

Nearly Normal Galaxies 3: Spiral Galaxies

- Many of the properties of spiral galaxies have been previously discussed
- Star formation in galaxies, much of which is occurring in spiral galaxies, will be discussed in the next section
- **Present focus:** structure of spiral galaxies and dynamics of disk structure

Review of Properties Previously Discussed

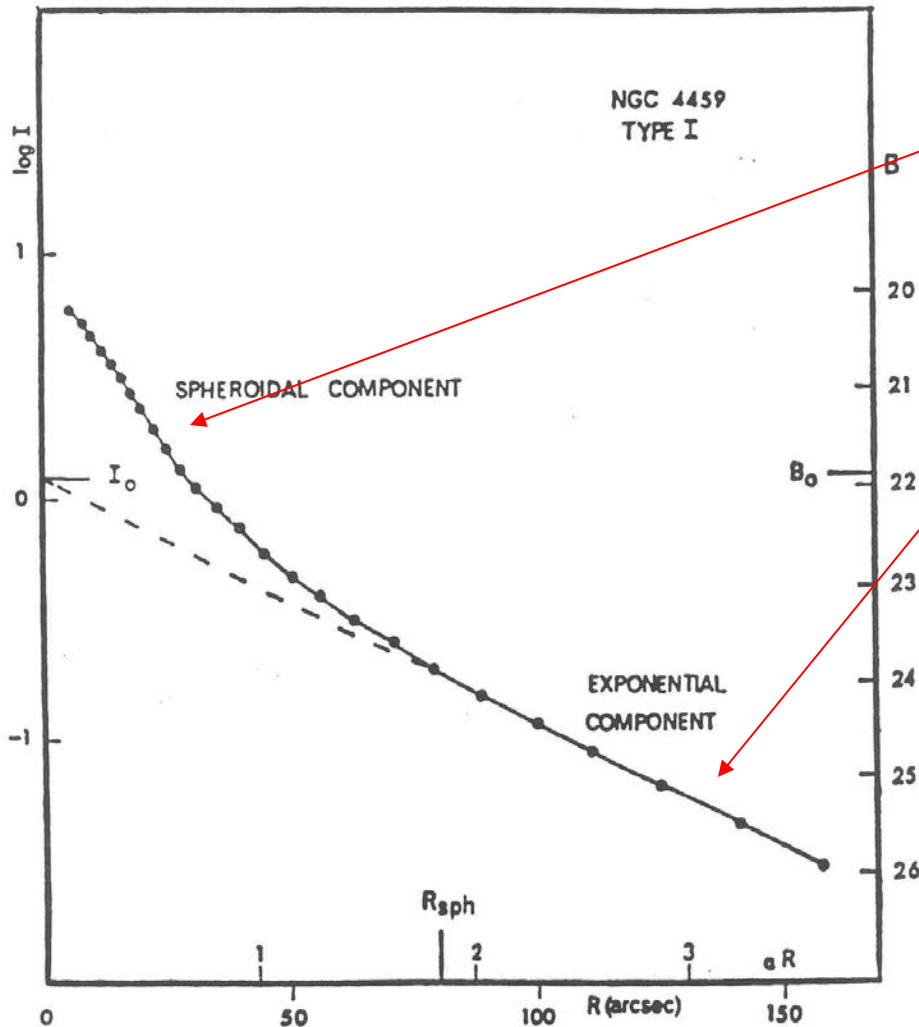
- Spiral galaxies are comprised of a bulge & disk component
- Bulge → old stars Disk → young stars
- The disk contains a large quantity of gas & dust
- $M_B \sim -18$ to -24
- $M / L_V \sim 4$
- Disks are cold (rotationally supported) may be important to maintain spiral structure
- The rotation curves of spiral galaxies rise like a solid body in the central regions, then flatten out (i.e., $v(r) = \text{constant}$). This flattening is due to the presence of a dark matter halo.

Trends with Hubble Type (Previously discussed)

- Total luminosity \downarrow with ST (Sa \rightarrow Sc)
- $M / L_B \downarrow$ with ST (i.e., young stars have low M / L_B)
- $M(\text{HI}) / M(\text{total}) \uparrow$ with ST (S0 \rightarrow Sm, Irr)
- $M / L_B \downarrow$ as $(B - V) \downarrow$ (i.e., because red stars = early type & blue stars = late type)
- Bulge / Disk \uparrow with increasing Hubble Type
- Tightness of the spiral arms \downarrow with increasing Hubble Type
- Degree to which the arms are resolved into stars & individual emission nebulae (HII regions) \uparrow with Hubble Type

Profiles

The profiles of spiral galaxies are a combination of an Inner $r^{1/4}$ - law bulge & an outer exponential disk,



$$\log I \propto R^{1/4} \quad (\text{inner});$$

$$I(R) = I_0 e^{-\alpha R} \quad (\text{outer})$$

Once again, α is the inverse scale height

(Freeman 1970)

