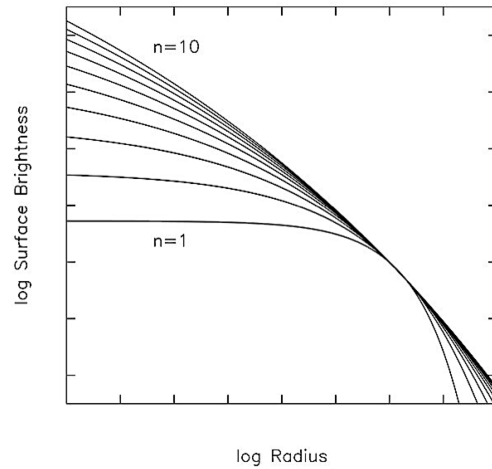


## Descriptions of Galaxy Optical Surface Brightness

- For most massive galaxies a two component description of the surface brightness is a reasonable approximation to the azimuthally averaged data
  - Bulges/spheroids
  - Disks
- The ratio of these two components has wide variation
- Both can be described by a radially symmetric 'Sersic' profile

$$\Sigma(r) = \Sigma(0) \exp(-k [(r/r_e)^{1/n} - 1]);$$

$k \sim 2n - 0.331$  (who called for that!)  
 where  $r_e$  is the half light radius



$$L = 2\pi \int_0^\infty I(R) R dR = \frac{2\pi n \Gamma(2n)}{(\beta_n)^{2n}} I_0 R_e^2,$$

total luminosity of  
 Sersic profile-  $\Gamma$  is  
 the gamma function

## Galaxy Optical Surface Brightness

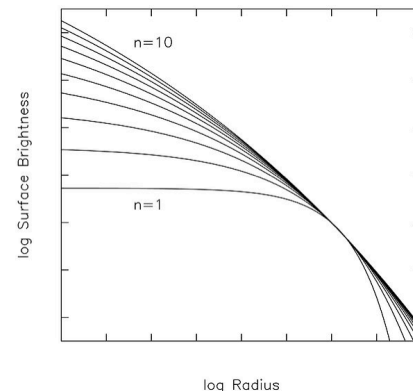
'Sersic' profile (S&G eq 5.13)

$$\Sigma(r) = \Sigma(e) \exp(-k [(r/r_e)^{1/n} - 1])$$

$k \sim 2n - 0.331$  where  $r_e$  is a  
 characteristic scale length and

$\Sigma(e)$  is the intensity at the effective  
 radius  $r_e$  that encloses half the  
 total light

- Disks have  $n \sim 1$  (exponential profile) while spheroids have  $n \sim 2-5$  (a special value is  $n=4$ , the DeVaucouleurs profile)
- Most spirals have a bulge and thus the surface brightness is the sum of 2 Sersic profiles (the bulge usually dominates for small  $r$ )



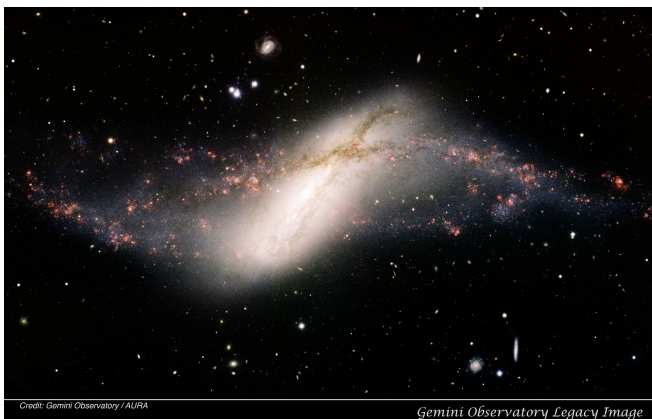
$$L = 2\pi \int_0^\infty I(R) R dR = \frac{2\pi n \Gamma(2n)}{(\beta_n)^{2n}} I_0 R_e^2$$

total luminosity of  
 Sersic profile-  $\Gamma$  is  
 the gamma function  
 $\Gamma(2n) = (2n-1)!$

# Total Luminosity

- $L(< R) = \int_0^R I(R) 2\pi R dR$
- $L(< R) = I(0) R^2 e^{2\pi n e^{b/(b)}^{2n} \Gamma(2n, x)$
- $\Gamma(2n, x)$  Gamma function
- $\Gamma(2n) = (2n-1)!$
- see <https://arxiv.org/pdf/astro-ph/0503176.pdf> for lots of details
- For an exponential ( $n=1$ ) profile, 99.1% of the flux resides within the inner  $4R_e$
- For an  $n=4$  profile, 84.7% of the flux resides with the inner  $4R_e$
- For large values of  $n$  the Sersic model tends to a power-law with slope equal to 5.

- If one express the surface brightness in magnitudes,  $\mu \propto -2.5 \log(I)$ , the Sersic profile can be expressed as
- $\mu(R) = \mu_e + 1.086k[(r/r_e)^{1/n} - 1]$



## Stellar Distribution-radial

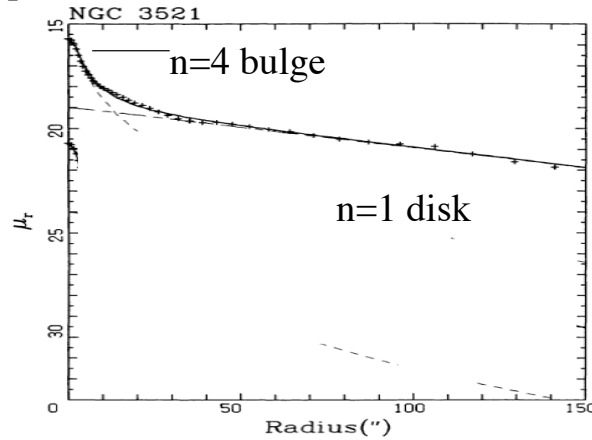
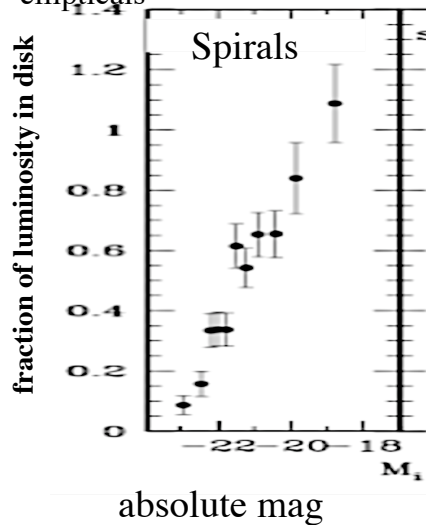
average

