

Class 12 : Supernova cosmology and the acceleration of the Universe

- This class
 - Redshift-distance relation as a probe of the cosmological model
 - Type-1A supernovae
 - Supernovae and cosmology
 - Discovery of acceleration
 - It all fits together... concordance cosmology

0 : Recap of last two classes

- Used FRW metric to examine propagation of photons. Radially propagating photons described by

$$\int_{t_e}^{t_r} \frac{c dt}{a} = \int_0^{r_0} \frac{dr}{\sqrt{1 - kr^2}}$$

- Derived redshift/scale-factor relation

$$1 + z = \frac{a(t_r)}{a(t_e)}$$

- Found that, for at least some cosmological models (e.g. matter or radiation dominated flat models), photons only travel finite proper distance since big-bang. Introduces idea of particle horizon. Example; for matter-dominated flat Universe we have

$$d_H = a_0 r_H = 3ct_0$$

- Found that, practically, there are different definitions of distances...

- Luminosity distance (i.e. that which appears in the inverse square law connecting luminosity and flux)...

$$d_L = a_0 r \times (1 + z)$$

- Angular size distance (i.e. that which appears in the expressions for the angular size of an object)

$$d_A = \frac{a_0 r}{(1 + z)}$$

I : Diagnostic power of redshift-distance relation

- Important point...
 - When viewing a galaxy, function $r(z)$ depends upon cosmological model.

- Example: matter-dominated flat Universe

- Coordinate distance is

$$a_0 r(z) = 3ct_0 \left[1 - \frac{1}{\sqrt{1+z}} \right]$$

- Luminosity distance is

$$d_L = 3ct_0 \left[1 + z - \sqrt{1+z} \right]$$

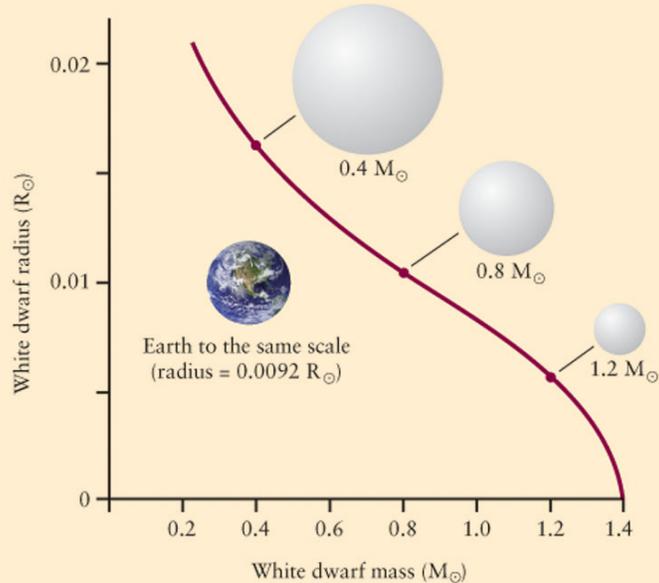
- For small redshifts, we have

$$d_L \approx \frac{3ct_0}{2} \left[z - \frac{1}{4}z^2 \right] = \frac{cz}{H_0} \left[1 - \frac{1}{4}z \right]$$

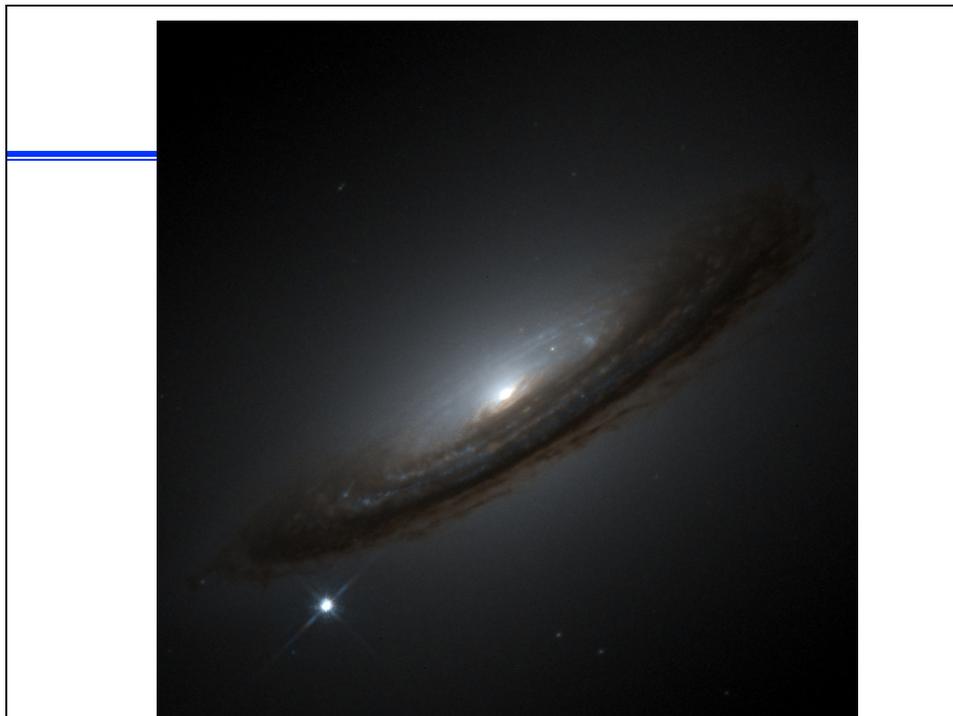
- What have we just recovered?