$\alpha^{-1} \downarrow$ as $S0 \rightarrow Im$

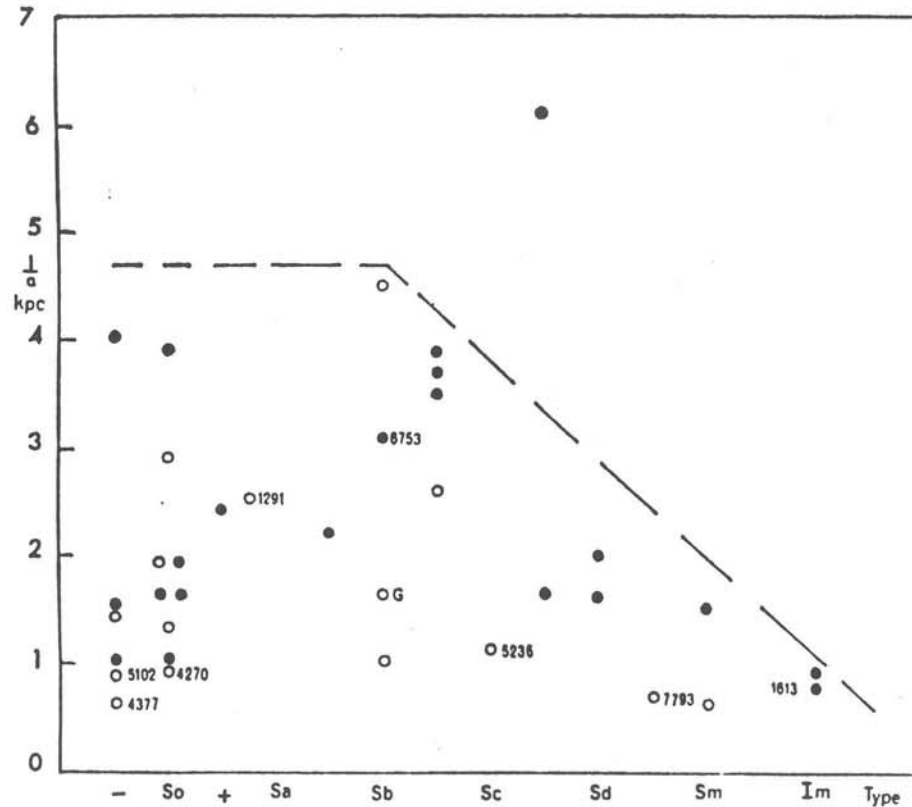


FIG. 6.—Length scale α^{-1} (kpc) for the exponential disks of thirty-six galaxies against their type. NGC numbers are shown for systems defined in Figure 5. *Filled circles*, Type I luminosity profile; *open circles*, Type II luminosity profile (see Fig. 1). *Broken line*, apparent upper envelope. *G* denotes an estimate for the Galaxy.

$$\alpha^{-1} \approx 1 - 5 \text{ kpc}$$

(Freeman 1970)

Intrinsic Blue Surface Brightness

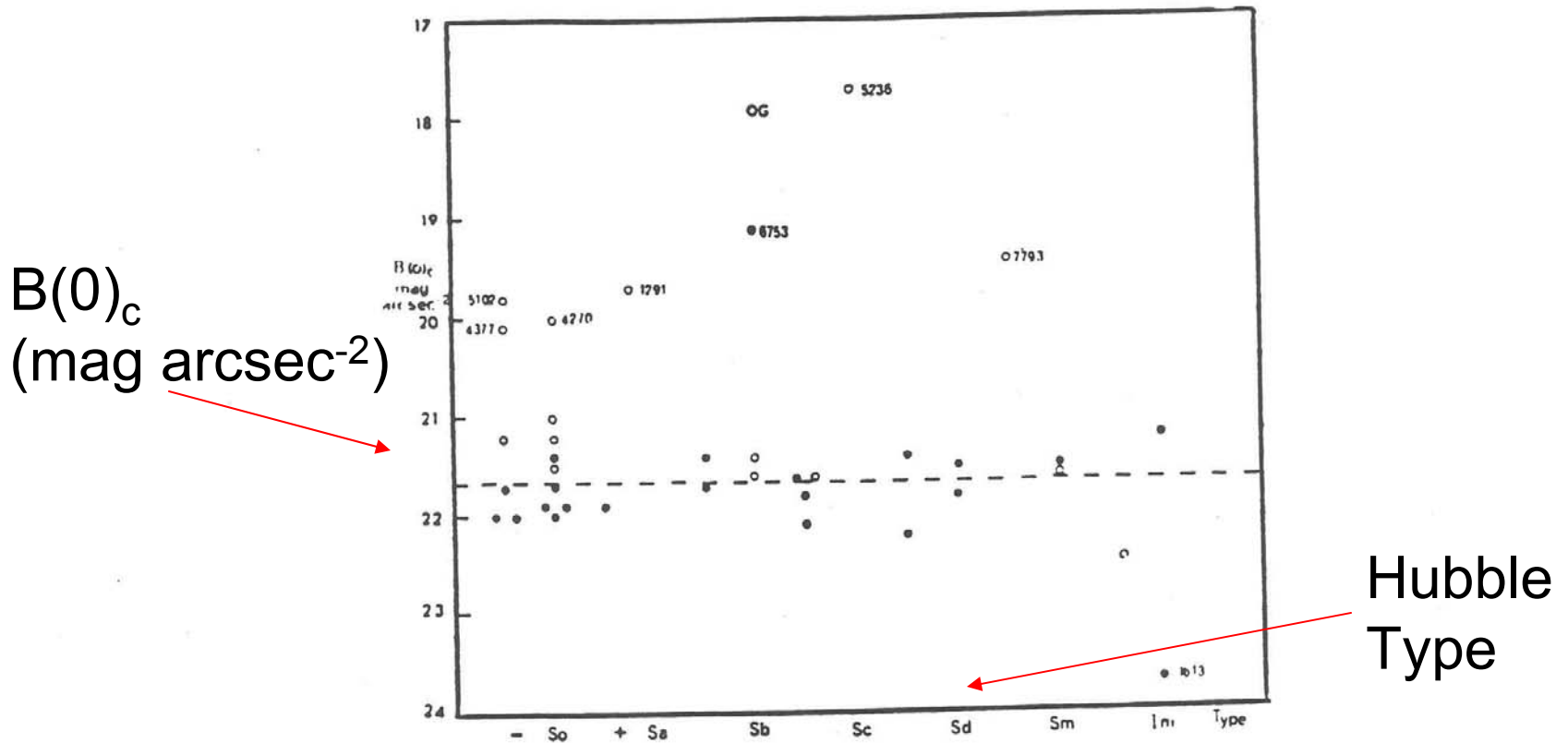


FIG. 5.—Intrinsic distance-independent blue-light luminosity scale $B(0)_c$ for the exponential disks of thirty-six galaxies against their morphological type. Broken line at $B(0)_c = 21.65$ is the mean for twenty-eight galaxies. NGC numbers are shown for the other eight. G denotes an estimate for the Galaxy. Filled circles, Type I luminosity profile; open circles, Type II luminosity profile (see Fig. 1).

$B(0)_c \approx \text{constant.}$ We will return to this soon.