- Massive galaxies (spirals and ellipticals) can be described by a '2' component radial profile model:

- disk;  $n \sim 1$
- bulge;  $n \sim 2-5$  ( $n \sim 4$  for giant ellipticals)

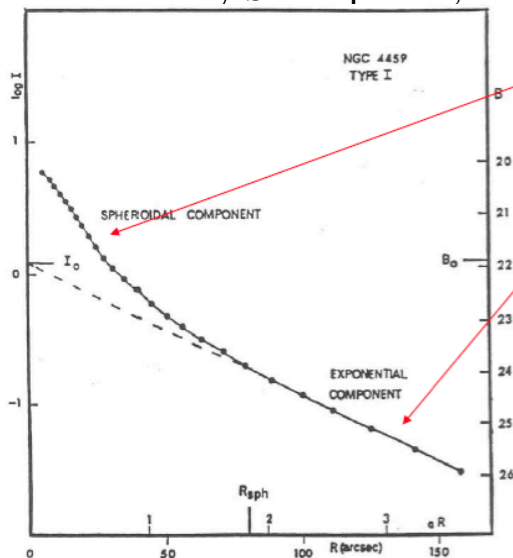
Sersic(1968) profile S+G eq 3.13

More massive galaxies have a higher fraction of their light (mass) in the bulge (and by definition 'earlier' type



## Azimuthally Averaged Light Profiles

- Bulge is more concentrated than the disk: bulge is described by Sersic profile, disk by an exponential profile



$$\log I \propto R^{1/4} \text{ (inner);}$$

$$I(R) = I_0 e^{-\alpha R} \text{ (outer)}$$

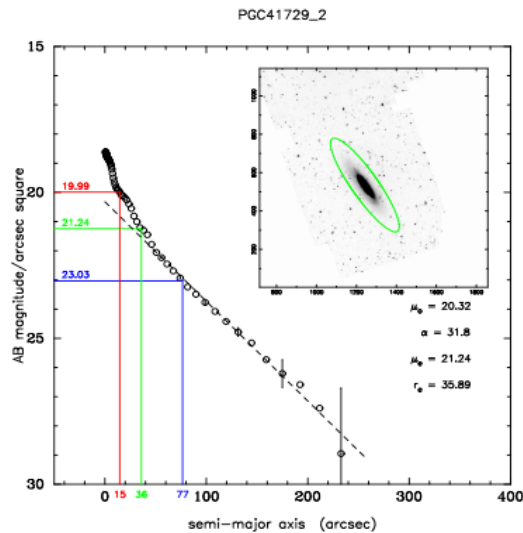
$\alpha$  is the inverse scale height

(Freeman 1970)

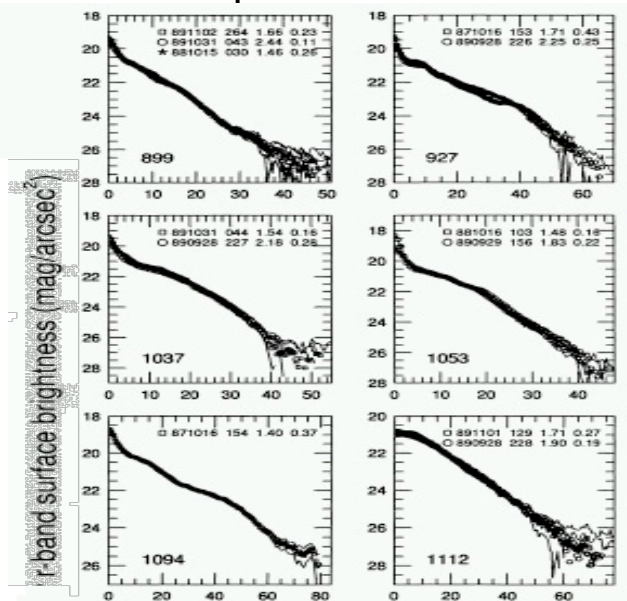
**This is an approximation**, galaxies with strong bars or other non-azimuthally symmetric features will clearly change this

Pure exponentials would be straight lines.

The exponential scale length is a measure of the size of the baryonic disk.- Most of the light is inside 2 scale lengths



Typical disk surface brightness profiles



Courteau, ApJS, 103, 363, 1996

Typical values for the scale length are:

$$1 < h_R < 10 \text{ kpc}$$

$$h_R \sim M_*^{1/3}$$

In many, but not all, spiral galaxies the exponential part of the disk seems to "end" at some radius  $R_{\text{max}} \sim 3 - 5 h_R$ .

Beyond  $R_{\text{max}}$  the surface brightness of the **stars** decreases more rapidly – "edge" of the optically visible galaxy.

The central surface brightness of many spirals is  $\sim$  constant, irrespective of the absolute magnitude of the galaxy!

Presumably this arises from physics of galaxy and /or star formation.



