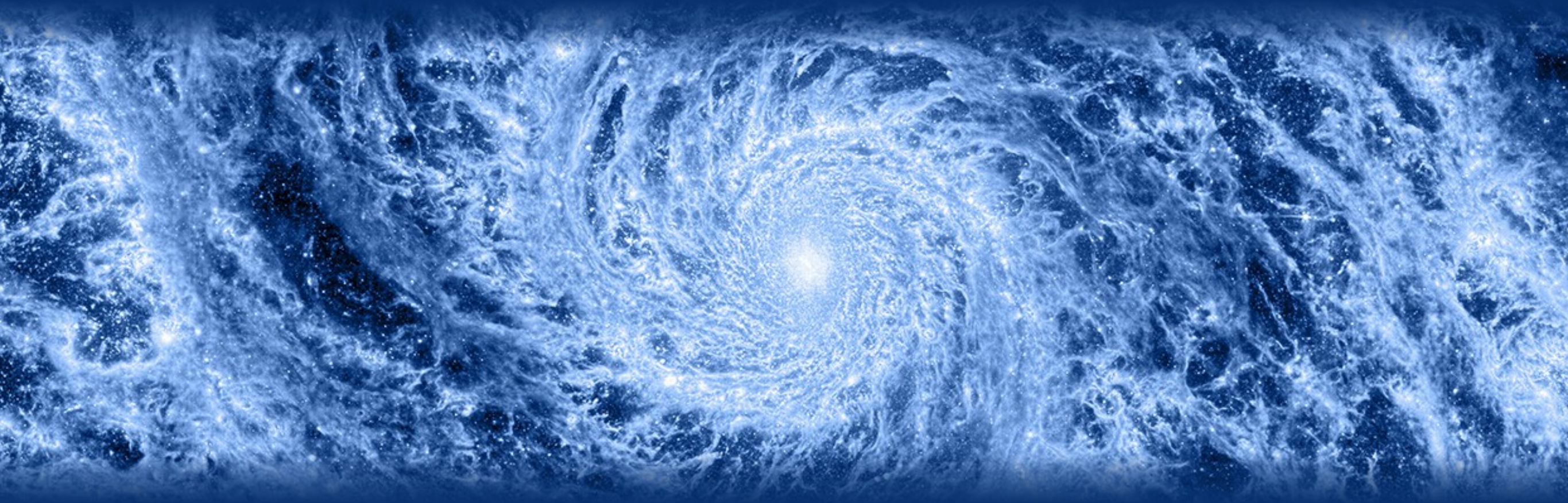


Galaxies

Prof. Benedikt Diemer



Chapter 4 • The formation of