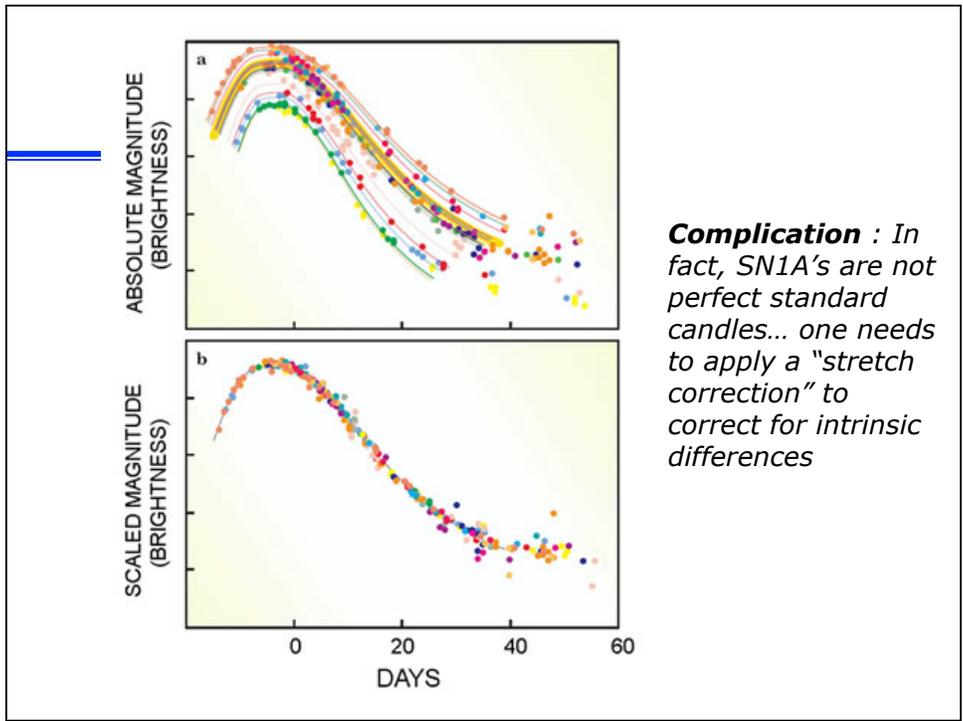
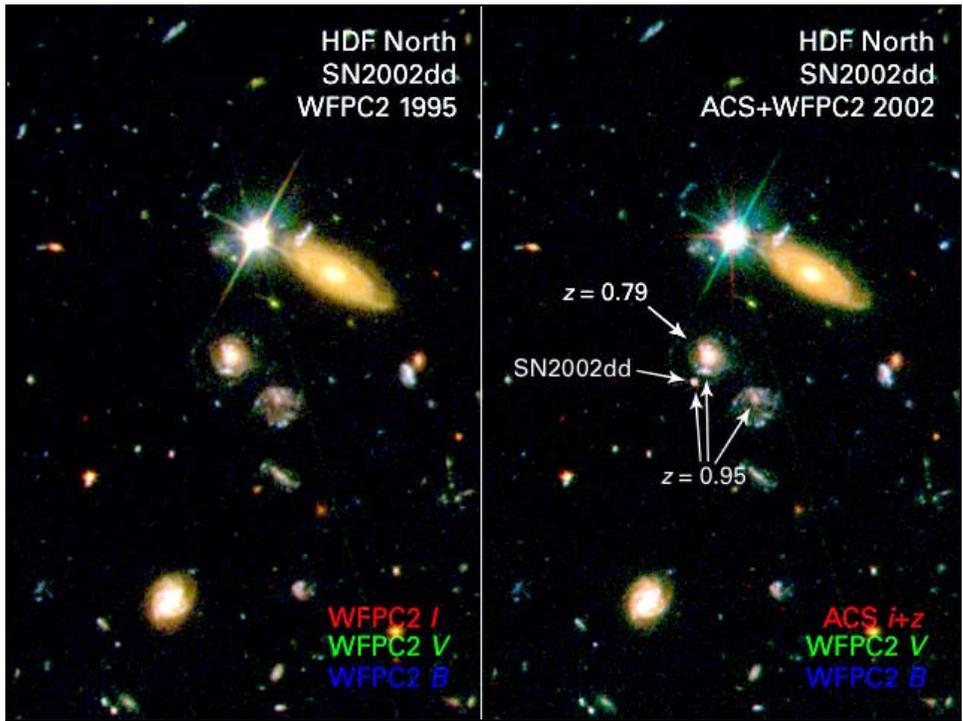
II : Type-1A Supernovae