## What's Important So Far

- The class of galaxies called spirals (based on morphology in the optical) has a set of strongly correlated properties (mass, star formation, dust, gas, color) - so there is physics in morphology
- The big bifurcation between color, mass, morphology classification by color, mass, morphology gives similar but NOT identical results
  - At one lower level (e.g sub-divisions in morphology (Sa, Sb, Sc etc) there are also trends.
  - the luminosity function of galaxies is fit by a simple function (Schechter function) which is different for ellipticals and spirals but sums together into a smooth form
  - spirals tend to 'live in the field' low density regions
  - ellipticals in denser regions(morphology density relation- Dressler 1978)

## Summary of Surface Brightness Profiles

- Most galaxies can be well fit with the Sersic profile, spirals have lower values of 'n' for the disk and 2 components to the profile (bulge, disk)
  - Sersic profile 2 asymptotic forms
    - low n ~exponential:  $I(R)=I(0)(\exp[-(R/R_d)])$  where  $R_d$  is the disk scale length  $I(R)=(1/e)I(0)$ ; total flux  $I_{tot}=2\pi R_d^2 I(0)$
    - high n -  $R^{1/4}$  profile
  - deVacouleurs profile (n=4)  $I(R)=I(R_e)(\exp-7.67[(R/R_e)^{1/4}-1]))$
  - $R_e$  is the half light radius

# ESO510-G13



- Beautiful but complex

## Tully-Fisher for Spiral Galaxies: S&G 5.3.3

- Relationship between the speed at which a galaxy rotates,  $V$ , and its optical luminosity  $L_{\text{opt}}$ : (the normalization depends on the band in which one measures the luminosity and the radius at which the velocity is measured)

$$-L_{\text{opt}} \sim A V_{\text{max}}^4$$

- Connects galaxy dynamics to optical luminosity
- Since luminosity depends on distance<sup>2</sup> while rotational velocity does not, this is a way of inferring distances

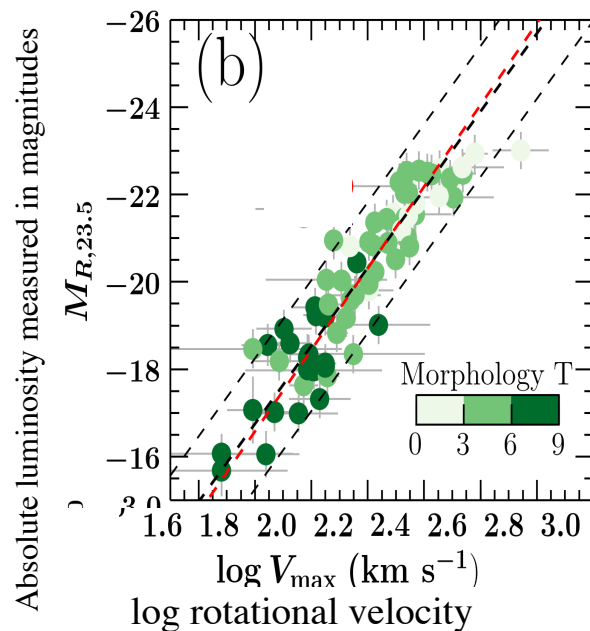


Figure shows the **T-F relation R band**

arXiv:1508.03004v1

Barbosa et al

- System in equilibrium: centripetal force balances gravity
- $GM(r)/r^2 = v_c^2/r$ ; so  $M(r) = v_c^2 r / G$ ; definition of surface density  $\Sigma = L/r$

- If all galaxies are alike and have the same surface densities  $L \sim r^2$
- Further if  $M/L$  is constant  $M \sim L$
- a little algebra gives  $L \sim v_c^2 L^{1/2} \sim v_c^4$
- If galaxies contained no dark matter, we could understand the Tully–Fisher relation fairly easily
- But, since the rotation speed  $V_{\max}$  is set largely by dark matter, while the luminosity comes from stars  
Somehow, the amount of dark matter is coordinated with the luminous mass.

## Tully-Fisher Back of the envelope derivation

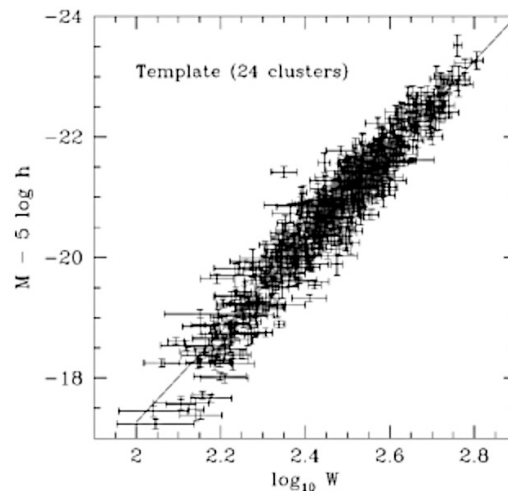


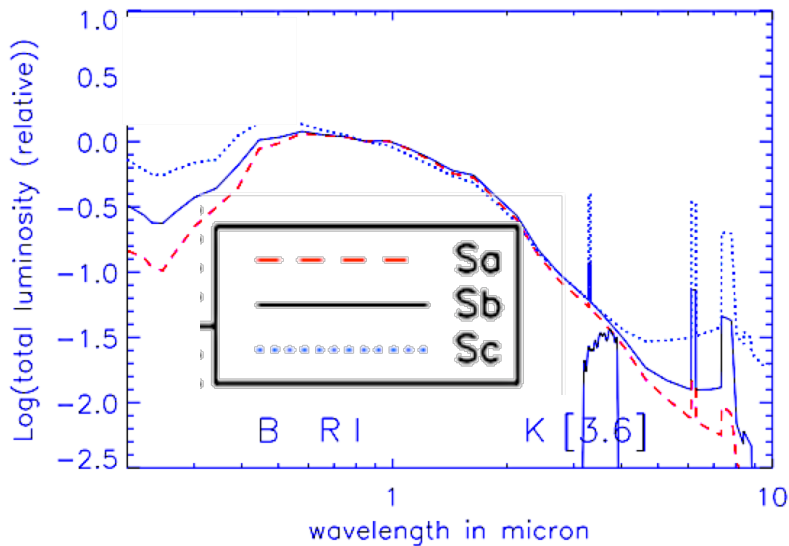
FIG. 1.—Template relation based on 555 galaxies in 24 clusters. The fit is  $-21.00 \pm 0.02 - 7.68 \pm 0.13 (\log W - 2.5)$ .