dark matter halos

§4.1 • Non-linear growth and halo collapse

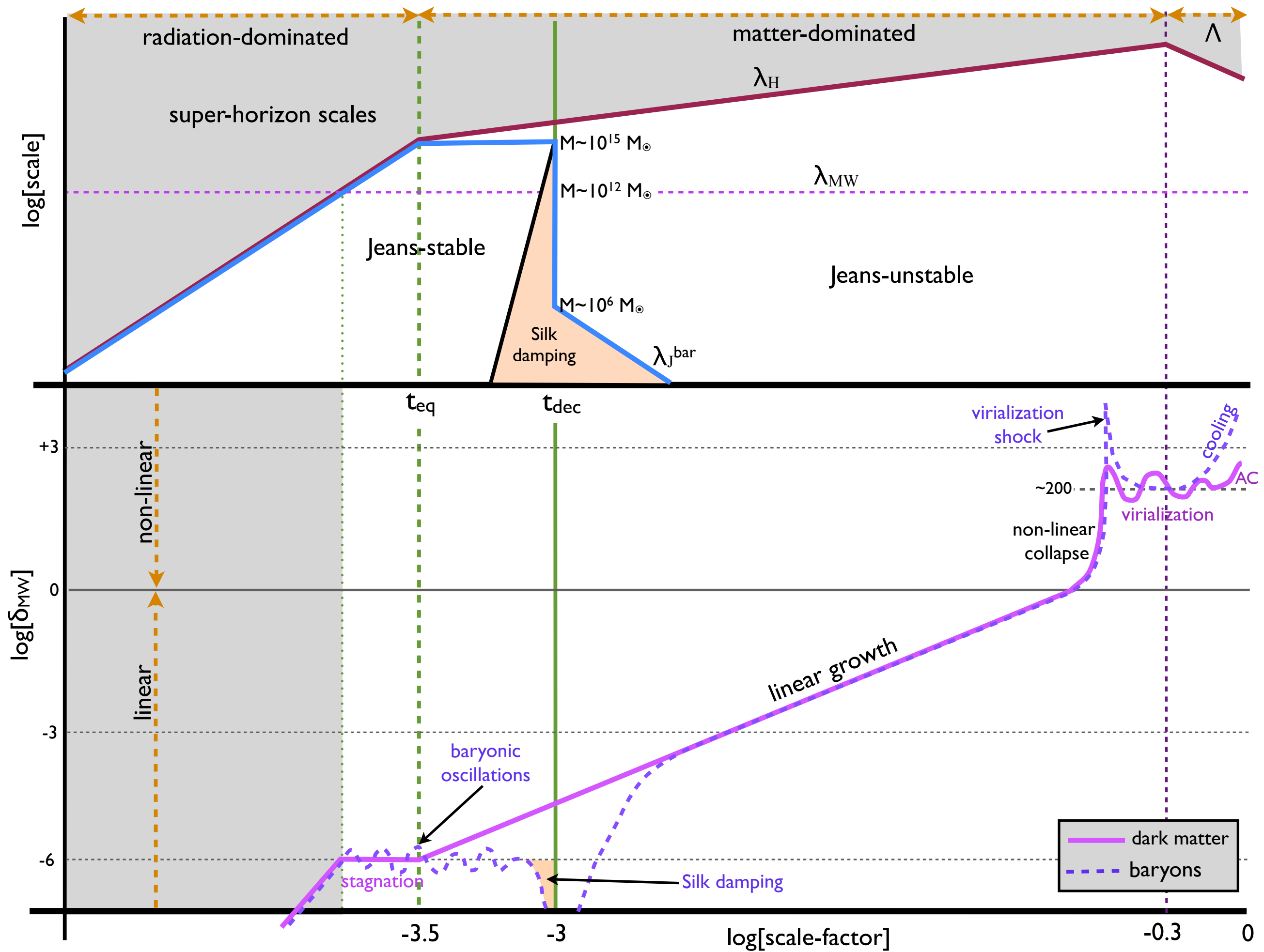


