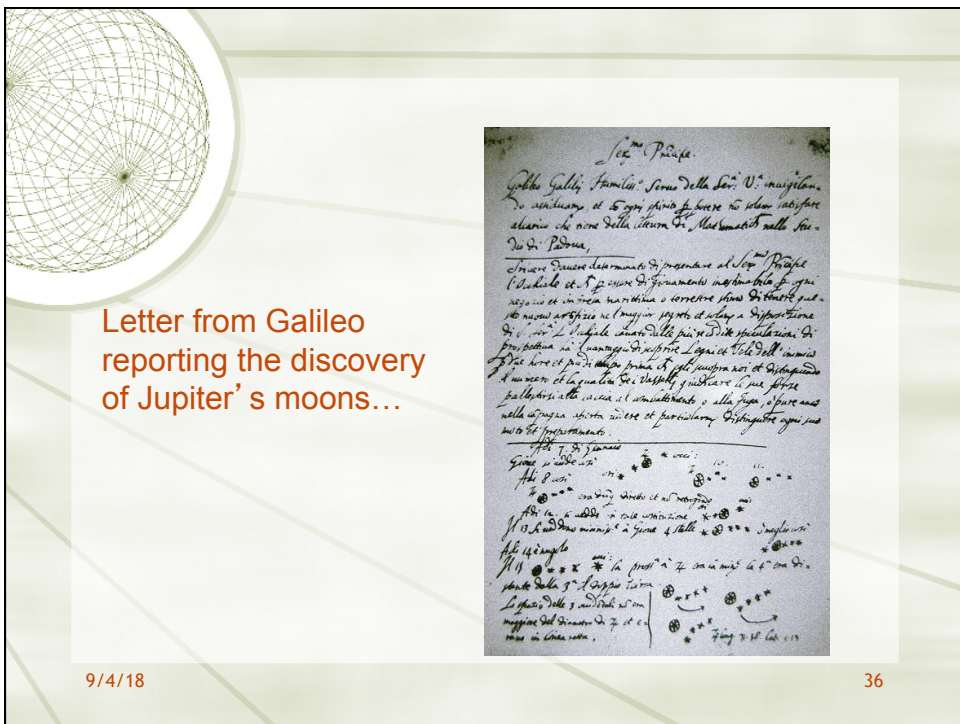
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Letter from Galileo reporting the discovery of Jupiter's moons...

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SIDEREUS NUNCIUS 75

On the third, at the seventh hour, the stars were arranged in this sequence. The eastern one was 1 minute, 30 seconds from Jupiter; the closest western one 2 minutes; and the other western one was

East                    \* ○ \*                    \* West

10 minutes removed from this one. They were absolutely on the same straight line and of equal magnitude.

On the fourth, at the second hour, there were four stars around Jupiter, two to the east and two to the west, and arranged precisely

East                    \* \* ○ \* \*                    West

on a straight line, as in the adjoining figure. The easternmost was distant 3 minutes from the next one, while this one was 40 seconds from Jupiter; Jupiter was 4 minutes from the nearest western one, and this one 6 minutes from the westernmost one. Their magnitudes were nearly equal; the one closest to Jupiter appeared a little smaller than the rest. But at the seventh hour the eastern stars were only 30 seconds apart. Jupiter was 2 minutes from the nearer eastern

East                    \*\* ○ \* \*                    West

one, while he was 4 minutes from the next western one, and this one was 3 minutes from the westernmost one. They were all equal and extended on the same straight line along the ecliptic.

On the fifth, the sky was cloudy.


On the sixth, only two stars appeared flanking Jupiter, as is seen

East                    \* ○ \*                    West

in the adjoining figure. The eastern one was 2 minutes and the western one 3 minutes from Jupiter. They were on the same straight line with Jupiter and equal in magnitude.

On the seventh, two stars stood near Jupiter, both to the east, arranged in this manner.

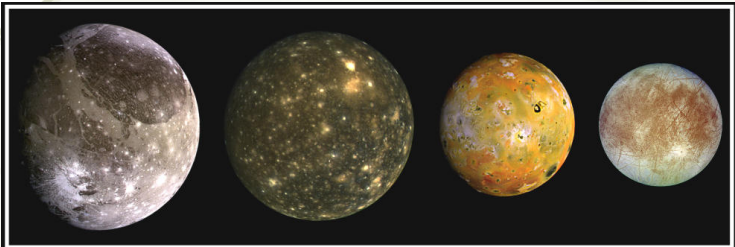
## Galilean Moons



<http://www.ladeltascience.com/astronomy/kisatchie04/>

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## Galilean moons (from Galileo spacecraft!)