- Basic goal : to determine luminosity distance as a function of redshift out to high redshift; then compare with predictions from cosmological models
- We need to objects that are good standard candles:
 - Need to have a known luminosity
 - Need to be very luminous (so we can see them at cosmological distances)
 - Need to be easily recognized (so we don't confuse them with other things)
- Type-1A supernovae fit the bill!



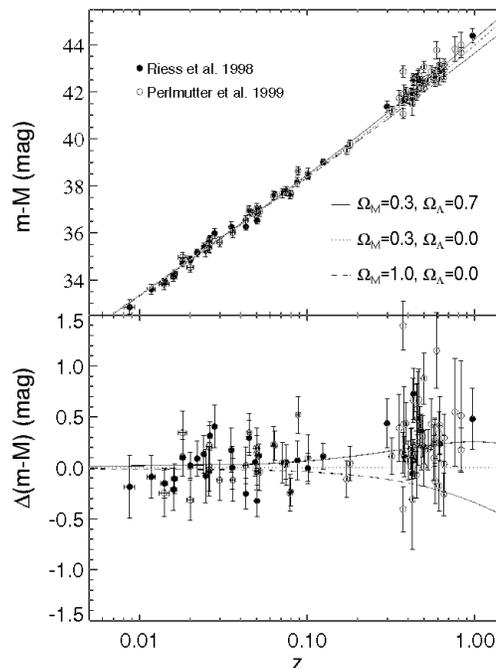
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- What is a Type-1A supernova?
 - SN1A's are white dwarfs that have been pushed over the Chandrasekar limit ($1.4M_{\text{sun}}$) by the accretion of material from a companion...
 - WD starts to collapse
 - Collapse induces thermonuclear incineration
 - In more detail, here's a possible scenario...
 - Start off with a binary star system
 - One star comes to end of its life – forms a "white dwarf" (made of helium, or carbon/oxygen)
 - If close enough, tidal forces of the white dwarf pull matter off the other star... adds to mass of white dwarf (accretion)
 - If accretion pushes white dwarf over the **Chandrasekhar Mass Limit**, it starts to collapse
 - Rapid compression initiates **thermonuclear runaway**... burn whole mass of white dwarf to iron/nickel in few seconds
 - Liberated energy blows the star apart... **no remnant**.





III : Supernova cosmology

- The program...
 - Search for SN1a in nearby & distant galaxies
 - When you find one... measure its redshift and track its lightcurve so you can apply the stretch correction and derive its luminosity
 - Compare inferred luminosity with measured flux in order to derive its luminosity distance
 - Compare with expectations from cosmological models...
 - Nearby supernovae give us H_0
 - Distant supernovae tell us about how H changes with time



IV : Acceleration and Dark Energy

- Supernovae imply that the scale factor is accelerating!!
- Let's look at acceleration equation

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3} \left(\rho + \frac{3p}{c^2} \right)$$

- Acceleration means that we must have

$$p < -\frac{1}{3}\rho c^2$$

- Strange stuff! Has negative pressure!
- Indeed, it formally violates the "Strong Energy Principle"