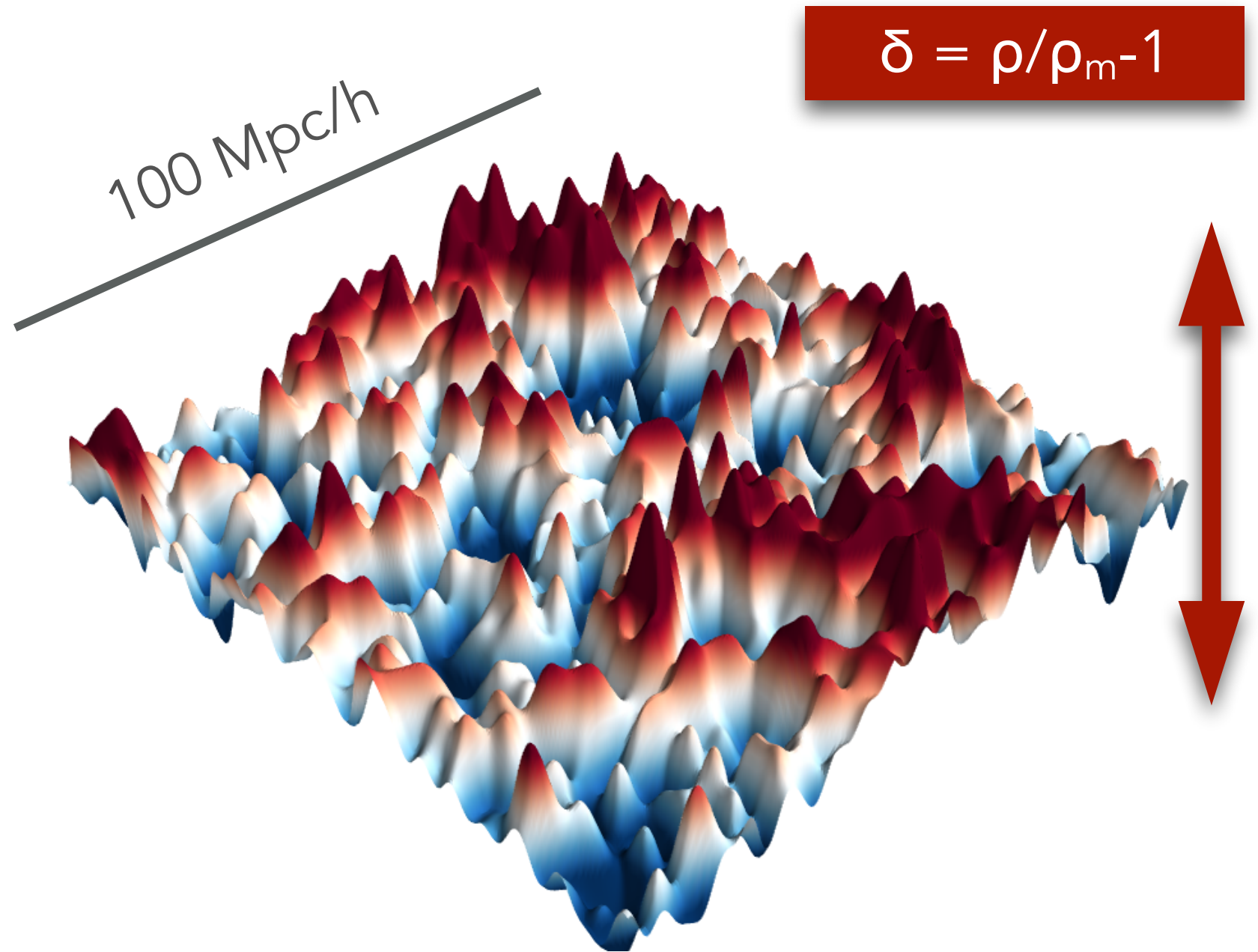
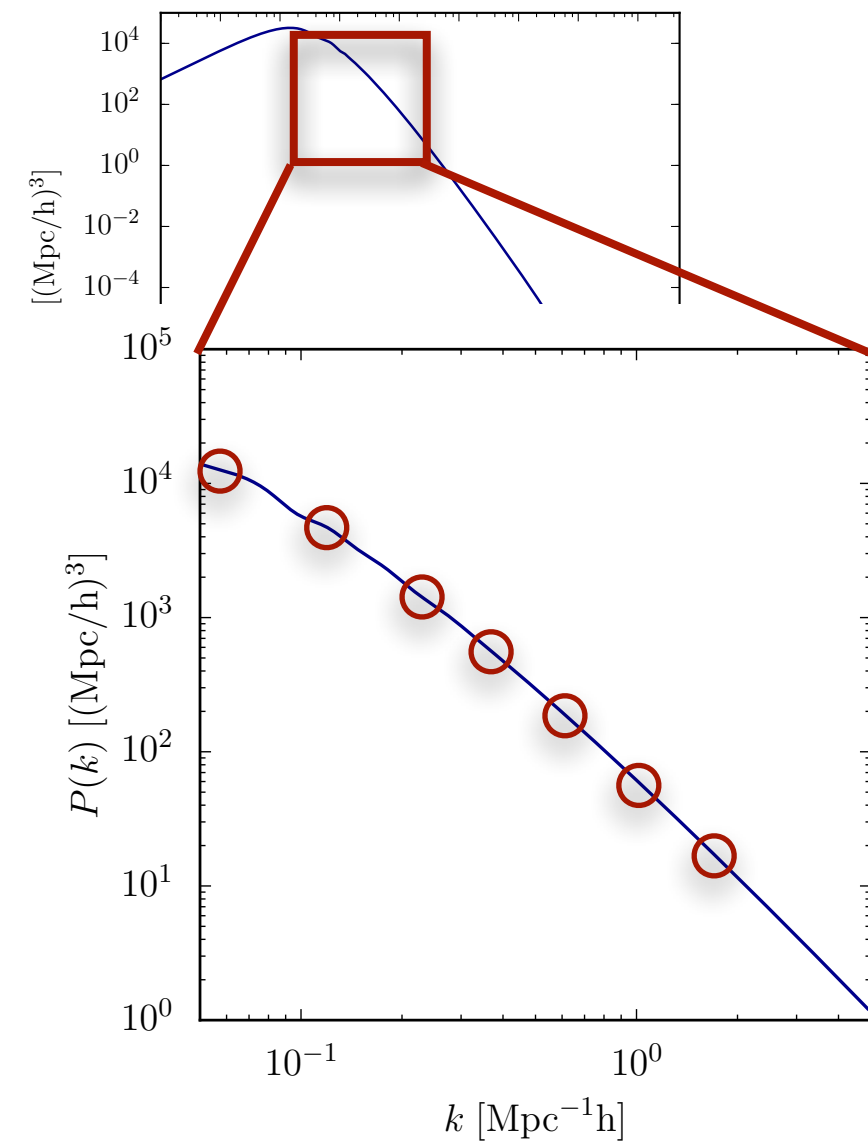
Figure by Frank van den Bosch