Giovanelli et al 1997

## New Topic- Galaxy Optical-IR Spectra

## Spiral Galaxy spectra

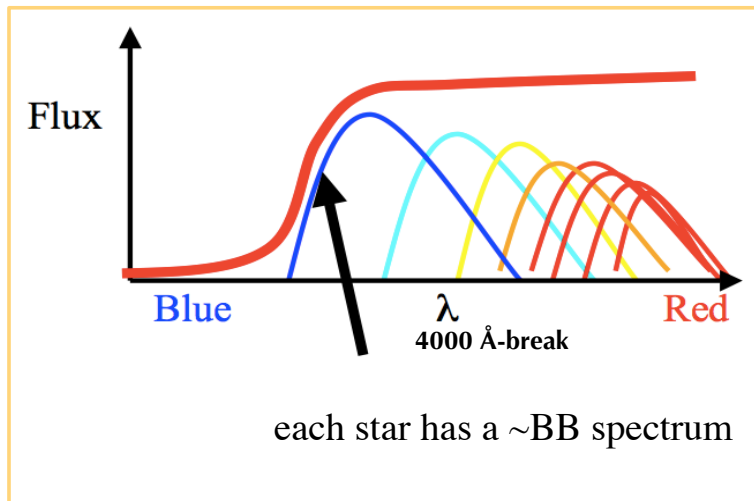
- Galaxies have composite spectra. They integrate contributions from different stars of different stellar populations, gas and the effects of dust
- The overall continuum shape is modulated by the gas, the stars, as well as by the presence of dust.



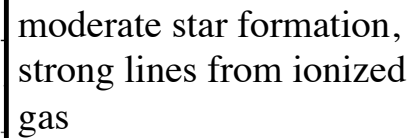
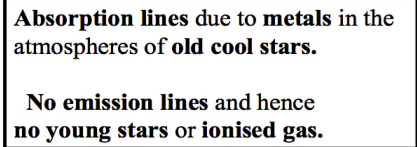
*Spiral* SEDs normalized at 8000Å with emphasis on near IR spectral features (PAHs)

## Galaxy Spectra The Simple Picture

- Continuum: the combination of many Black-Body spectra (from a wide range of stellar types, spanning a range in temperatures, weighted by the IMF) *just happens* to produce a fairly flat overall spectrum



Little star formation,  
little ionized gas



- Connection between morphology and spectrum (S&G fig5.24)

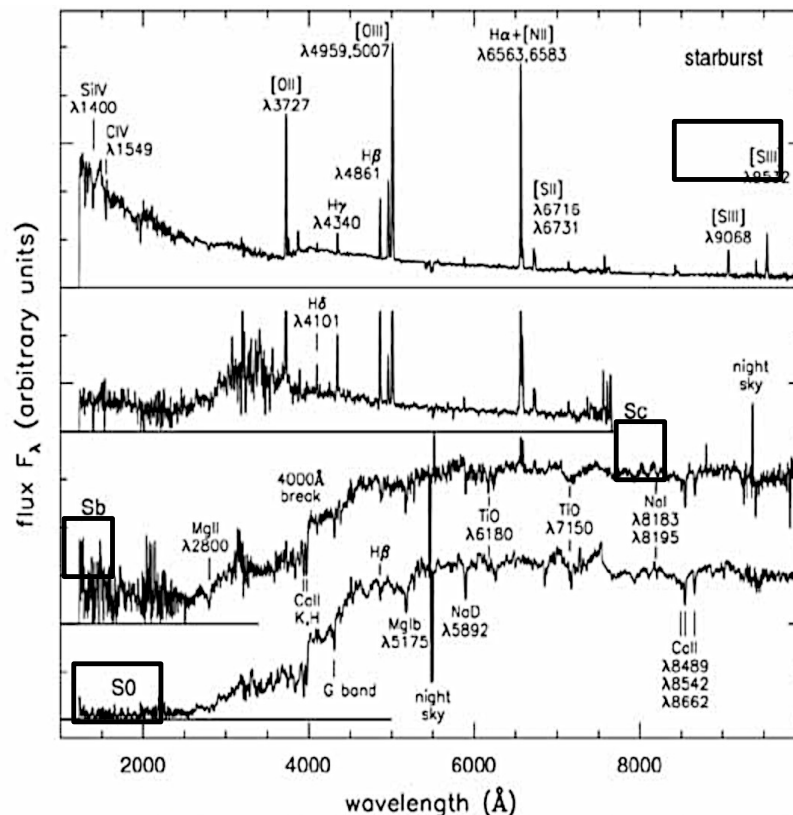


Fig 5.24 (A. Kinney) 'Galaxies in the Universe' Sparke/Gallagher CUP 2007



## Galaxy spectra

- Galaxies have composite spectra. They integrate contributions from different stars of different stellar populations, gas and the effects of dust
- The emission lines trace the ionized gas and its excitation mechanism.
- The absorption lines trace the stellar populations, their ages and metallicities.
- The overall continuum shape is modulated by the gas, the stars, as well as by the presence of dust.
  - color of line is based on g-r color

