#### Stellar Populations Physics of Galaxies 2012 part 3



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## Why do we need to know about stars to study galaxies?

- We can't see the vast majority of the mass in galaxies
  - dark matter!
- We only see the "baryons" in galaxies
  - stars
  - gas
- To understand the properties of galaxies, we need to study these components



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#### Stellar atmospheres



- When we look at galaxies in the UV, visible, and NIR, we see (mostly) the atmospheres of their stars
  - their continua: blackbody curves
  - their absorption lines
    - ...and sometimes the emission lines of the gas, if there is star formation or an active galactic nucleus



- Stellar spectra depend mainly on three variables:
  - Effective temperature, where  $L \equiv 4\pi R^2 \sigma T_{eff}^4$
  - To first order, the emitted continuum of a star is a blackbody curve with  $~T\sim T_{\rm eff}$ 
    - and a peak at  $\lambda_{\max} = [2.9/T \,(\mathrm{K})] \,\mathrm{mm}$



Composition: more-or-less the mean abundance of elements heavier than He

 $[Fe/H] \equiv \log_{10}[\epsilon(Fe/H)_*] - \log_{10}[\epsilon(Fe/H)_{\odot}]$ 

where  $\epsilon$ (Fe/H) is the number of Fe atoms relative to the number of H atoms

- causes absorption lines where atoms "intercept" continuum light of star
  - also "line blanketing": when absorption lines "pile up", like below 4000 Å (not to be confused with Balmer decrement...)





flux F<sub>A</sub> (arbitrary units)



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- Surface gravity:  $g \equiv \frac{GM}{R^2}$ 
  - set gas pressure
    - ionization balance (e.g., singly- vs. doubly-ionized Fe)
    - pressure broadened lines (like H lines)
    - abundances of certain molecules (in cool stars: CN, CO, etc.)





## Stellar classification (quickly)

- Morgan-Keenan spectral classes
  - based on ratios of strong absorption lines
  - OBAFGKM(LT)  $\Rightarrow$  T<sub>eff</sub>
  - Luminosity class I-V  $\Rightarrow \log g$ 
    - Sun is G2V star
  - Only works within ~2x of solar abundance; qualitative; discrete steps; no abundance calibration



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## Magnitudes and colors

- Unfortunately, spectra are expensive in telescope time
  - need to spread photons out into lots of pixels takes a lot of time to do!
- Need faster way to get stellar properties



- Consider two objects with fluxes  $f_1$  and  $f_2$
- Then the magnitude difference between these objects is  $m_1 - m_2 = -k \log_{10} \left( \frac{f_1}{f_2} \right)$ • where k = 2.5 means that  $m_1 - m_2 = 5$  when
  - where k = 2.5 means that  $m_1 m_2 = 5$  when  $f_2/f_1 = 100$

• SO 
$$m_1 - m_2 = -2.5 \log_{10} \left( \frac{f_1}{f_2} \right)$$
  
• Or  $\frac{f_1}{f_2} = 10^{-0.4(m_1 - m_2)}$ 





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- This defines the **apparent magnitude**, the magnitude of the flux received by the detector at the telescope, where  $f \equiv \int_0^\infty f_\nu F_\nu R_\nu T_\nu d\nu$ 
  - here
    - $f_{\nu}$  is the flux of the object (in frequency units)
    - $F_{\nu}$  is the transmission of any filter used to isolate the (frequency) region of interest
    - ${}^{\bullet} R_{\nu}$  is the transmission of the telescope, optics, and detector
    - $T_{\nu}$  is the transmission of the atmosphere (if any)



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- Most (but not all) magnitude systems are based on taking a magnitude with respect to a star with a known (or predefined) magnitude
  - the "Vega" system defines a set of AOV stars as having apparent magnitude 0 in *all* bands of a system (see below)
  - So to get a "magnitude on system X", one observes stars with known magnitudes and *calibrates* the "instrumental magnitudes" onto the "standard system"