Violent relaxation

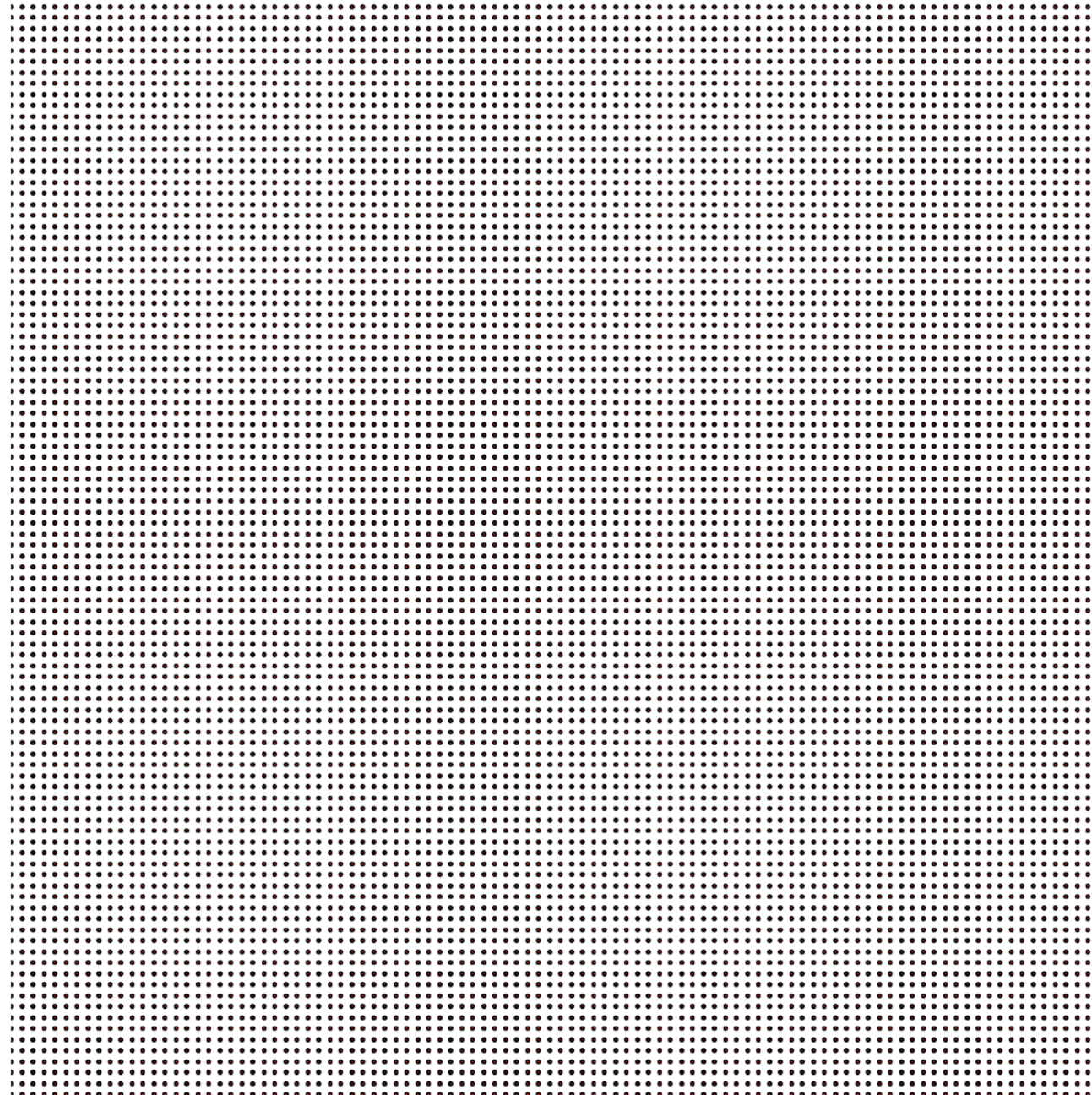


(Source unknown)