continuum mostly from stars

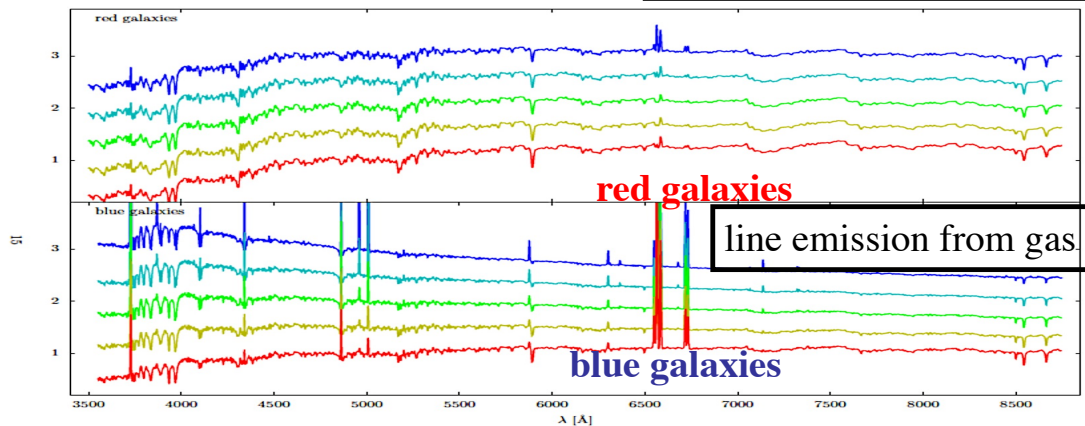
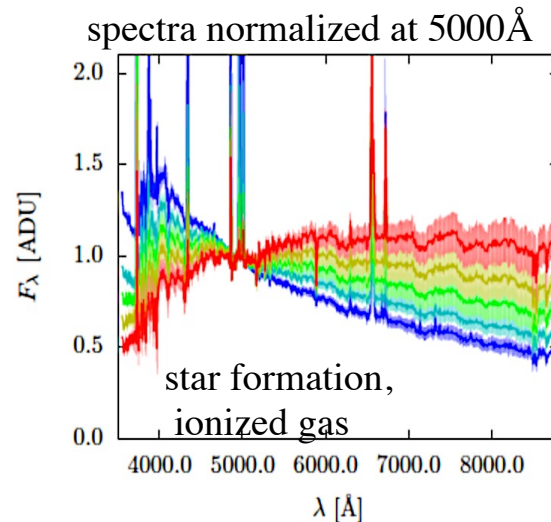
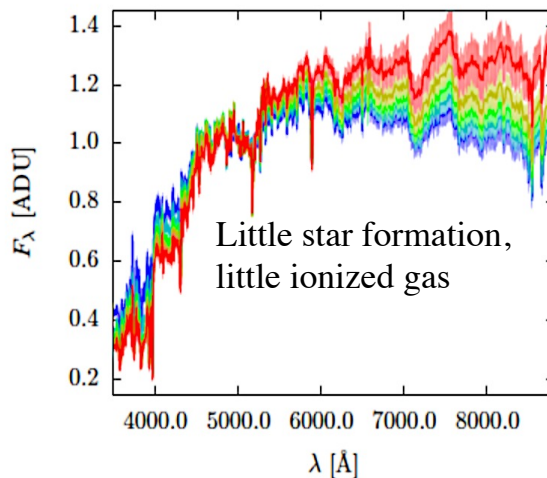


Figure 12: Composite spectra of the refined colour classes as described in Sec. 3.4. The curves are colour-coded from blue (top) to red (bottom) based on the  $g - r$  colour of the galaxies. See the online edition for a colour version of this plot.

## Galaxy spectra

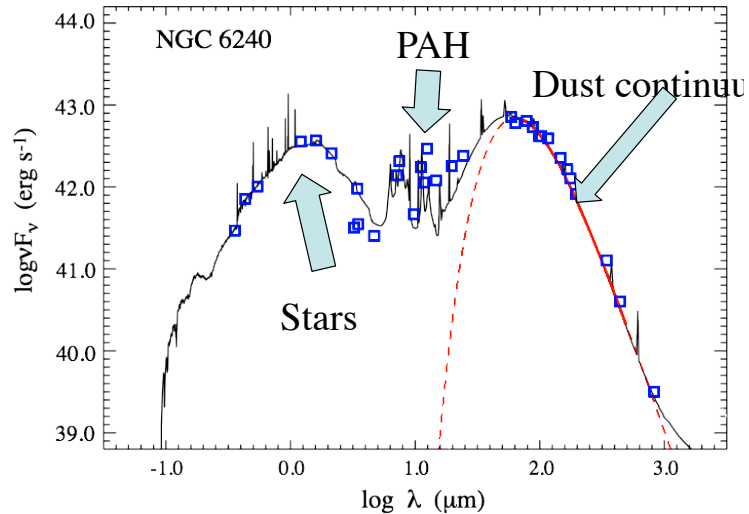
- Sequence of ages of a composite SSP population (star forming-spiral population)
- bulges are dominated by stellar absorption lines and have little 'blue' light
- The star forming galaxies- *almost all spirals at low redshift*, show emission lines (from ionized gas) and much more blue light (especially when they are young)



## Galaxy Spectra -IR

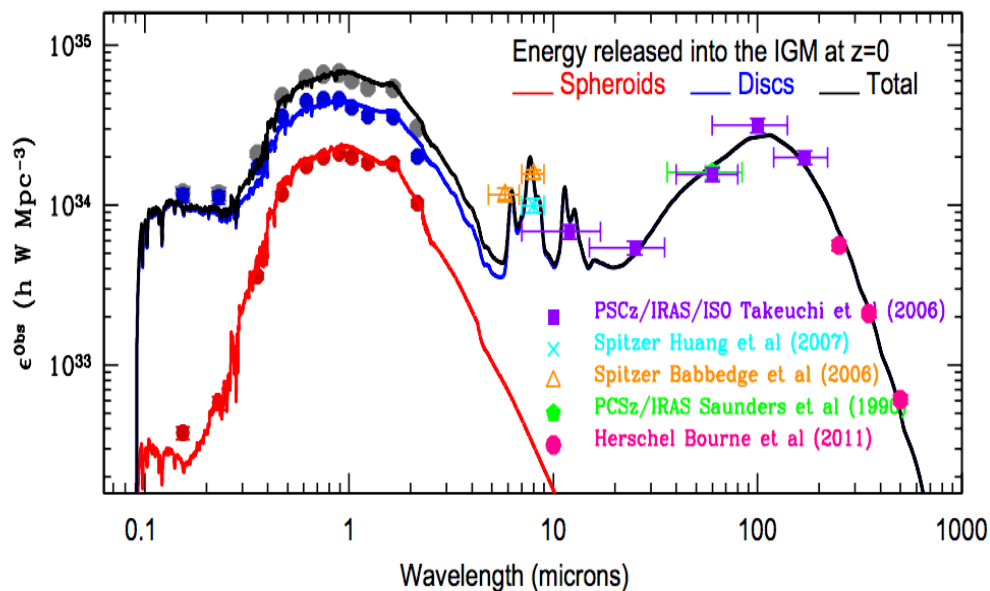
- At  $\lambda > 5\mu$  in most spiral galaxies continuum dominated by emission from dust -there are atomic and molecular features as well
- In many spiral galaxies  $L(\text{opt}) \sim L(\text{IR})$ 
  - dust heated by star light - temperature to which it is heated depends on geometry and the nature of the stars