- Some useful properties and "factoids" about magnitudes...
  - The magnitude system is roughly based on *natural* logarithms:  $m_1 - m_2 = 0.921 \ln(f_1/f_2)$
  - If  $\Delta f \ll 1$ , then  $\Delta m = m_2 m_1 \approx 1.086 \Delta f$ 
    - so the magnitude difference between two objects of nearly-equal brightness is equal to the fractional difference in their brightnesses – i.e., a difference of 0.1 magnitudes is ~10% in brightness
  - A factor of 2 difference in brightness is a difference of 0.75 magnitudes



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- We define the color of an object as the magnitude difference of the object in two different filters ("bandpasses")
  - if the filters are X and Y, then the color (X-Y) is

$$(X - Y) \equiv m_X - m_Y = \text{const.} - 2.5 \log \frac{\int_0^\infty d\lambda S_\lambda(X) f_\lambda}{\int_0^\infty d\lambda S_\lambda(Y) f_\lambda}$$
$$= \text{const.} - 2.5 \log \frac{f_X}{f_Y}$$

• where  $S_{\lambda}$  is the combined telescope-detector-filter sensitivity

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16

## Two common magnitude systems



- Notice that stars of different temperatures have very different spectra, so they have different fluxes through the filters
  - therefore they have different colors
  - and therefore well-chosen colors can be good
     temperature indicators
    - problems: calibration is tricky requires good stellar radii; line blanketing makes bands bluer than ~V sensitive to [Fe/H] and log g



# Apparent to absolute magnitudes

strictly true only if M is constant, but this is almost true on the giant branch.

- At fixed effective temperature, stars with lower log g must be bigger, since  $g\equiv \frac{GM}{R^2}$ 
  - so they must have higher luminosity, since  $L \equiv 4\pi R^2 \sigma T_{\rm eff}^4$
- But we measure the flux, not the luminosity:  $F = \frac{L}{4\pi D^2}$
- so we need the distance D to the stars



- We will come back to how to determine distances in the next lecture. In the meantime...
- We receive flux *f* at our telescopes from an object at distance *d*. If we wanted instead to know what the flux *F* is of that object if it were at distance *D*, then

$$f = \left(\frac{D}{d}\right)^2 F$$

The difference in magnitudes m of f at d and M of F at
 D is then

$$m - M = -2.5 \log\left(\frac{f}{F}\right) = 5 \log\left(\frac{d}{D}\right)$$

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Now, we always pick D to be 10 parsecs (10 pc), so if d is measured in parsecs, then

$$m - M = 5\log(d[\mathrm{pc}]) - 5$$

• If d is measured in  $10^6$  pc=1 Mpc, then

$$m - M = 5\log(d[Mpc]) + 25$$

- m-M is called the **distance modulus** and is sometimes written  $\mu=m-M$
- ...and M is called the absolute magnitude



### Color-magnitude diagrams

- By combining preciselymeasured distances with apparent magnitudes and colors, we can plot a
   color-magnitude diagram (CMD) of stars
  - This CMD is for stars within 100 pc of the Sun with accurate distances and colors



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- Note!
  - A Hertzsprung-Russell diagram is a plot of luminosity as a function of effective temperature
  - A color-magnitude diagram is a plot of magnitude as a function of color
  - They are not the same!
    - The conversion from color to temperature depends on knowing the *radii* of stars, which (as mentioned) are difficult to measure!
    - Magnitude ≠ luminosity unless you know the distance and the *bolometric correction*, which depends on stellar type (or color)



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- The local CMD is made up of stars of many ages (we'll return to this point!)
- When we look at an object like a globular cluster, we see a very distinct pattern



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### Evolutionary timescales

- Stars burn hydrogen into helium for most of their lifetimes, until they exhaust the H in their cores
  - How long does this take?
    - Let's call *E* the amount of energy released by H burning during its *main-sequence lifetime*  $\tau_{\rm MS}$
    - If the star's luminosity on the main sequence is L, then  $E=L\tau_{\rm MS}$
    - So if we can determine *E*, we can determine  $\tau_{\rm MS}$



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- Now, the amount of energy released by converting a mass dM of H into He is  $dE=0.007c^2dM$
- So if a fraction  $\alpha$  of the total mass of the star M is burned into He before core H-exhaustion, then  $E=0.007c^2 \alpha M$
- so the main-sequence lifetime is  $\tau_{\rm MS} = 0.007 \alpha M c^2 / L$
- Typically,  $\alpha = 0.1$ , so  $\tau_{\rm MS} = 10M/M_{\odot}(L/L_{\odot})^{-1}$  Gyr