(Freeman 1970)

Departures from an Exponential Disk Profile

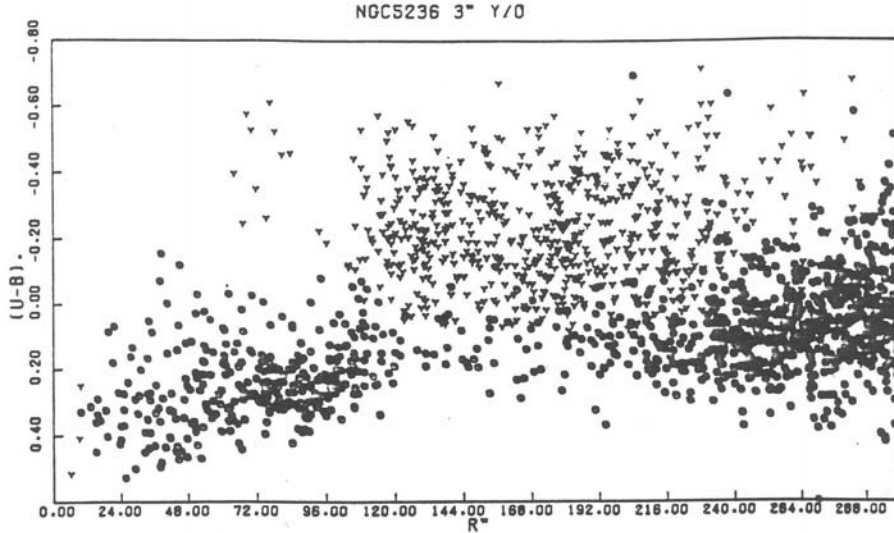


FIG. 7a

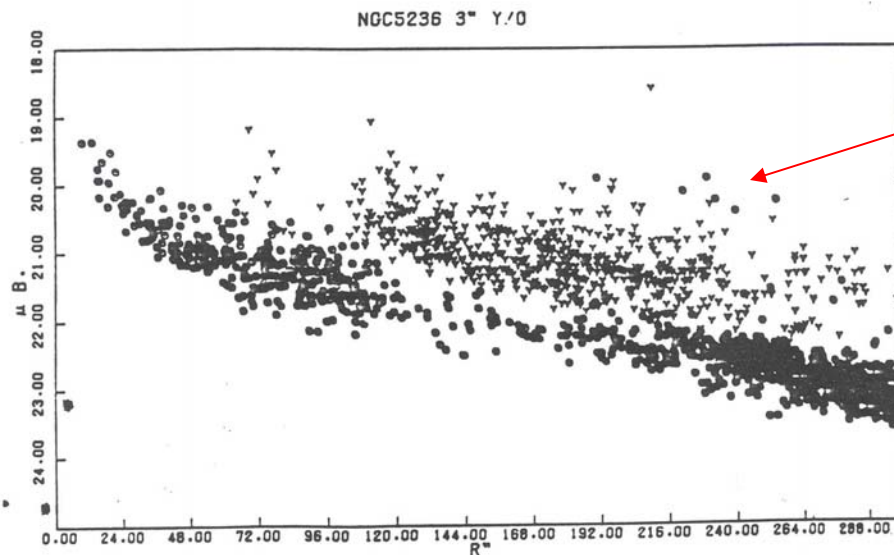


FIG. 7b

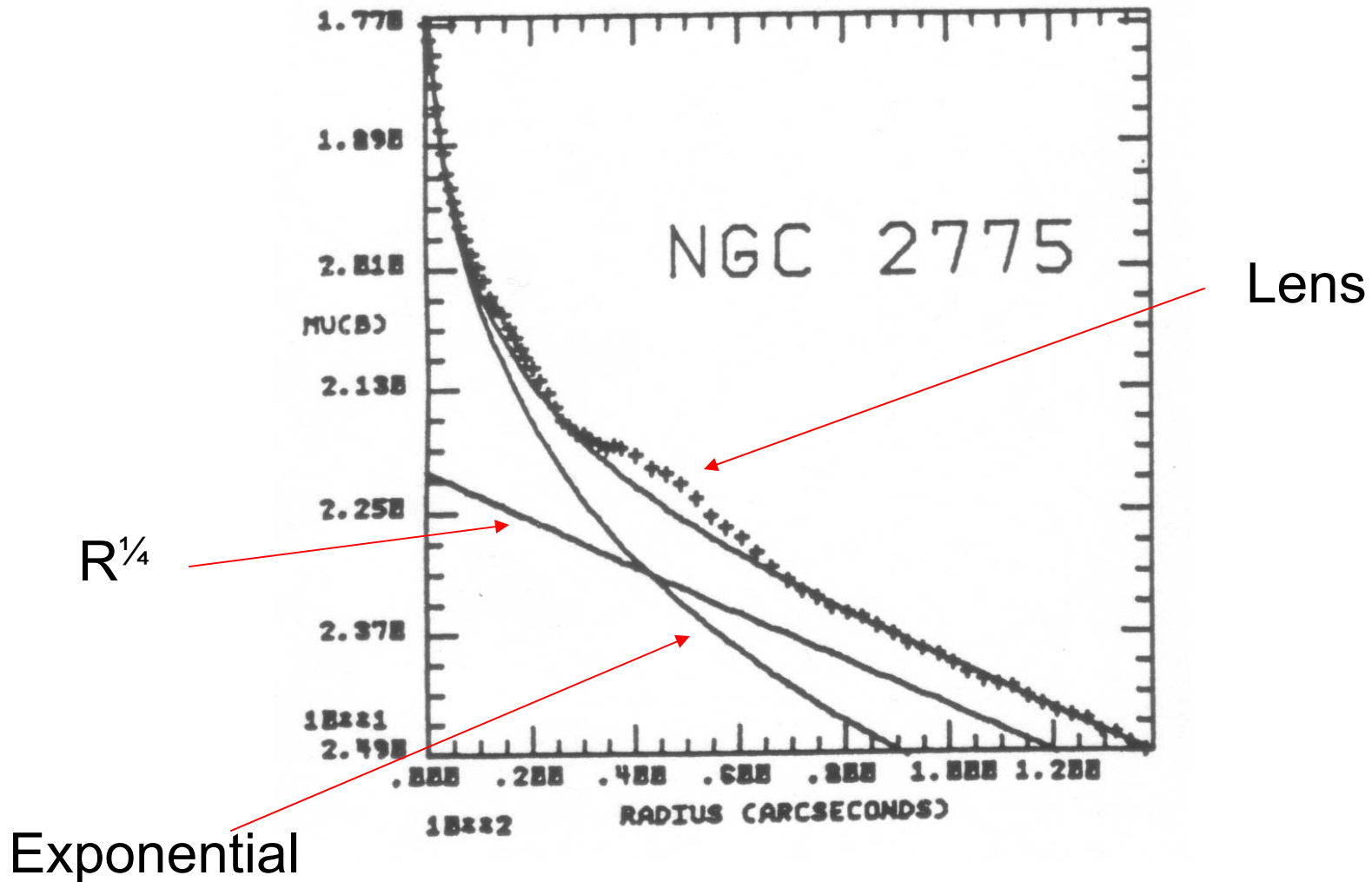
FIG. 7.—(a) $(U - B)_0$; (b) μ_{80} , for pixels selected on the basis of their color. “Old light” pixels [$(B - V)_0 > 0.65$] are shown as O's, and “young light” pixels [$(B - V)_0 < 0.40$] are shown as Y's.