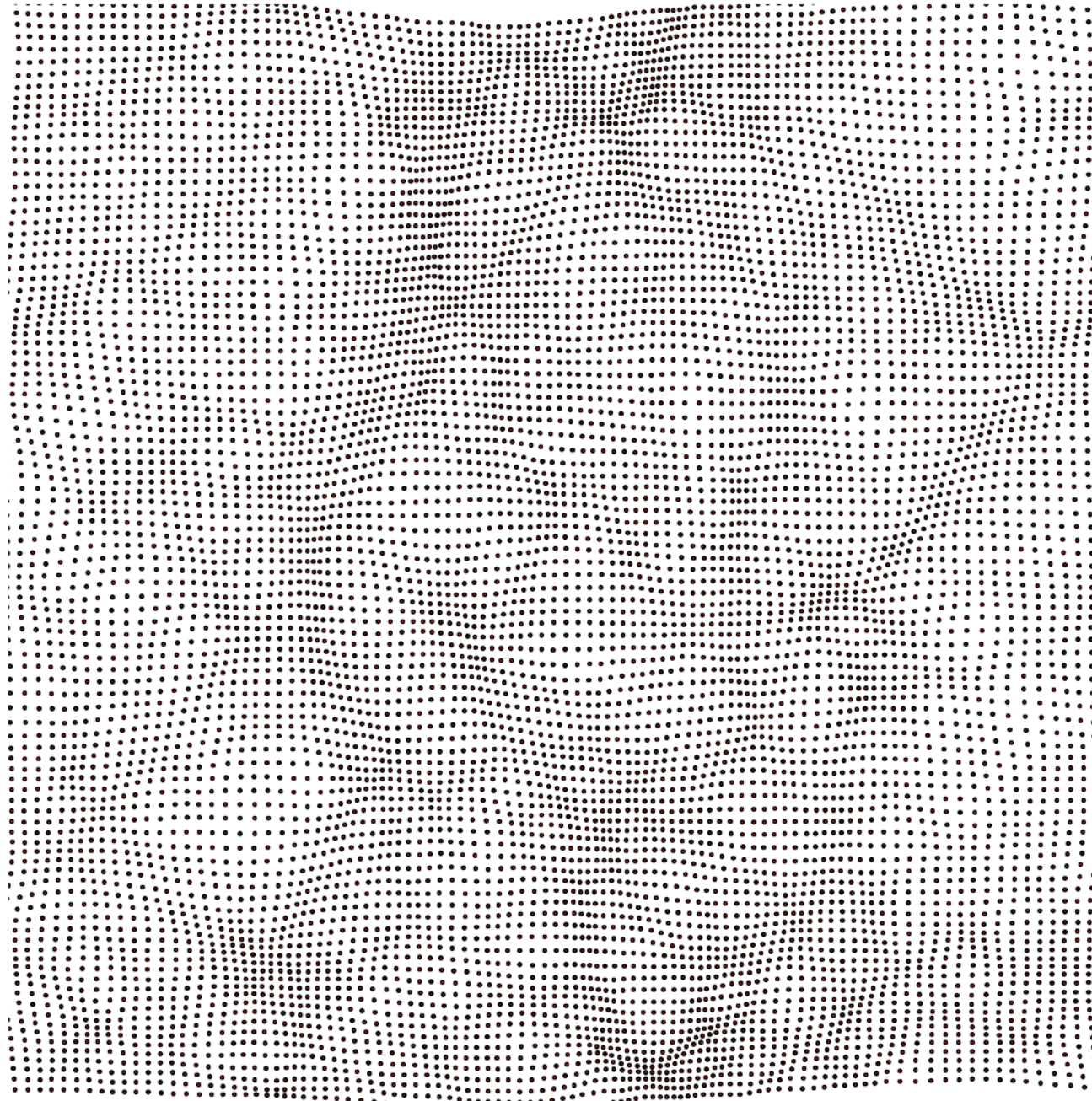
Gaussian random field



N-body simulations

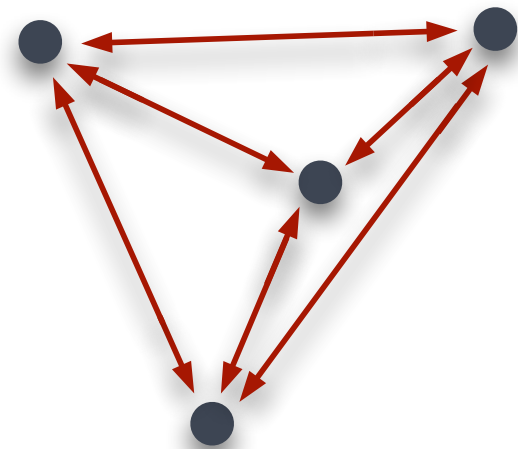


N-body simulations



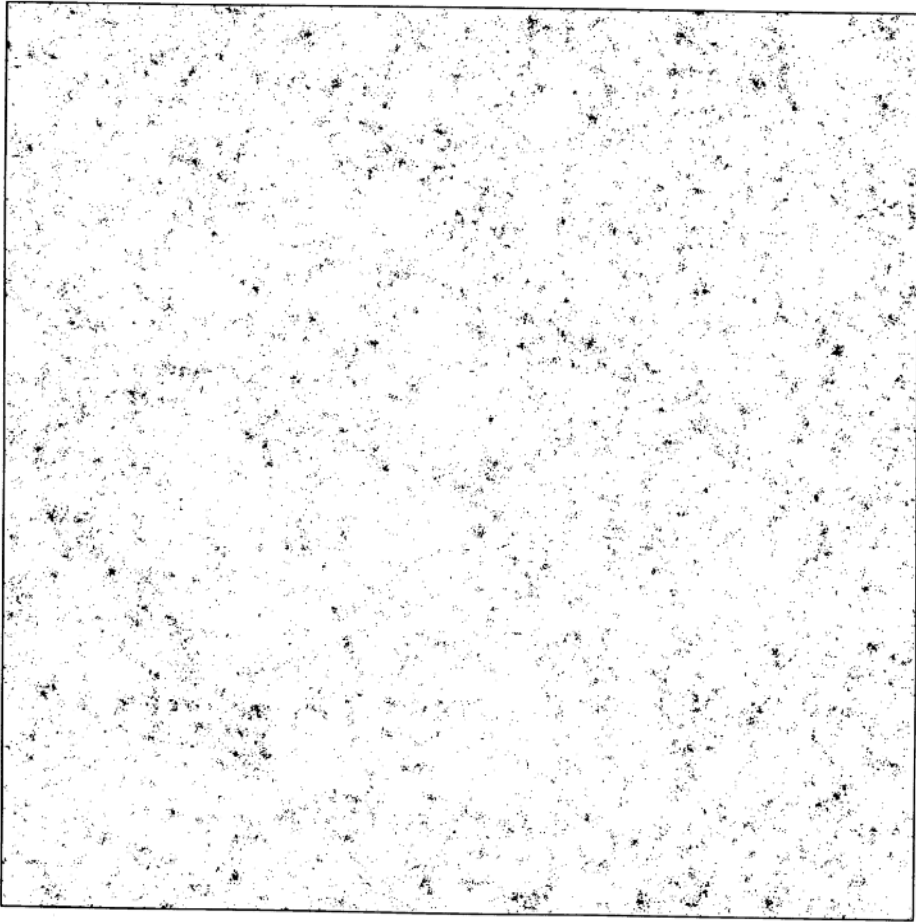
Simulations of dark matter

- Simulate the evolution of dark matter in a large **cube of space**
- Start at a time...
 - A while **after recombination**
 - Early enough that **initial fluctuations are still small**
- Physics in equations includes:
 - **Expansion** of Universe, including dark energy
 - **Gravity** of dark matter
 - **No collisions** between dark matter particles
- Solve Newton's law between N particles (**N-body simulation**)
- Compute gravitational force, move particles a bit, and so on