- It is straightforward to work out from the equations of stellar structure that  $L \propto M^4$  over a good chunk of the main sequence (for stars near the solar composition; this is also true observationally!)
- Then finally we have the main-sequence lifetime as a function of mass:  $\tau_{\rm MS} = 10 A (M/M_{\odot})^{-3} \, {\rm Gyr}$ 
  - where A is a constant of ~1
- So a star ten times the mass of the sun lives for 1/1000 of the time: 10 Myr!



- The main-sequence lifetime is a crucial timescale: it is a clock
  - By measuring the magnitude and color of the main sequence turnoff (MSTO or just TO) we can determine the age of a stellar population – and therefore something about its evolution
  - The brighter and bluer the MSTO, the younger the population
    - brighter, bluer MS stars are more massive



### **Open or Galactic Clusters**

- "Open" or Galactic clusters are low mass, relatively small (~10 pc diameter) clusters of stars in the Galactic disk containing <10<sup>3</sup> stars
  - The Pleiades cluster is a good example of an open cluster
    - the "fuzziness" is starlight reflected from interstellar dust





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- Because open clusters live in the disk of our Milky Way, they are subject to strong tides and shearing motions
- Because they are so small and contain few stars, they also evaporate quickly
- Therefore they do not live very long unless they are very massive — so most of them are quite *young*



30

- All stars in an open cluster
  - are at the same distance
  - formed at the same time
  - have the same composition
- Very useful for testing stellar evolution models!





- They are also very useful for studying the evolution of the properties of the MW's disk
  - Which of these clusters is the youngest?
  - Which is the oldest?





#### Globular clusters

Globular clusters are named for their spherical shape and contain  $\sim 10^4$ - $10^6$  stars and are bigger than open clusters, with diameters of 20-100 pc

In the Milky Way, *all* globular clusters are **old**: >10 Gyr!

M15 imaged with JKT at La Palma core of M15 observed with HST

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### Globular cluster CMDs

- As all MW GCs are old, their CMDs are very similar. They vary primarily due to composition differences
  - "metallicity" [Fe/H]
  - He content
  - variations of other elements
- Age is an important but secondary consideration



## Isochrones: "single burst" stellar populations

- Take a set of stellar
   models all with the same
   age and same
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   different masses
  - the resulting track in an HR diagram or a CMD is called an *isochrone*



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- When populations get old, the isochrones "pile up" at very similar luminosities and temperatures
  - It is easy to determine ages for **young** populations
  - ...but not for old populations!
    - "Age dating" GCs is difficult!



### The effect of metallicity

- Stellar temperatures and luminosities also depend on composition at fixed age
  - This is an *opacity* effect: more metals mean more absorption, especially in the blue (it's reradiated into the IR), so stars become cooler (redder) and dimmer



### The effect of metallicity



 Putting all of this together, the absolute V magnitude of the MSTO varies as

 $M_V(MSTO) = 2.7 \log(t/Gyr) + 0.3 [Fe/H] + 1.4$ 

- Uncertainties:
  - Difficult to measure the location of the MSTO, as the isochrones are ~vertical
  - Distance errors cause big age errors:
    - 10% distance error → 0.2 mag error in distance modulus → 0.2 mag uncertainty in MSTO magnitude → 20% error in age



 faculty of mathematics and natural sciences  Globular clusters in the Milky Way are generally very old (>10 Gyr), with only a few younger, metalrich globular clusters



## The age-metallicity degeneracy

- Because both age and metallicity affect isochrones, it can be very difficult to separate their effects on single-burst stellar populations
- Because the *colors* of an unresolved stellar population come from <u>both</u> the giant branch and the MS, colors are **not useful** to determine the ages of "old" populations