1) might be due to regions of recent Star Formation

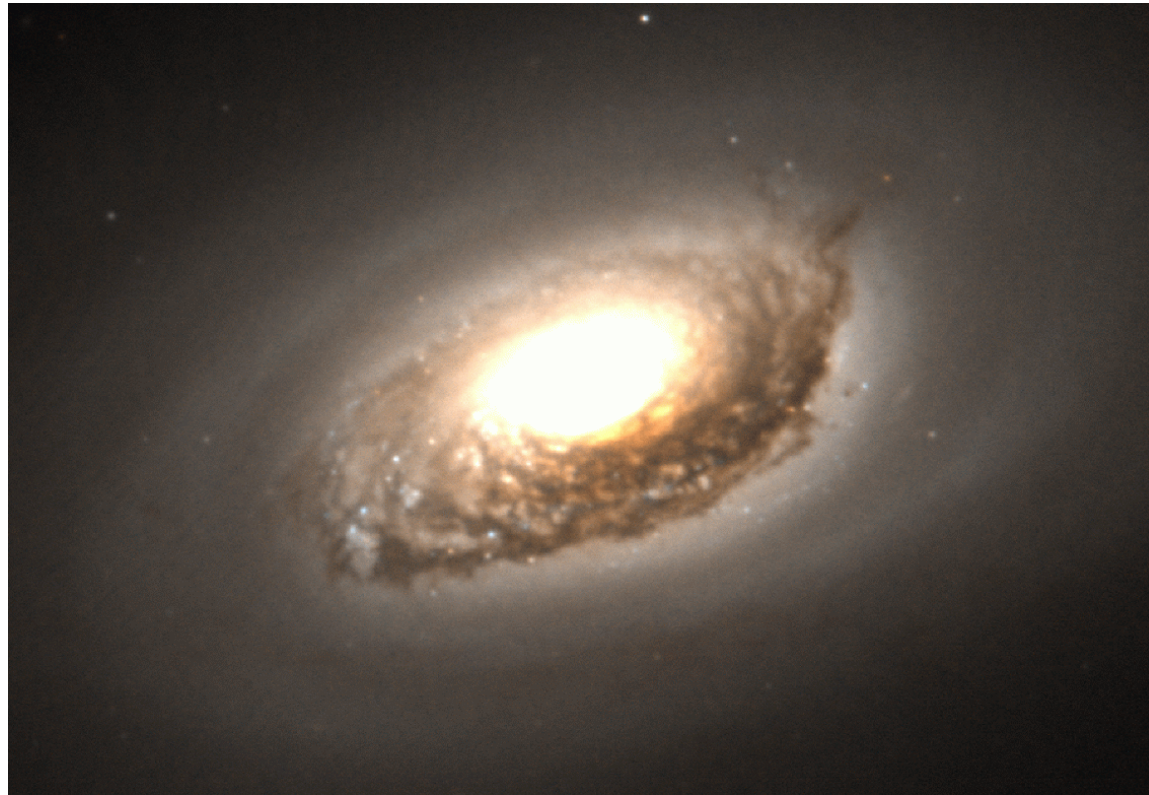
Blue Pixels are contributing to non-exponential Disk

(Talbot, Jensen & Dufour 1979)

