



So... where are we?

- ★ We have described the first ~10 mins of the Universe's life...
 - ★ Origin of matter (well within first second)
 - ★ Origin of elements (within first few mins)
- ★ Universe continues to expand and cool...
 - ★ $t=70,000\text{yr}$: Radiation ceases to be dominant over matter
 - ★ $t=380,000\text{yr}$: Universe cools to the point where neutral hydrogen can form
 - ★ EPOCH OF RECOMBINATION
 - ★ Universe suddenly becomes transparent... photons free stream, redshift and are observed today as the CMB!!
- ★ Until now, there's essentially no structure in the Universe. To discuss emergence of structure, we need to look harder at contents of Universe

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Lecture 19 : Weighing the Universe, and the need for dark matter

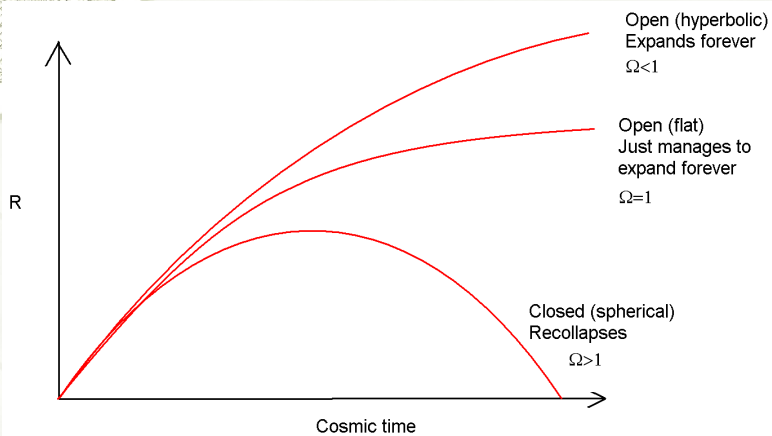
- ★ Recap -
 - ★ Constraints on the baryon density parameter Ω_B
 - ★ The importance of measuring the total density parameter Ω
- ★ Measuring the mass of the Universe
 - ★ Mass to light ratio
 - ★ Mass of luminous stars
 - ★ Masses of galaxies and galaxy clusters
- ★ Non-baryonic dark matter
- ★ [Read Chapter 15 for useful background]

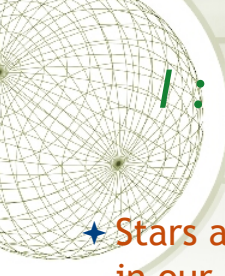
0 : RECAP

- ★ Define the density parameter as

$$\Omega = \frac{\rho_{total}}{\rho_{crit}}$$

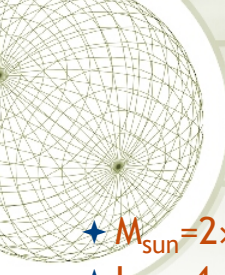
- ★ Value of Ω very important for determining the geometry and dynamics (fate) of the Universe
- ★ Constraints from nucleosynthesis
 - ★ To get observed mixture of elements, we need the **baryon density parameter** to be $\Omega_B \approx 0.037$
 - ★ If there is only baryonic (“normal”) matter in the universe, then this tells us that $\Omega \approx 0.037$.
 - ★ Thus, the Universe would be open (hyperbolic)
- ★ But life is more complicated than that...





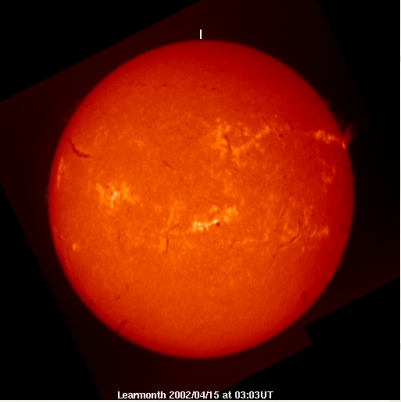
I: THE MASS OF STARS IN THE UNIVERSE

- ★ Stars are the easiest things to see and study in our Universe...
 - ✦ Can study nearby stars in detail
 - ✦ Can see the light from stars using “normal” optical telescopes in even distant galaxies.
- ★ Of course, what we see is the light, and what we’re interested in is the mass... need to convert between the two using the mass-to-light ratio M/L .