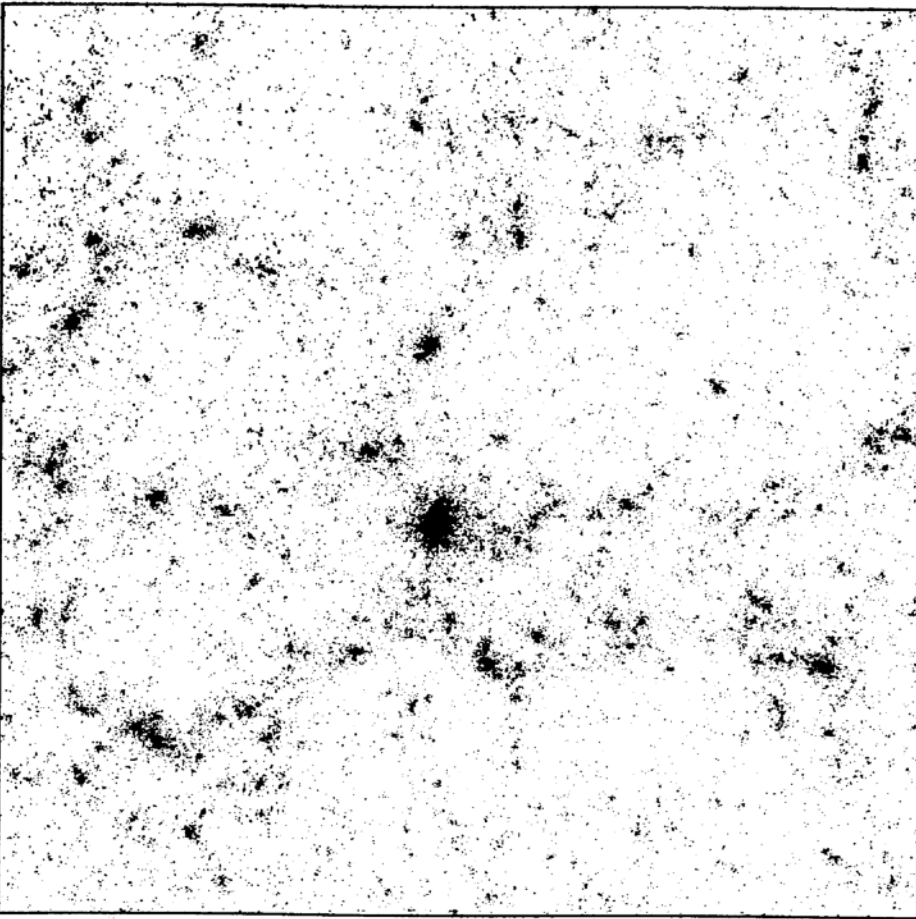


$$F = \frac{Gm_1m_2}{r^2}$$

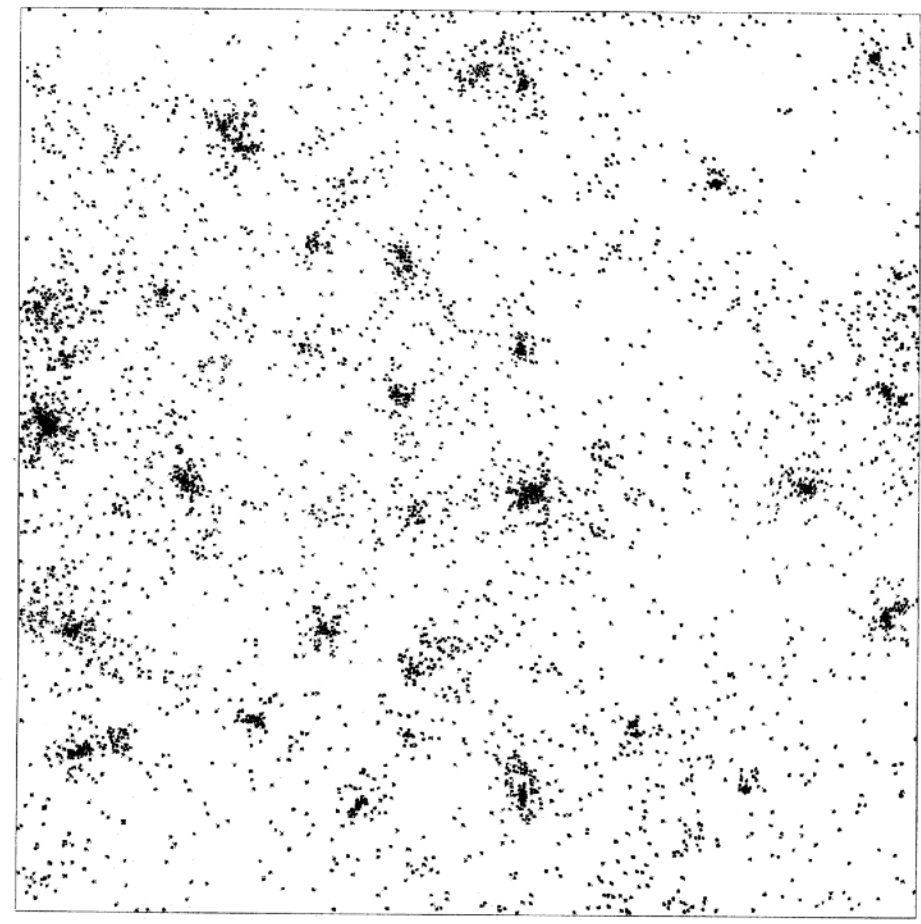
Efstathiou et al. 1981