Departures: 2) Presence of Lens recent made by resonance (bar) destruction

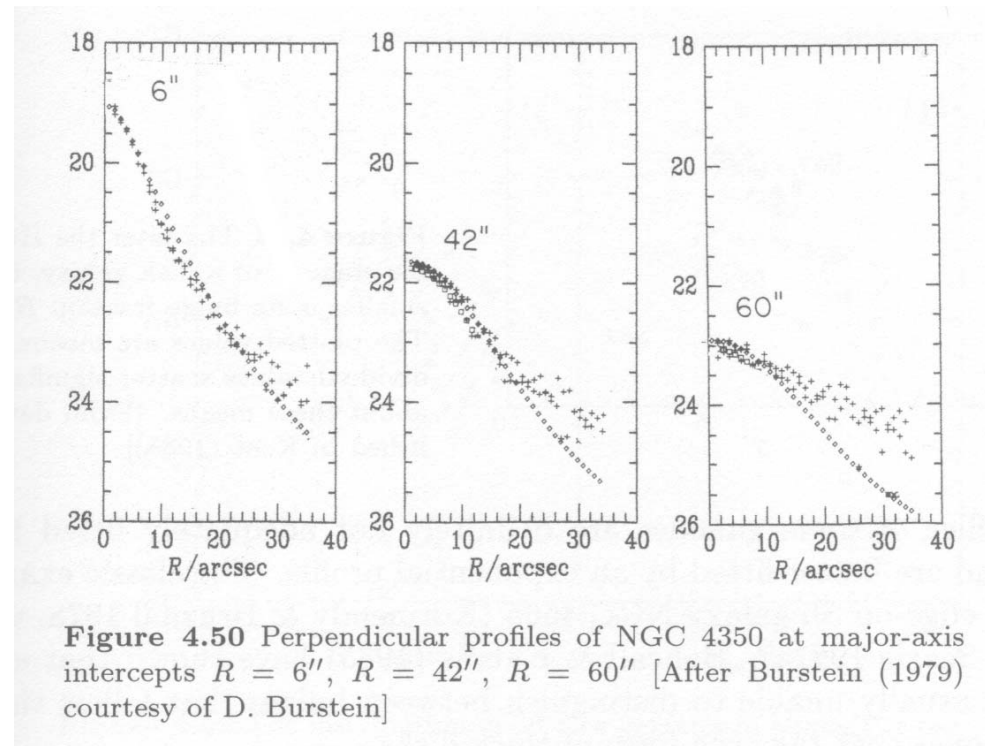


Departures: 3) Bulges that are really disks



- They can be fitted by an $r^{1/4}$ profile, but have spiral structure & $(v / \sigma)^*$ consistent with rotation
- You can make a bulge by transporting gas inward & igniting a nuclear starburst.

Departures: 4) Thick Disk



- Have intermediate flattening between that of a thin disk and a bulge
- Are more diffuse than thin disk
- Have a shallow luminosity gradient parallel to the major axis
- Have a rectangular box shape in thick disk galaxies seen edge-on

Thick Disk Formation

- Intermediate Dissipation
- Dynamical Heating
- A merger which partially destroyed the thin disk through heating

Mass & Luminosity

The central mass surface density can be written as,

$$\Sigma_0 = \frac{M}{L} I_0,$$

where I_0 is the central surface brightness. Because M/L is constant with radius, the surface brightness profile,

$$I(R) = I_0 e^{-r/r_0},$$

can be written be written in terms of the mass surface density as,

$$\Sigma(R) = \Sigma_0 e^{-r/r_0}.$$

For a sheet model of a disk, we can write,

$$\frac{dM(r)}{dr} = 2\pi r \Sigma.$$

Mass & Luminosity, cont'

Integrating $M(r)$ from 0 to r ,

$$M(r) = 2\pi \int_0^r r \Sigma_0 e^{-r/r_0} dr = 2\pi \Sigma_0 r_0^2 \left[1 - \left(1 + \frac{r}{r_0} \right) e^{-r/r_0} \right].$$

As $r \rightarrow \infty$,

$$M(\infty) = 2\pi \Sigma_0 r_0^2.$$

Similarly,

$$L(\infty) = 2\pi I_0 r_0^2.$$

We can write,

$$L(\infty) = 2\pi I_0 r_0^2.$$

in terms of M_B ,

$$2.5 \log I = 2.5 \log(2\pi I_0) + 2.5 \log r_0^2;$$

$$-M_B = \text{constant} + 5 \log r_0.$$

Once again, the important thing is that $I_0 = \text{constant}$ with Hubble Type.