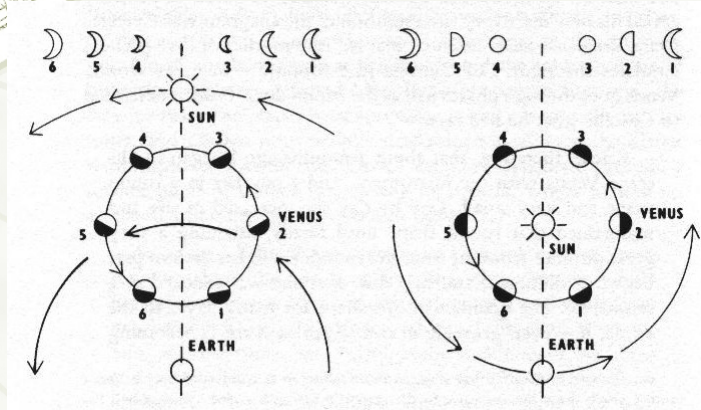


NASA

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## Phases of Venus: the test of the Heliocentric system



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<http://www.telescope1609.com/Galileo.htm>

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## Galileo's lens, Florence



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## Museo di Storia della Scienza, Florence



IV. 10  
Dito medio della mano destra di Galileo  
Taca e incisione: c. 1737  
Taca: marmo, vetro  
Middle finger of Galileo's right hand  
Stand, case, and inscription: c. 1737  
Stand: marble, glass



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## Impact of Galileo's observations

- ✦ Chipping away at Aristotelian point of view:
  - ✦ Features on Sun, Moon, Saturn indicated they are not "perfect" orbs
  - ✦ Faint stars resolved in Milky Way indicates stars at many distances -- not just single sphere
  - ✦ Moons of Jupiter showed that Earth was not sole center of motion
- ✦ Crucial experiment ruling out Ptolemaic model:
  - ✦ Possible phases of Venus in Ptolemaic model are only crescent or new -- but Galileo *observed full phase*
  - ✦ Observation supported Copernican (or Tycho's) model (Venus on far side of Sun when full)
- ✦ As a result of his observations, Galileo became ardent supporter of Copernican viewpoint
- ✦ In 1632, published *Dialogue Concerning the Two Chief Systems of the World - Ptolemaic and Copernican*
- ✦ The Inquisition banned the book; Galileo was found guilty of heresy in supporting Copernican view, and sentenced to house arrest

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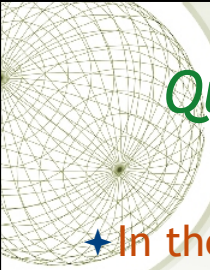


## Galilean physics

- ★ After 1633 trial, Galileo returned to work on physics of mechanics
- ★ Published *Discourses and mathematical demonstrations concerning the two new sciences* (1642)
- ★ Made experiments with inclined planes; concluded that distance  $d$  traveled under uniform acceleration  $a$  is  $d = a t^2$
- ★ Used “thought experiments” to conclude that all bodies, regardless of mass, fall at the same rate in a vacuum --contrary to Aristotle
  - ★ Now known as “equivalence principle”
- ★ Realized full principle of inertia:
  - ★ body at rest remains at rest;
  - ★ body in motion remains in motion (force *not* required)
- ★ Realized principle of relative motion (“Galilean invariance”):
  - ★ If everything is moving together at constant velocity, there can be no apparent difference from case when everything is at rest.
  - ★ Ball dropped from top of moving ship’s mast hits near bottom of mast, not behind on deck.

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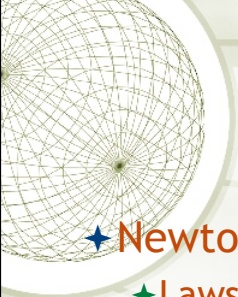


## Quiz: Write your name and answer in the card

- ★ In the first lecture we talked about the characteristics of a scientific theory. This lecture we pointed out a fundamental problem (in terms of modern scientific thinking) with Ptolemy’s system of epicycles to explain planetary motions.
  - ★ What was it?

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## Next time...


- ★ **Newton and his laws**
  - ✦ Laws of motion
  - ✦ Law of universal gravitation

*Start reading Chapter 3 of text*

*First Homework will be posted tomorrow!!!!*

*HW #1 due on Sept 20th!*

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## Isaac Newton (1643-1727)

- ★ Attended Cambridge University, originally intending to study law, but reading Kepler, Galileo, Descartes
- ★ Began to study mathematics in 1663
- ★ While Cambridge was closed due to plague (1665-1667), Newton went home and
  - ✦ began to work out foundations of calculus
  - ✦ realized (contrary to Aristotle) that white light is not a single entity, but composed of many colors
  - ✦ began to formulate laws of motion and law of gravity
- ★ Became professor of mathematics starting in 1669 (age 27!)
- ★ Worked in optics, publishing “Opticks” (1704)
  - ✦ invented reflecting telescope
  - ✦ showed color spectrum from prism recombines into white light with a second prism
  - ✦ analyzed diffraction phenomenon

*Isaac Newton in 1689, by Sir Godfrey Kneller.*

**Father of modern physics and cosmology**

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## Newton's history, cont.

- ★ In 1687, published *Philosophiæ naturalis principia mathematica*, or “*Principia*”
  - ★ publication was prompted (and paid for) by Halley
  - ★ partly in response to claim by Hooke that he could prove gravity obeyed inverse-square law
  - ★ included proof that inverse square law produces ellipses
  - ★ generalized Sun's gravity law to universe law of gravitation:  
*all matter attracts all other matter with a force proportional to the product of their masses and inversely proportional to the square of the distance between them*
  - ★ many other applications, including tides, precession, etc.
  - ★ laid out general physics of mechanics -- laws of motion
  - ★ showed that Kepler's laws follow from more fundamental laws
- ★ The *Principia* is recognized as the greatest scientific book ever written!
- ★ Retired from research in 1693, becoming active in politics and government

9/4/18

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