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## The luminosity function

- At a given point in the galaxy, the number of stars will vary, with both luminous and faint stars
  - Consider a number dN of stars with absolute magnitudes in the range (M, M+dM) in the volume element  $d^3\mathbf{x}$  around the point **x**:

$$dN = \Phi(M, \mathbf{x}) \, dM \, d^3 \mathbf{x}$$



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- Now let's assume that the *mix* of stars of different luminosities is independent of location (not always true...):
  - Then we can separate  $\Phi(M, \mathbf{x})$  into two functions,  $\Phi(M)$ and  $\nu(\mathbf{x})$ :  $dN = [\Phi(M) dM][\nu(\mathbf{x}) d^3\mathbf{x}]$
  - We call  $\Phi(M)$  the **luminosity function**, the relative fraction of stars of different luminosities, while  $\nu(\mathbf{x})$  is the total number density of stars at  $\mathbf{x}$ .



- Note that we will encounter and use the concept of luminosity functions even when we talk about galaxies
  - In this case we generalize  $\Phi(M)$  to mean the relative fraction of galaxies with different luminosities and  $\nu(\mathbf{x})$  to be the number of density of galaxies



- Let's consider again the local stars observed by Hipparcos within 100 рс
  - Hipparcos was *targeted* on stars with  $m_V < 8$
  - So we can construct an LF by writing

$$\Phi(M_V)dM = \frac{dN}{V_{\text{max}}}$$

where  $V_{\text{max}}$  is the volume over which stars with  $M_V$  could be seen



45



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- This is the result (in black). Note the following:
  - Most of the stars are **faint**: peak is at M<sub>V</sub>~14
  - If we weight by the *luminosity* of the stars, nearly all of the light is in **bright** stars: peak is at M<sub>V</sub>~1
  - If we weight by the mass of the stars, most of the stellar mass is in **low-mass** stars: over range 3<M<sub>V</sub><15</li>



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- Another interesting result is the mass-to-light ratio of stars in the Solar Neighborhood:
  - the V-band luminosity density is  $0.053 L_{\odot} \, \mathrm{pc}^{-3}$
  - the mass density is (including white dwarfs)  $0.039 M_{\odot}\,{
    m pc}^{-3}$
  - combining, the mass-to-light ratio in solar units is

 $M/L_V \sim 0.67\,M_\odot/L_\odot$ 

this is a *lower limit* to the total mass per unit luminosity (in a given band), because we haven't included the dark matter – which we must do in a different way...



- Note that what we've defined here is the present-day luminosity function (PDLF)
  - this is the LF we see after the high-mass stars have evolved away



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## The initial mass function: IMF

- A critical input for stellar population models crucial to understand the formation and evolution of galaxies is the initial mass function
  - specifies the distribution of mass in stars *immediately* after a star formation event: the number of stars dN with masses between  $\mathcal{M}$  and  $\mathcal{M}+d\mathcal{M}$  is

 $dN = N_0 \xi(\mathcal{M}) d\mathcal{M}$ 

• We normalize  $\xi(\mathcal{M})$  such that  $N_0$  is the total number of solar masses formed in the event:

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- To determine  $\xi(\mathcal{M})$ , we need to determine dN immediately after a star-formation event to get the *initial luminosity function*  $\Phi_0$ : remember that  $dN = \Phi(M) dM$ 
  - if all the stars *just* formed in one burst: no correction



- If that's not the case, but the system has been forming stars at a *constant* rate (roughly true for the MW disk), then  $\Phi_0(M) = \Phi(M) \times \begin{cases} t/\tau_{\rm MS} & \text{for } \tau_{\rm MS}(M) < t \\ 1 & \text{otherwise} \end{cases}$ 
  - The factor  $t/\tau_{\rm MS}$  corrects for the fact that we only see stars of magnitude *M* that formed in the last fraction  $\tau_{\rm MS}/t$ of the population's life
- Now we can determine  $\xi(\mathcal{M})$ :

$$\xi(\mathcal{M}) = \frac{dM}{d\mathcal{M}} \Phi_0[M(\mathcal{M})]$$



- The function  $M(\mathcal{M})$ specifies the relation between stellar mass and absolute magnitude
  - unfortunately, you also need the derivative of this function...