M_B vs. α^{-1}

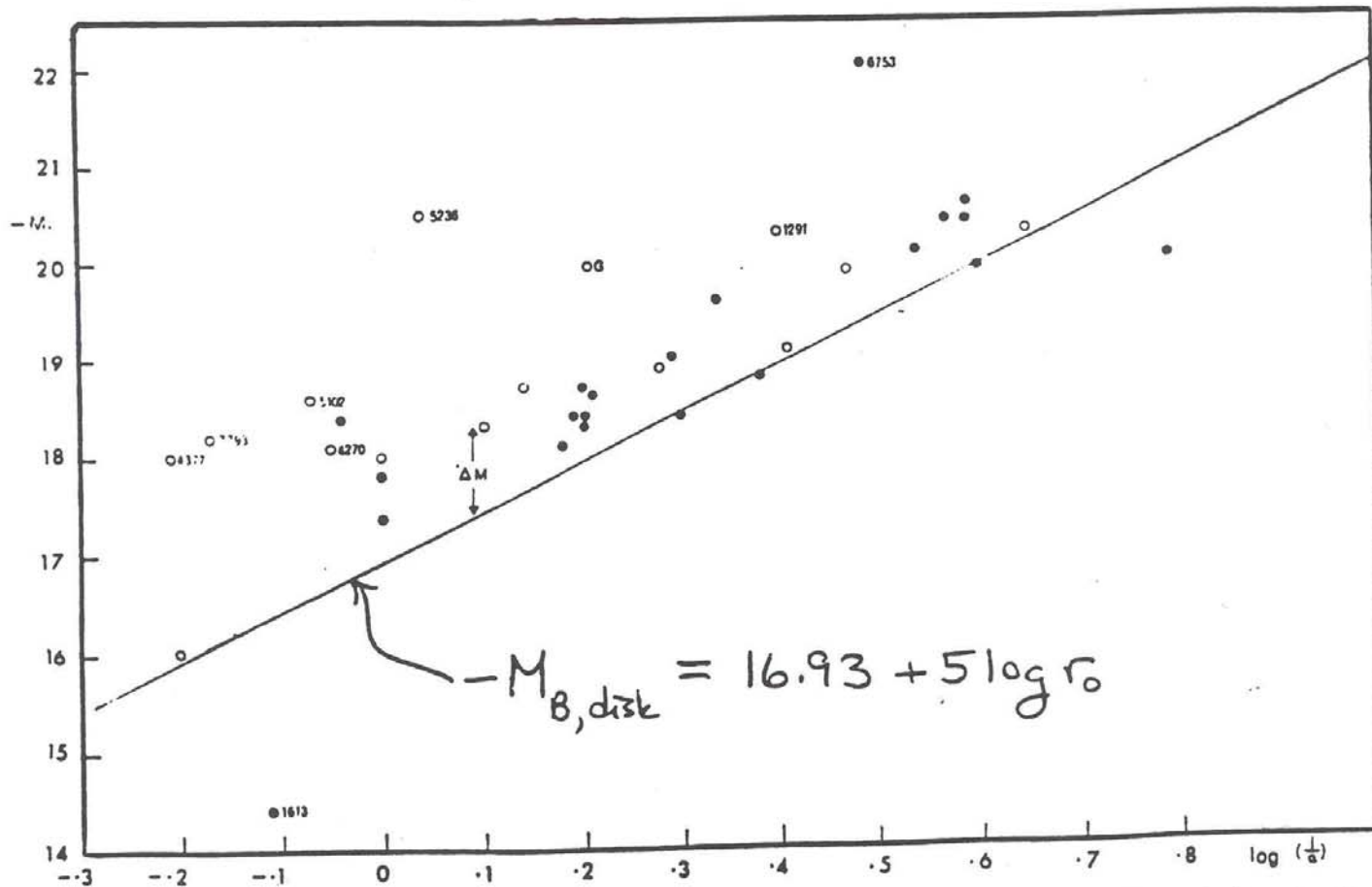


FIG. 7.—Absolute magnitude M_B against the logarithm of the length scale α^{-1} (kpc). Straight line represents $[M_B, \log(\alpha^{-1})]$ -relation for exponential disks with $B(0)_c = 21.65$ mag per square second of arc; see eq. (22). Coding is same as for Fig. 6.

$\alpha^{-1} \downarrow$ as M_B

(Freeman 1970)

Total Angular Momentum

The total angular momentum of a disk can be approximated by first considering stars in circular orbits at the scale length radius r_0 ,

$$\frac{v^2}{r_0} \approx \frac{GM}{r_0^2},$$

which can be rewritten as,

$$v \approx \left(\frac{GM}{r_0} \right)^{1/2}.$$

It turns out that the total angular momentum is approximately equal to,

$$H \approx Mvr_0 = M \left(\frac{GM}{r_0} \right)^{1/2} r_0 \approx (GM^3r_0)^{1/2}.$$

The actual equation derived by Freeman (1970) for a rotating exponential disk is,

$$H = 1.109 \left(GM^3r_0 \right)^{1/2}.$$

Faber-Jackson Relation for Elliptical Galaxies

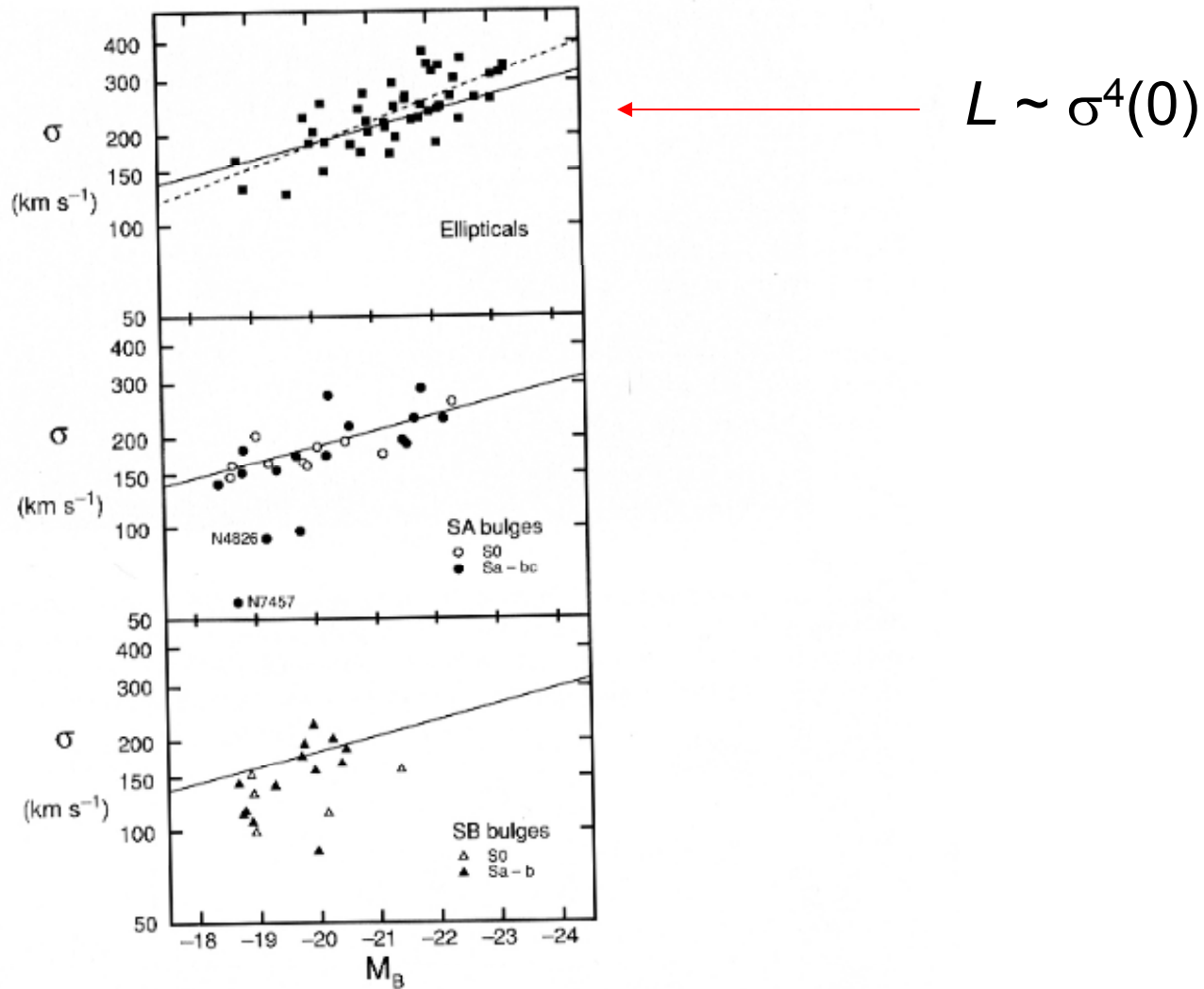


Fig. 6. Correlation between central velocity dispersion σ and absolute magnitude M_B for elliptical galaxies and for bulges of unbarred (SA) and barred (SB) disk galaxies. The solid line is a fit to the galaxies in the middle panel; the dashed line is a fit to the ellipticals. Except for the NGC 4826 point, this figure is from Kormendy and Illingworth (1983).