The Sun

- ★ $M_{\text{sun}} = 2 \times 10^{30} \text{ kg}$
- ★ $L_{\text{sun}} = 4 \times 10^{26} \text{ W}$
- ★ Actual numbers not very instructive...
- ★ From now on, we will reference mass-to-light ratios to the Sun ($M_{\text{sun}}/L_{\text{sun}}$).




Learnmonth 2002/04/15 at 03:03UT




Other stars

- ★ Different types of stars have different mass-to-light ratios
 - ✦ Massive stars have small M/L (they shine brightly compared with their mass).
 - ✦ Low-mass stars have large M/L (they are very dim compared with their mass).
 - ✦ We're interested in an average M/L
- ★ Averaging stars near to the Sun, we get $M/L \approx 3 M_{\text{sun}}/L_{\text{sun}}$

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- ★ But, we also need to include effect of “dead” stellar remnants...
 - ✦ white dwarfs, neutron stars, black holes.
 - ✦ These have plenty of mass M , but very little light L .
 - ✦ These have very high ratio M/L
 - ✦ Including the remnants, can have mass-to-light ratio as high as $M/L \approx 10 M_{\text{sun}}/L_{\text{sun}}$




- ★ So, can add up the visible star light that we see in the Universe, and convert to a mass.
 - ✦ We get $\Omega_{L^*} \approx 0.005-0.01$
 - ✦ Comparing with $\Omega_B = 0.036$ from nucleosynthesis, we see that most baryons cannot be in stars...



II : THE MASS OF GALAXIES

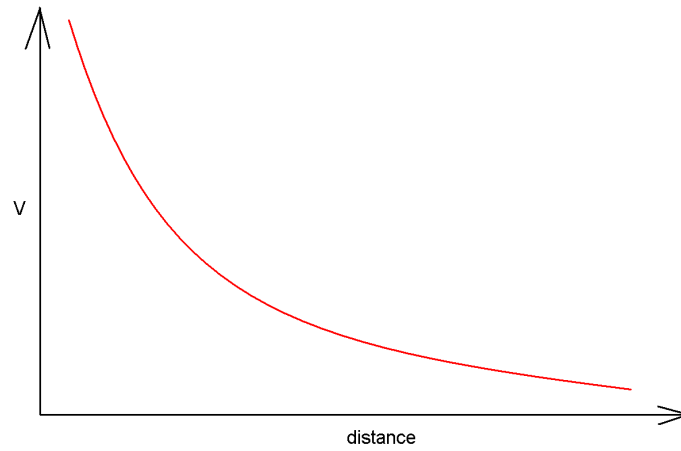
- ★ We can also measure total mass of a galaxy using Kepler's/Newton's laws
- ★ Remember the case for planets...

$$M_{sun} = \frac{4\pi R^3}{GP^2}$$

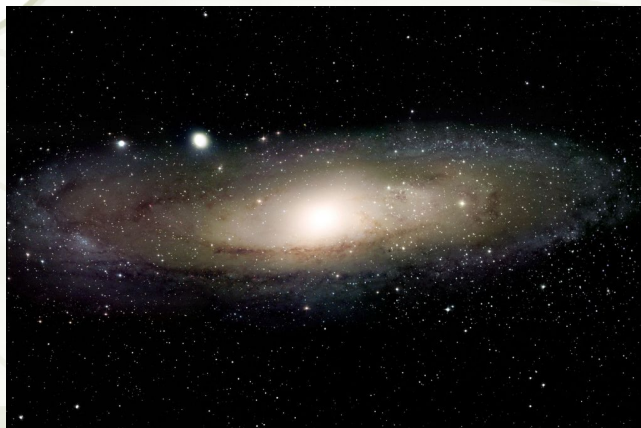
- ★ Can rewrite this as

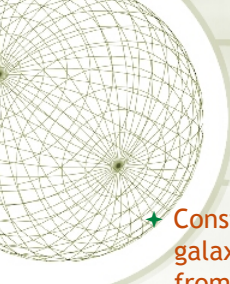
$$M_{sun} = \frac{V^2 R}{G} \quad \text{or} \quad V = \sqrt{\frac{GM_{sun}}{R}}$$