Dust emission spectrum is a grey body  $L_\lambda = (\epsilon(\lambda)) F_{\text{BB}}$  where  $F_{\text{BB}}$  is the black body function



## Energy Released By Galaxies

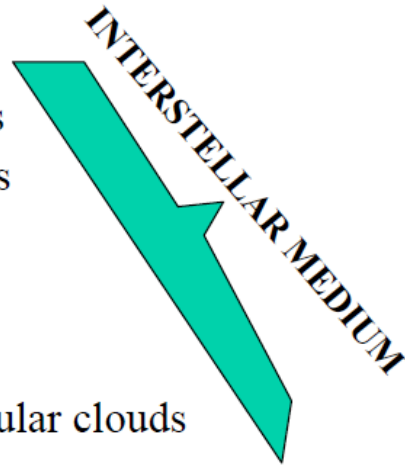
- Extensive galaxy surveys have allowed the measurement of the total energy released by all low  $z$  galaxies across the UV-far IR spectrum  $1.3 \times 10^{35}$  W/ Mpc<sup>3</sup> (Driver 20120; 35-45% of energy generated by stars is absorbed by dust and re-radiated in IR- this occurs predominately in spirals)



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## Composition of 'Average' Spiral

- Stars ~80% of mass
  - DISK ~80% of stars
  - BULGE ~20% of stars
- Gas ~20% of mass
  - atomic gas (“H I”) ~2/3 of gas
  - molecular gas (H<sub>2</sub>) ~1/3 of gas
  - hot, ionized gas (“H II”)
- Dust
  - between stars
  - mostly in spiral arms & molecular clouds



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## Reminder of Big Picture See S&G table 5.1

- Disks :

Metal rich stars and ISM

Nearly circular orbits with little (~5%) random motion & spiral patterns

Both thin and thick components

- Bulge :

Wide range of metals; poor to super-rich stars (only in nuclear regions)

- $V(\text{rot})/\sigma \sim 1$ , so dispersion (random velocity-hot systems) support important.

- Bar/Spiral Patterns/rings :

- Dense 'cold' ISM + star formation

- Stellar Halo :

Very low surface brightness; ~few % total light; little/no rotation

Metal poor stars; GCs, dwarfs; low-density hot gas

- Dark Halo :

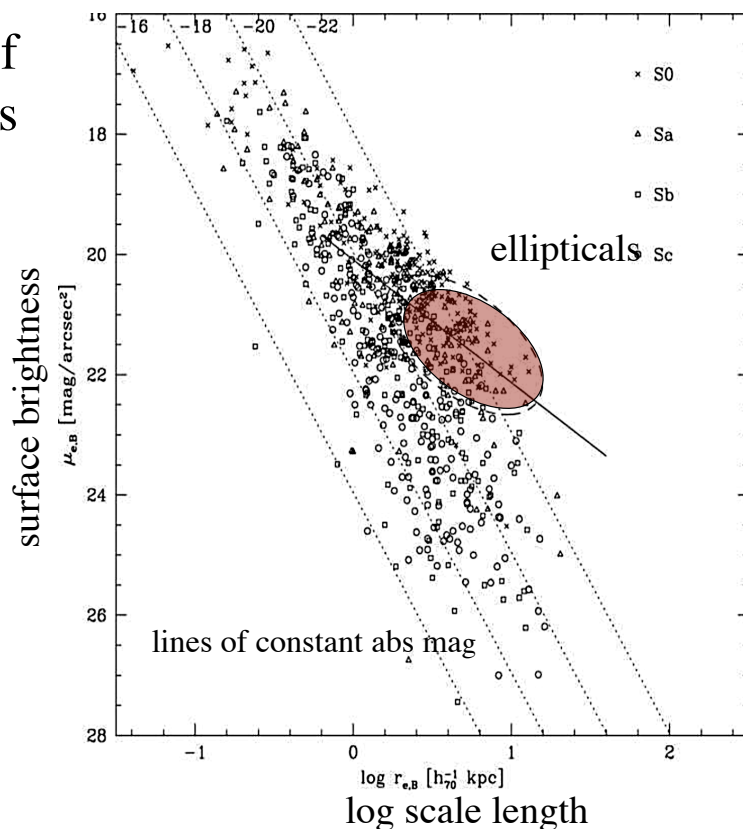
**Dark matter** dominates mass (and potential) outside ~a few scale lengths

## General Patterns- reminder, please review

- Relationship of 'class' (e.g. S0,Sa,Sb..) to physical properties -
- Correlations of surface brightness, size, color, star formation etc etc
- 'Later' types, lower mass, more of baryons in gas, higher specific star formation rates (today):
- Sa -> Sb -> Sc -> Sd in order of decreasing bulge size.
- Patterns
  - More luminous galaxies have larger  $V_{\max}$
  - Earlier Hubble-type galaxies rotate faster for the same L
  - Fraction of DM inside optical radius increases with decreasing  $V_{\max}$
- Large fraction of energy radiated in the IR due to dust
- Spectroscopic signature of gas in spirals in form of emission lines from hydrogen, oxygen etc; gives information about physical conditions (temperature, density, velocity field)

### The properties of Bulges of Spirals

- The bulges of all Hubble types show similar pattern (surface brightness, size, total luminosity) but ellipticals have a smaller range of parameters than spiral bulges.
  - Dwarfs have different bulges (large n values, scale lengths and higher surface brightness)