- So we say that, in addition to matter and radiation, there is a new component/fluid, **dark energy**, with an equation of state

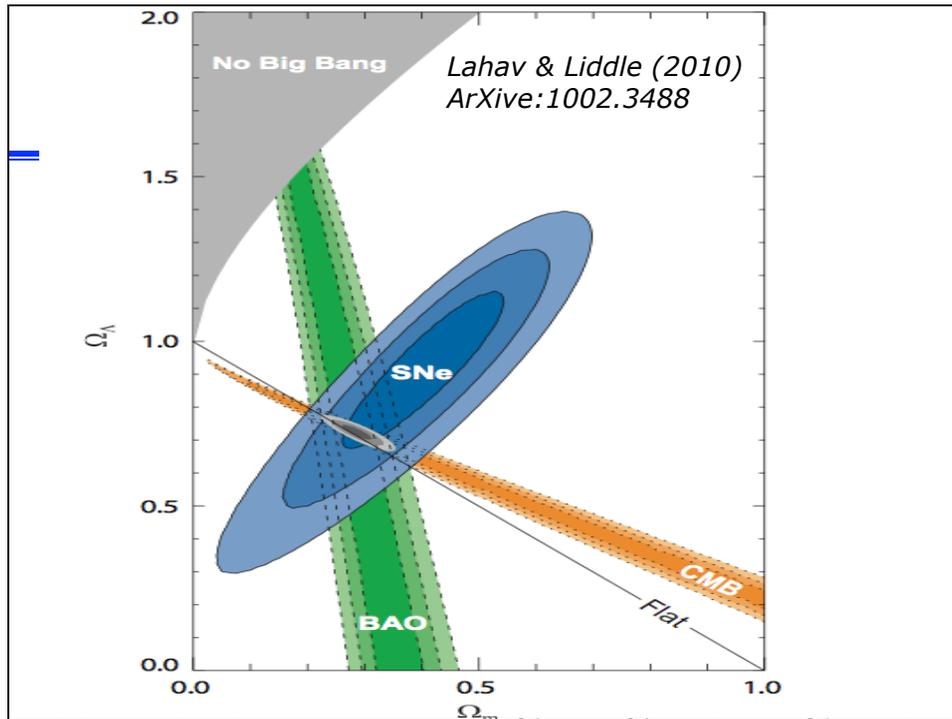
$$p = w\rho c^2 \quad \text{with } w < -\frac{1}{3}$$

- There is a different way of looking at things...
- What if we change the way gravity works?
 - Einstein found that the mathematics permitted the inclusion of an additional term in the GR field equations.
 - Tracking this through gives the "Cosmological Constant" (Λ) terms in the Friedmann and acceleration equation...

$$\left(\frac{\dot{a}}{a} \right)^2 = \frac{8\pi G}{3} \rho - \frac{kc^2}{a^2} + \frac{\Lambda}{3}$$

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3} \left(\rho + \frac{3p}{c^2} \right) + \frac{\Lambda}{3}$$

- Einstein first proposed Λ -term because he thought that the Universe was static (later called this his "greatest mistake")
- Λ -term acts just like dark energy with $p = -\rho c^2$.
- Λ -term also acts like a vacuum energy $\rho = \text{constant}$



Parameter	Symbol	Value
Hubble parameter	h	0.72 ± 0.03
Total matter density	Ω_m	$\Omega_m h^2 = 0.133 \pm 0.006$
Baryon density	Ω_b	$\Omega_b h^2 = 0.0227 \pm 0.0006$
Cosmological constant	Ω_Λ	$\Omega_\Lambda = 0.74 \pm 0.03$
Radiation density	Ω_r	$\Omega_r h^2 = 2.47 \times 10^{-5}$
Neutrino density	Ω_ν	See Sec. 1.1.2
Density perturbation amplitude	$\Delta_{\mathcal{R}}^2(k = 0.002 \text{ Mpc})$	$(2.41 \pm 0.11) \times 10^{-9}$
Density perturbation spectral index	n	$n = 0.963^{+0.014}_{-0.015}$
Tensor to scalar ratio	r	$r < 0.43$ (95% conf.)
Ionization optical depth	τ	$\tau = 0.087 \pm 0.017$
Bias parameter	b	See Sec. 1.3.4

Lahav & Liddle (2010)
ArXiv:1002.3488