*Velocity dependence on radius
for a planet orbiting the Sun...*

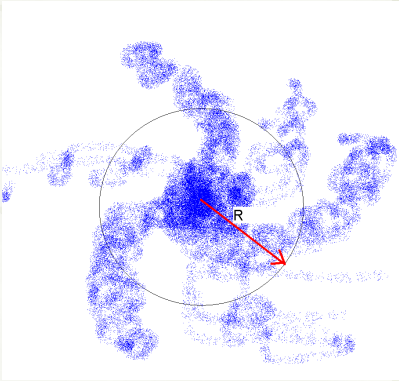
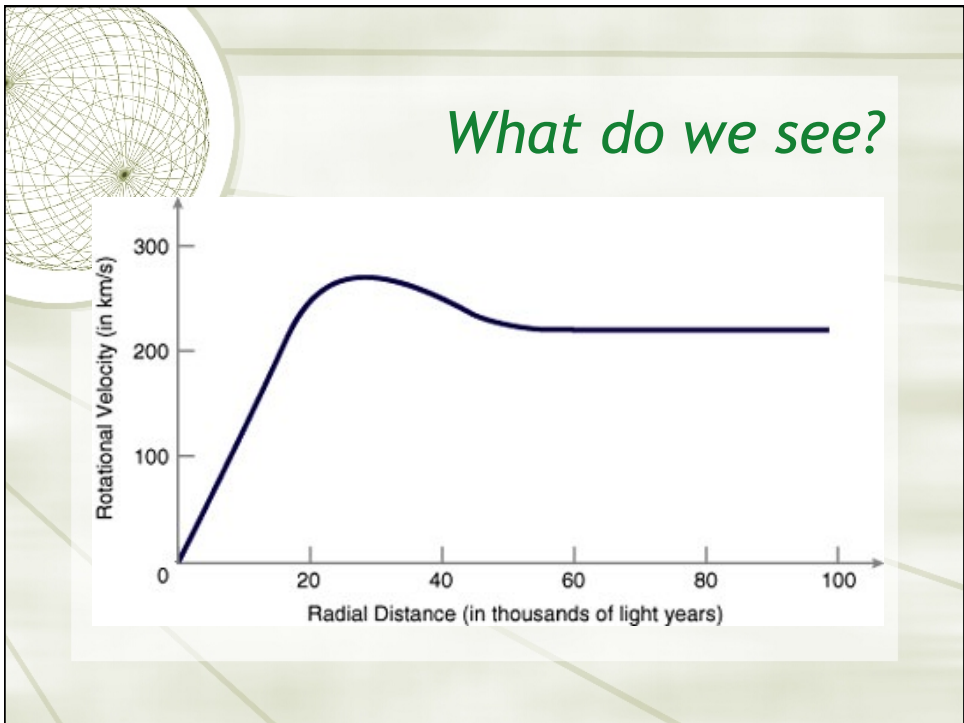


★ Apply same arguments to a galaxy...

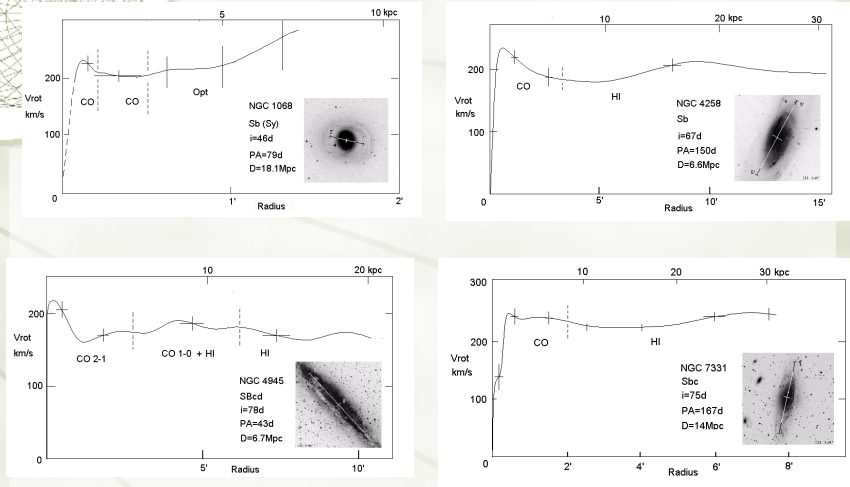




- ★ Consider a star in the galaxy at distance R from center
- ★ Work out how fast its orbiting around the galaxy
- ★ Turns out that relevant thing is mass of that part of the galaxy within radius R , $M_{\text{sun}}(<R)$


$$M_{\text{galaxy}}(< R) = \frac{V^2 R}{G}$$


Real measurements



- ★ Orbital velocity stays almost constant as far out as we can track it
 - ★ Means that enclosed mass increases linearly with distance... expected?
 - ★ Mass continues to increase, even beyond the radius where the starlight stops
 - ★ So, in these outer regions of galaxies, the mass isn't luminous...
 - ★ This is **DARK MATTER**.