# Gas Motions

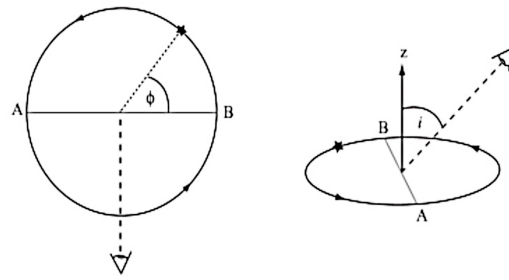
- If there is a well defined disk, inclined at some angle  $i$  to the plane of the sky (inclination) and rotating perpendicular to this angle (fig 5.18 in text)
- 2 sets of coordinates
  - disk of galaxy ( $R, \phi$ )
  - plane of sky ( $\rho, \theta$ )
  - When  $\theta = \phi$  line of nodes
- The measured radial velocity of gas in circular orbits is

$$v_R(\rho, \theta) = v_{\text{system}} + v_R(R, \phi) \sin \phi \sin i + v_\phi(R, \phi) \cos \phi \sin i + v_z(R, \phi) \cos i$$

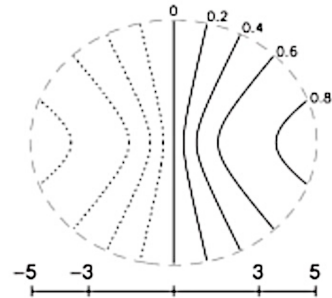
$v_R$  velocity in radial direction

$v_\phi$  angular speed

$v_z$  vertical speed



**Fig. 5.18.** Left, a rotating disk viewed from above. Azimuth  $\phi$ , measured in the disk plane, gives a star's position in its orbit; an observer looks from above the disk, perpendicular to diameter AB. Right, the observer's line of sight makes angle  $i$  with the disk's rotation axis  $z$ .

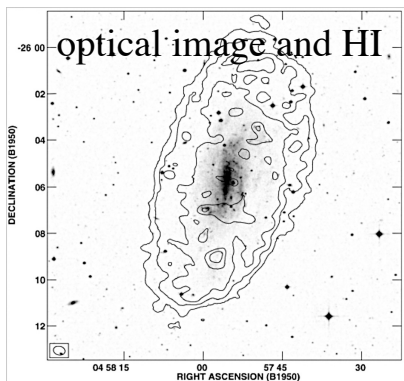
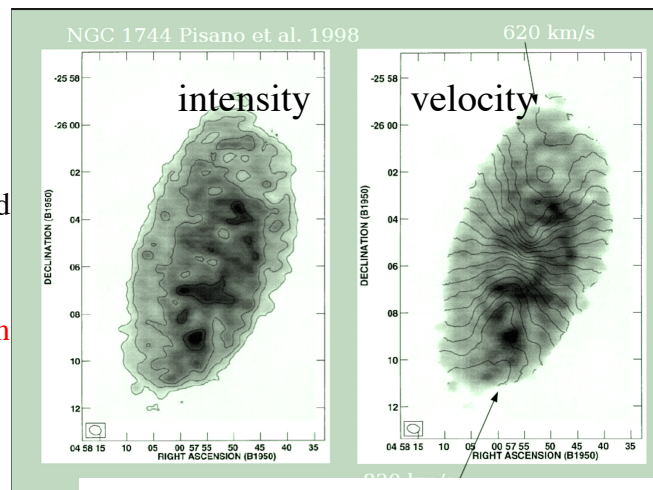


**Fig 5.19**

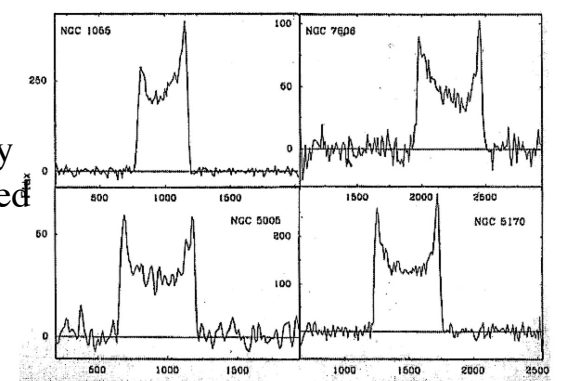
contours of constant  $v_r$ , velocity pattern disk observed at  $i=30$   
negative velocities ----

## HI

- Spirals have large HI disks
    - This gas is optically thin
- This means that we see all the gas and can measure the amount directly from the line intensity
- **HI gas is much more extended than the optical light,**
  - – Gives a unique tracer for the velocity in spiral galaxies



Spatially integrated

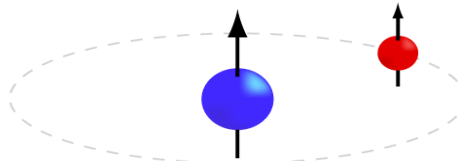




## Physics of 21cm Line

- While Hydrogen is the most abundant element in the ISM, but the symmetric  $H_2$  molecule has no dipole moment and hence does not emit a spectral line at radio frequencies.
- But it is detectable in the 21 cm ( $\lambda=1420.405751$  MHz) hyperfine line, a transition between two energy levels due to the magnetic interaction between the quantized electron and proton spins. When the relative spins change from parallel to antiparallel, a photon is emitted. Collisions excite the line.
  - The equilibrium temperature of cool interstellar HI is determined by the balance of heating and cooling. The primary heat sources are cosmic rays and ionizing photons from hot stars.

<http://www.cv.nrao.edu/course/ast534>



One  $\lambda = 21$  cm photon is emitted when the spins flip from parallel to antiparallel.