Tully-Fisher Relation

I.e., the Faber-Jackson Relation for spiral galaxies. It makes use of HI rotation curves in order to trace the kinematics of spiral galaxies.

Assume stars in circular orbits,

$$v^2 \sim \frac{GM}{r_0};$$

And express the luminosity, L , as,

$$L \sim I_0 r_0^2.$$

Squaring the velocity equation, then making the appropriate substitutions,

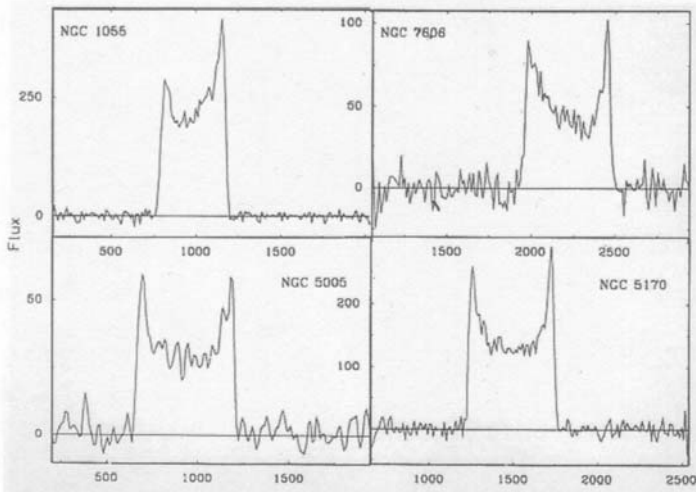
$$v^4 \sim \frac{G^2 M^2}{r_0^2} \sim \frac{G^2 M^2 I_0}{L}.$$

Solving for L yields,

$$L \propto \frac{v^4}{I_0 (M/L)^2} \propto v^4.$$

Determining Parameters for Tully Fisher Relation

- Determine distances to a sample of spiral galaxies using other methods
- Observe the sample of spirals in HI. From the velocity curve, determine the full width of the HI at 20% the maximum flux density
- Take out inclination & random disk motion effects in order to get $\Delta v = W_R$,



$$W_R = \frac{(W_{FW20M} - W_{\text{random}})}{\sin i}.$$

Tully-Fisher Relation

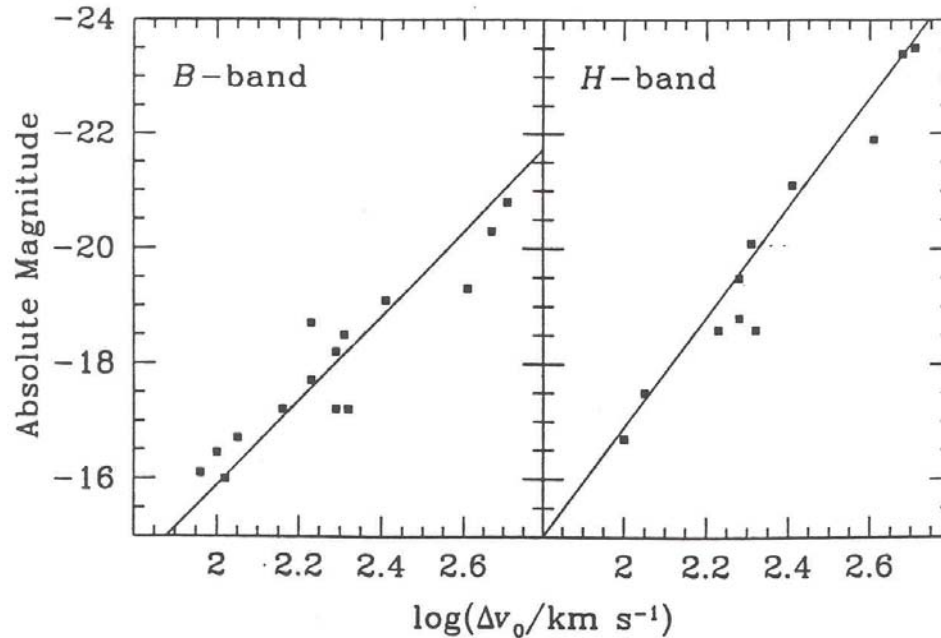


Figure 7.6 Plot of absolute magnitude in *B*- and *H*- bands as a function of velocity width for galaxies with independently determined distances. [From the data published in Pierce & Tully (1992)]

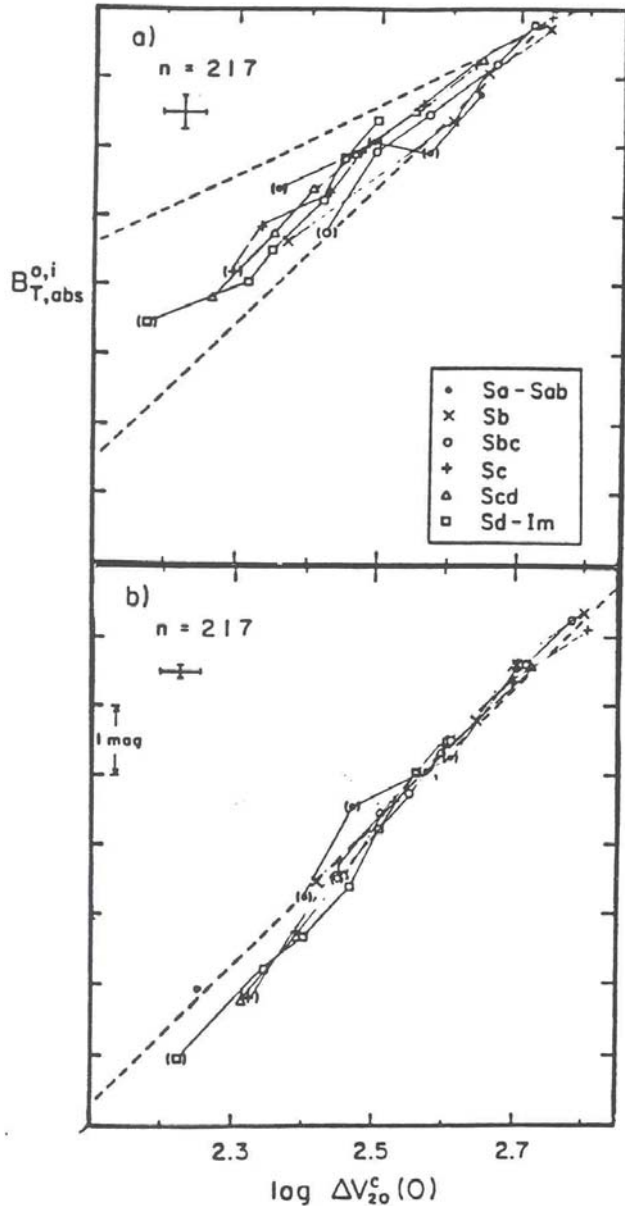
$$M_B^i = -7.48(\log W_R^i - 2.50) - 19.55 + \Delta_B \pm 0.14,$$