What is the weight of the Milky Way?

★ Using the formula $M=V^2R/G$, with $v=200$ km/s, $R=6 \times 10^{23}$ cm (that is 200 kpc) and $G=6.7 \times 10^{-8}$ (cgs units) what is the mass of the Milky Way?

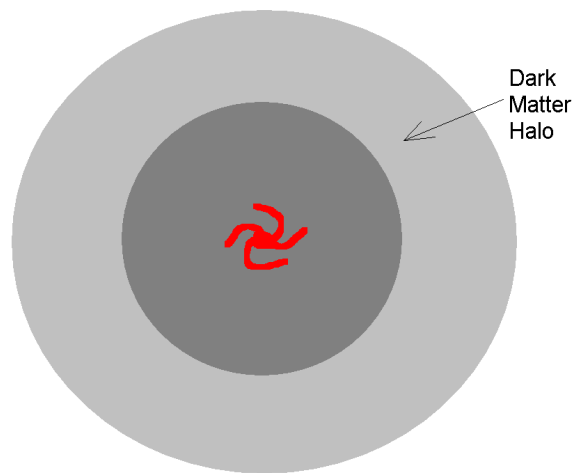
- a) $\sim 4 \times 10^{33}$ grams
- b) $\sim 4 \times 10^{40}$ grams
- c) $\sim 4 \times 10^{45}$ grams
- d) $\sim 4 \times 10^{47}$ grams


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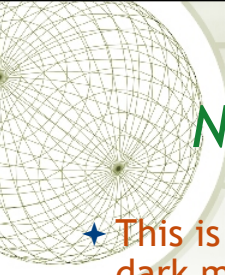


Called a dark matter “halo”





- ★ How big are galaxy halos?
 - ✦ We don't know!
 - ✦ But they might be huge... maybe 10 times bigger than luminous part of the galaxy!
- ★ Add up all the galaxy halos... how much mass would there be?
 - ✦ Uncertain - we don't know how far out galaxy halos go.
 - ✦ Somewhere in range $\Omega_{\text{halos}}=0.1-0.3$



Non-baryonic dark matter

- ★ This is our first evidence for non-baryonic dark matter...
 - ✦ $\Omega_{\text{B}}=0.036$ (nucleosynthesis)
 - ✦ $\Omega_{\text{halos}}=0.1-0.3$ (galaxy rotation curves)
- ★ So, substantially more mass in the galaxy halos than could possibly be due to baryons.
- ★ Suggests a non-baryonic form of matter may exist... something not based on protons and neutrons.

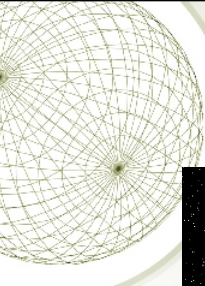


III : MASS OF GALAXY CLUSTERS

★ Galaxy clusters


- ★ Large groups of galaxies
- ★ Bound together by mutual gravitational attraction
- ★ Let's use same arguments as for galaxies (i.e., based on Newton's laws) to measure mass...

$$M_{gal}(< r) \approx V_{gal}^2 R$$



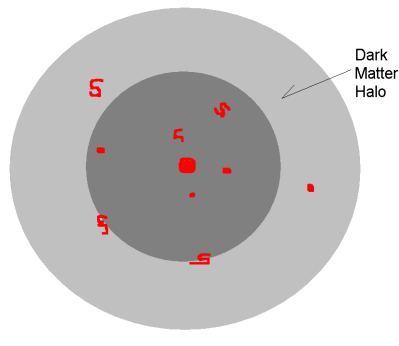
The Virgo cluster...