## Gas Motions- continued

- Circular disk tilted by an angle  $i$ , projects to an ellipse
- What to look for in the 'spider' plot (see figure C.4 in text)
  - Kinematic major axis - line through nucleus perpendicular to velocity contours- should be aligned to photometric axis if mass is traced by light
  - If  $V(r)$  is flat at large radii outer contours are radial
  - if  $V(r)$  is declining at large radii contours close in a loop
  - spiral arms give perturbations to pattern near arms
  - warped disk (see figure)

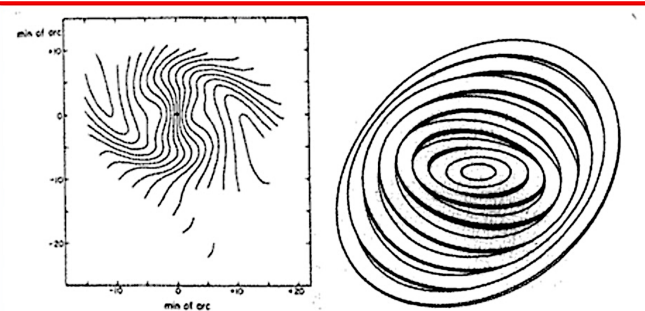


Figure 8.36 A tilted ring model of M83 (right) and the spider diagram predicted by this model (left). [After Rogstad, Lockhart & Wright (1974)]

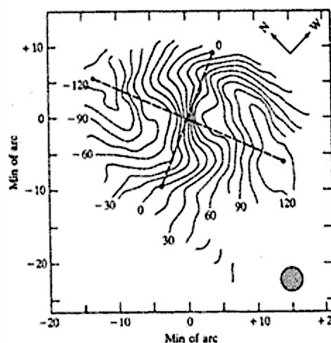
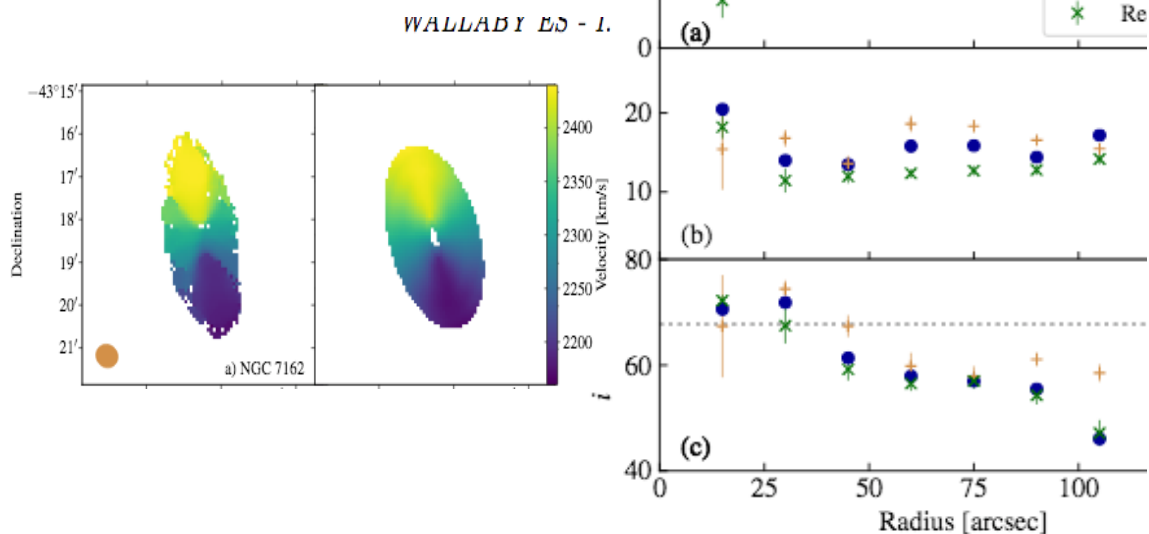


Figure 8.37 The observed spider diagram of M83. [After Rogstad, Lockhart & Wright (1974)]

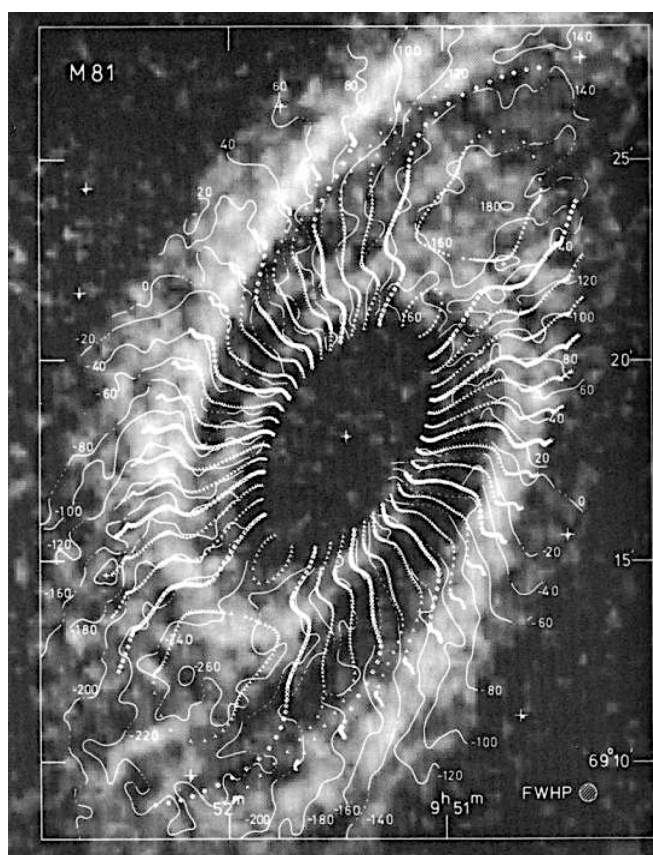
# Tilted Ring Modeling

- Data left panel- model right panel T.N. Reynolds, et al. 2018



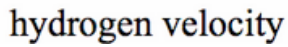
## Gas Motions

- This is what is seen in 'real' galaxies in the motion of HI (fig 5.13 S=G)
- e.g spider diagram is 'A diagram that gives the equations for lines of constant radial velocities as seen for a rotating galaxy inclined to the observer's line of sight.'
- Deviation from Spider plot in M81 shows influence of spiral arms (real density increases-not just light increases)



# NGC5033

- color coded by velocity.

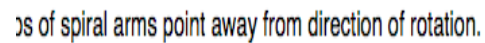


Spiral Arms (sec 11.6 in MBW- sec 5.5.2 in S+G)

- Observational clues

Seen in disks that contain gas, but not in  
gas poor S0 galaxy disks.

- Defined by blue light from hot massive stars. Lifetime is  $\ll$  galactic rotation period.
- When the sense of the galactic rotation is known, the spiral arms trail the rotation.
  - First ingredient for producing spiral arms is differential rotation.



(From P. Armitage)