The simplest (and still commonly used) IMF is that inferred by Salpeter (1955), which is a *power-law*:

 $\xi(\mathcal{M}) \propto \mathcal{M}^{-2.35}$ 

- note that you often see the exponent as –1.35, but this is a different definition of the IMF, in log  $\mathcal M$  instead of (linear)  $\mathcal M$
- In reality, we know that the low-mass IMF must be *flat* or even *decline* with decreasing mass, at least in the Solar Neighborhood



- This has led to a number of different parameterizations of the IMF...
  - Salpeter, Kroupa, and Chabrier are the most commonly-used IMFs today



- The big question: is the IMF universal?
  - Nearly everyone assumes so... but this may not be true....



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## The evolution of stellar populations

- Stars with masses  $<1.5 M_{\odot}$  live for >2.5 Gyr (at solar) abundance) and put out most of their energy after the **MSTO** 
  - for instance, a 1 M<sub> $\odot$ </sub> star puts out  $E_{MS}$ ~10.8 L<sub> $\odot$ </sub> Gyr on the MS and  $E_{GB}$ ~24 L<sub>o</sub> Gyr in the post-MS (RGB, HB, AGB) phases



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 If stars of mass M emit a total energy of E<sub>GB</sub> on the giant branch, then the luminosity of the population will be

$$L \approx \left( E_{\rm GB} \frac{dN}{d\mathcal{M}} \right)_{\mathcal{M}_{\rm GB}} \left| \frac{d\mathcal{M}_{\rm GB}}{dt} \right|$$

this is the energy released on the giant branch per star times the change in the number of stars per unit time

For these low-mass stars, the MS lifetimes are

$$\frac{\tau_{\rm MS}}{10 \,{\rm Gyr}} \approx \left(\frac{\mathcal{M}}{M_{\odot}}\right)^{-3}$$
Note that 6F lifetimes are 10% of MS lifetimes, so the range of masses on the 6F is small ---- roughly that of the MSTO plus a very small amount
or
$$\frac{\mathcal{M}_{\rm GB}}{M_{\odot}} \approx \left(\frac{\tau_{\rm MS}}{10 \,{\rm Gyr}}\right)^{-1/3}$$
and so
$$\frac{d\mathcal{M}}{dt} \approx -\frac{1}{3} \left(\frac{\mathcal{M}_{\rm GB}}{M_{\odot}}\right)^4 \left(\frac{M_{\odot}}{10 \,{\rm Gyr}}\right)$$
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- Now, if we take the IMF to be a power-law with  $\alpha \leq -2.35$  around  $\mathcal{M}_{\text{GB}}$ , then  $dN/d\mathcal{M} \approx K(\mathcal{M}/M_{\odot})^{-\alpha}$
- And the luminosity is then

$$L \approx \frac{KM_{\odot}E_{\rm GB}(\mathcal{M}_{\rm GB})}{30\,{\rm Gyr}} \left(\frac{\mathcal{M}_{\rm GB}}{M_{\odot}}\right)^{4-\alpha}$$

Finally, we can differentiate L to find

$$\frac{d\ln L}{dt} \approx \left[\frac{d\ln E_{\rm GB}}{d\ln \mathcal{M}_{\rm GB}} + (4-\alpha)\right] \frac{d\ln \mathcal{M}_{\rm GB}}{dt}$$

$$\approx 0.3\alpha - \left[1.3 + 0.3\frac{d\ln E_{\rm GB}}{d\ln \mathcal{M}_{\rm GB}}\right] \qquad \text{take the log of the 2nd eq.}$$
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This is strikingly close to the expression found by Tinsley & Gunn (1976):  $(d \ln L/dt) \approx 0.3\alpha - 1.3$ 



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- So as long as α<4, then the luminosity of a coeval population decreases with time</p>
  - in other words, in the absence of star formation, galaxies (and star clusters) get fainter with time!



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- Stellar population models support this (using Salpeter IMFs)
  - note also that populations get redder with age, as expected!



Spectra do the same thing, of course...





- But watch out for the dreaded age-metallicity degeneracy!
- Two spectra with
  - 5 Gyr, [Fe/H]=-0.4
  - 15 Gyr, [Fe/H]=-0.7
- Can you tell the difference?



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