$$M_R^i = -8.23(\log W_R^i - 2.50) - 20.46 + \Delta_R \pm 0.10,$$

$$M_I^i = -8.72(\log W_R^i - 2.50) - 20.94 \pm 0.10,$$

$$M_H^i = -9.50(\log W_R^i - 2.50) - 21.67 \pm 0.08.$$

Tully-Fisher: $L \rightarrow \Delta v^4$ at Longer λ s



I.e, because $M / L_{\lambda > 0.8 \mu m}$ is

- 1) sensitive to light from older stars
- 2) less sensitive to dust

FIGURE 12.7

The Tully-Fisher relation in the optical (B , top) and the near IR (H , bottom). The sample of 217 galaxies has been binned using regressions of the two variables, and morphological types are distinguished by different symbols. The lines have slopes corresponding to $\alpha = 2$ and 4 in Eq. (12.29), but at H only the latter is shown. The absolute-magnitude scales are arbitrary (that is, independent of the actual Hubble constant), and distances have been calculated using a Virgocentric inflow model. (From Aaronson and Mould 1983.)

Dynamics of the Self-Gravitating Isothermal Sheet

Poisson's Equation in cylindrical polar coordinates is,

$$\frac{1}{R} \frac{\partial}{\partial R} \left(R \frac{\partial \Phi}{\partial R} \right) + \frac{1}{R^2} \frac{\partial^2 \Phi}{\partial \theta^2} + \frac{\partial^2 \Phi}{\partial z^2} = 4\pi G \rho(R, z).$$

If axial symmetry is assumed, and the rotation curve is flat, then,

$$\frac{1}{R} \frac{\partial}{\partial R} \left(R \frac{\partial \Phi}{\partial R} \right) + \frac{\partial^2 \Phi}{\partial z^2} = \frac{1}{R} \frac{\partial}{\partial R} (R F_R) + \frac{\partial^2 \Phi}{\partial z^2};$$

$$\frac{1}{R} \frac{\partial}{\partial R} (v_c^2) + \frac{\partial^2 \Phi}{\partial z^2} = \frac{\partial^2 \Phi}{\partial z^2} = 4\pi G \rho(R, z),$$

where,

$$-\frac{\partial \Phi}{\partial R} = F_R = \frac{v_c^2}{R}.$$

Assuming that the isothermal sheet has an isothermal distribution function,

$$f = f(E_z) = \frac{\rho_0}{(2\pi\sigma_z^2)^{1/2}} e^{-E_z/\sigma_z^2},$$

where,

$$E_z = \Phi(z) + 1/2v_z^2$$

(note that the disk height \ll disk scale length), the density is thus,

$$\rho = \int_{-\infty}^{\infty} \frac{\rho_0}{(2\pi\sigma_z^2)^{1/2}} e^{-(\Phi+1/2v_z^2)/\sigma_z^2} dv_z = \rho_0 e^{-\Phi/\sigma_z^2}.$$

Poisson's Equation is thus,

$$\frac{\partial^2 \Phi}{\partial z^2} = 4\pi G \rho_0 e^{-\Phi/\sigma_z^2}.$$

We can express the above equation in a non-dimensional form by making the following substitutions,

$$\phi = \Phi/\sigma_z^2 \quad \text{and} \quad \xi = z/z_0,$$

where,

$$z_0 = \left(\frac{\sigma_z^2}{8\pi G\rho_0} \right)^{1/2}.$$

Differentiating the substituted terms,

$$\sigma_z^2 d\phi = d\Phi \quad \text{and} \quad z_0 d\xi = dz.$$

Thus,

$$2\sigma_z^2 \frac{d^2\phi}{dz^2} = 8\pi G\rho_0 e^{-\phi};$$

$$2 \frac{d^2\phi}{d\left(\frac{z}{(\sigma_z^2/8\pi G\rho_0)^{1/2}}\right)^2} = e^{-\phi};$$

$$2 \frac{d^2\phi}{d\xi^2} = e^{-\phi}.$$

From the density expression derived from the distribution function, ϕ can be substituted into the previous equation such that,

$$\ln \rho = \ln \rho_0 - \phi.$$

Thus,

$$2 \frac{d^2 \phi}{d\xi^2} = \frac{\rho}{\rho_0},$$

which has the solution,

$$\rho = \rho_0 \operatorname{sech}^2 \left(\frac{\xi}{2} \right),$$

or,

$$\rho = \rho_0 \operatorname{sech}^2 \left(\frac{1}{2} \frac{z}{z_0} \right).$$

From,

$$z_0 = \left(\frac{\sigma_z^2}{8\pi G \rho_0} \right)^{1/2},$$

we can solve for σ_z ,

$$\sigma_z^2 = 8\pi z_0^2 G \rho_0.$$

If ρ_0 (i.e., $\rho_{z=0}$) at any radius, r , is an exponential function of r , then,

$$\sigma_z^2 \propto \rho_0 \propto e^{-r/r_0}.$$

Because of this, many have modified the surface brightness Profile equation to take into account the isothermal sheet Model,

$$I(r, z) = I_0 e^{-r/r_0} \text{sech}^2(z/z_0).$$