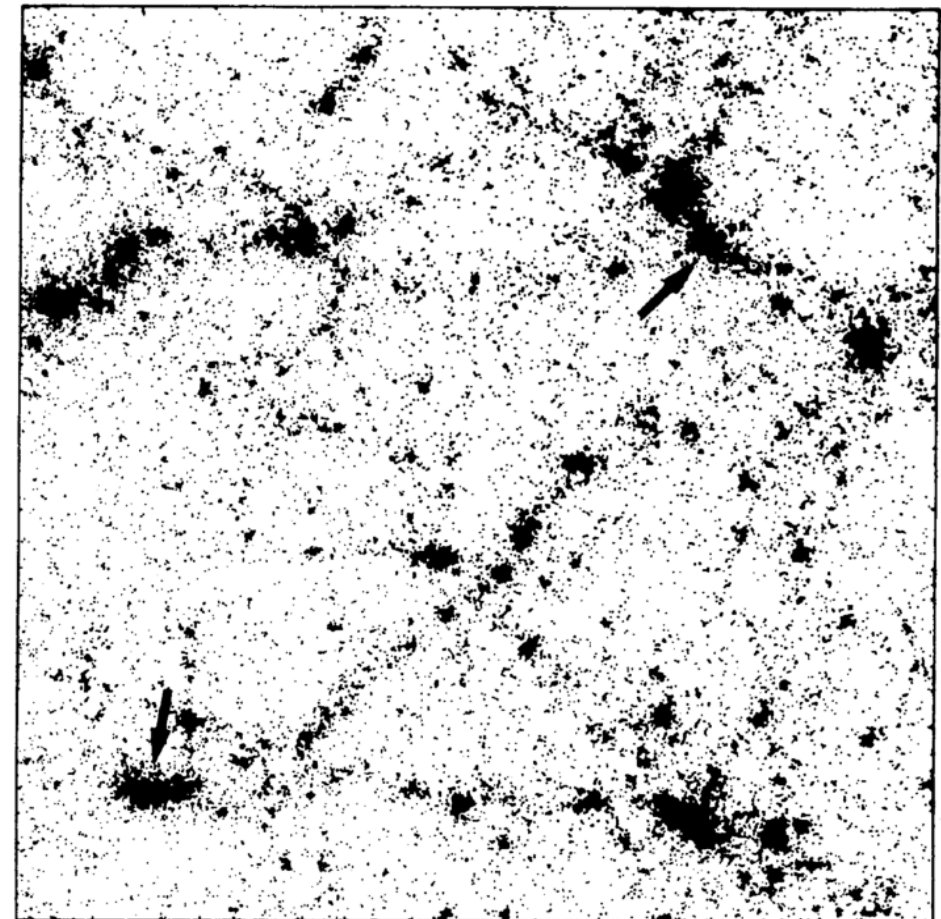
Davis et al. 1985

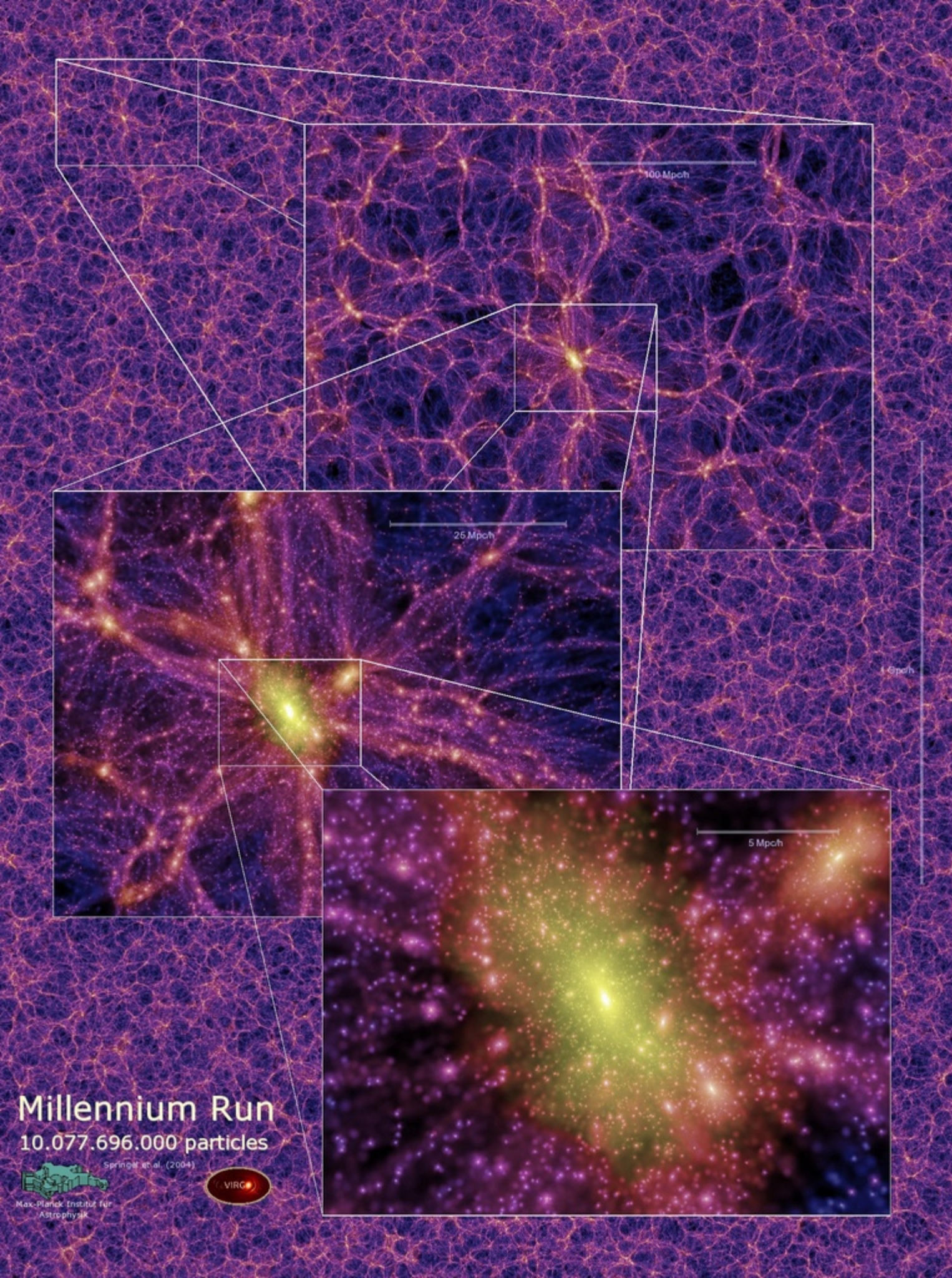


Klypin & Shandarin 1983



Frenk et al. 1988