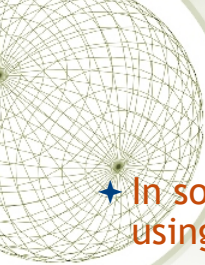


★ Find a similar situation...

- ✦ There is a giant halo of dark matter enveloping the galaxy cluster
- ✦ Probably in addition to the individual halos that the galaxies possess
- ✦ Add up the mass in these cluster halos...
- ✦ $\Omega_{\text{clus}}=0.3$
- ✦ Most of this must be non-baryonic

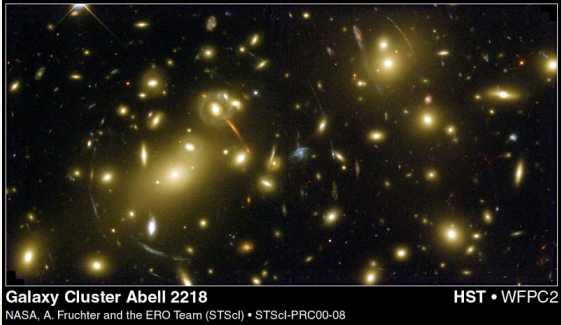


Dark Matter Halo



Gravitational lensing...

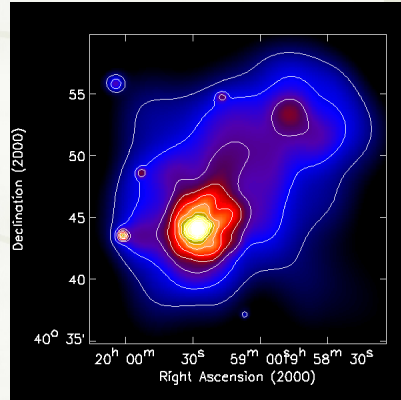
- ★ In some cases, can also measure cluster mass using gravitational lensing.
- ★ Get good agreement with dynamical measurements



Galaxy Cluster Abell 2218 HST • WFPC2
NASA, A. Fruchter and the ERO Team (STScI) • STScI-PRC00-08

Where's the rest of the baryonic matter if its not in stars?

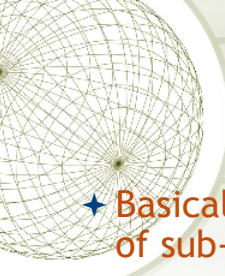
- ★ Some of it may be in very low-mass stars (MACHOs)
- ★ Where's the rest?
 - ✦ The dark matter halo of galaxy clusters traps a lot of hot gas
 - ✦ Gas temperature of 10-100 million K.
 - ✦ Can see it using X-ray telescopes.
 - ✦ Such gas contains a lot of the baryons
- ★ The rest is in "warm" (1 million K) gas in intergalactic space.



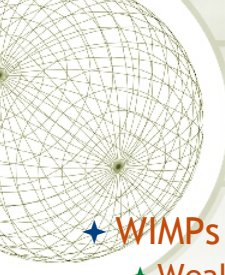
X-ray emission from the hot gas trapped in the Cygnus-A cluster

IV: NON-BARYONIC DARK MATTER

- ★ Recap again...
 - ✦ Nucleosynthesis arguments constrain the density of baryons ($\Omega_B \approx 0.037$)
 - ✦ But there seems to be much more mass in galaxy and cluster halos ($\Omega = 0.1-0.3$)
 - ✦ So, most of the matter in the Universe is not baryonic
- ★ So... what is it?



- ★ Basically, we have to appeal to other kinds of sub-atomic particles.
- ★ Neutrinos (a mundane possibility)
 - ★ Already come across neutrinos when talking about nuclear reactions
 - ★ They are part of the “standard model” of particle physics... they have been detected and studied.
 - ★ Maybe the dark matter is in the form of neutrinos?
 - ★ No... each neutrino has very small mass, and there just are not enough of them to make the dark mass (mass measured only very recently)



- ★ WIMPs
 - ★ Weakly Interacting Massive Particles
 - ★ Generic name for any particle that has a lot of mass, but interacts weakly with normal matter
 - ★ Must be massive, to give required mass
 - ★ Must be weakly interacting, in order to have avoided detection
 - ★ Various possibilities suggested by Particle Physics Theory...
 - ★ Super-symmetric particles
 - ★ Gauge bosons
 - ★ Many experiments currently on-going