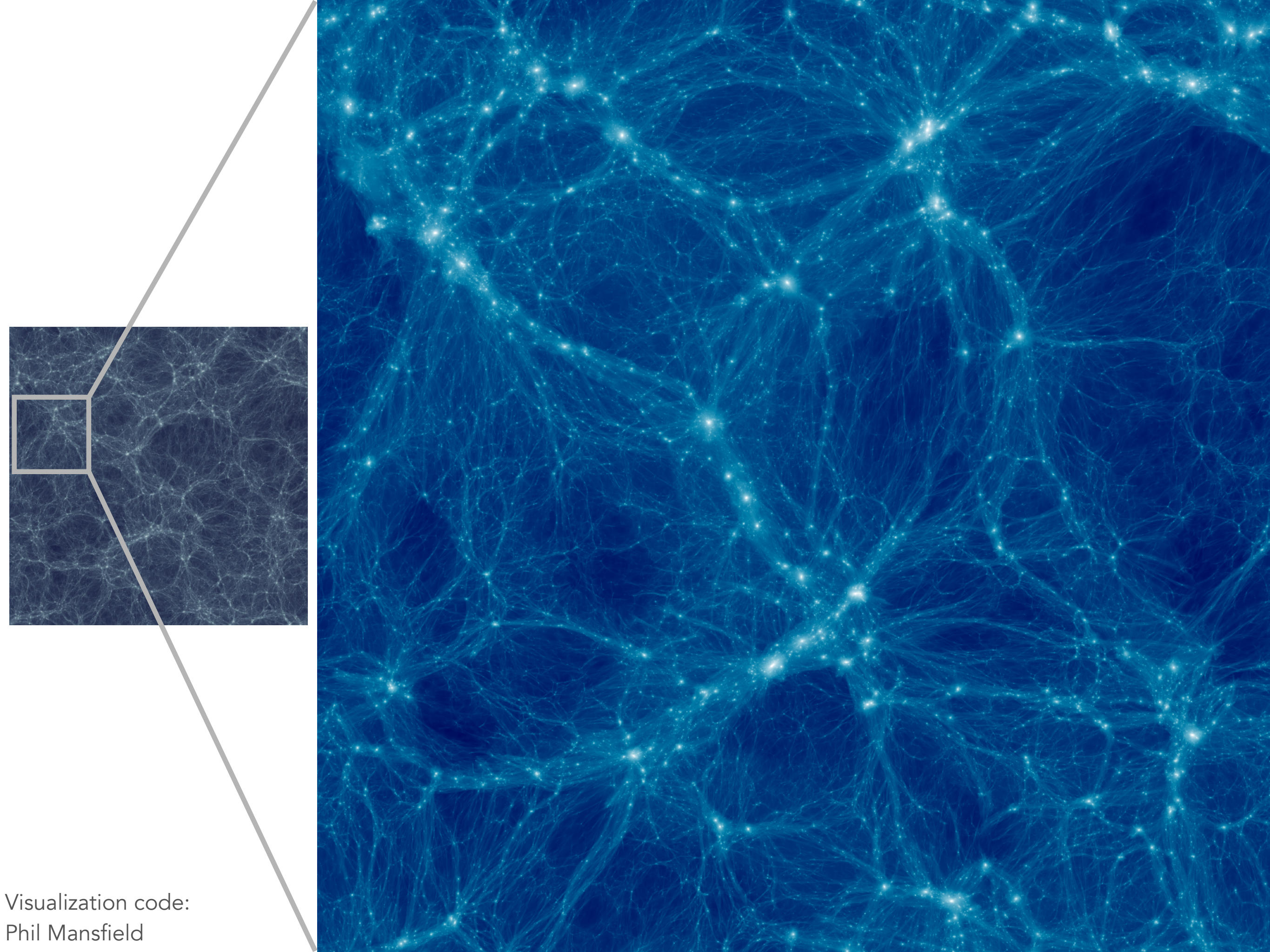


- Millennium Simulation (10 billion particles) was largest for a while
- Today reach **1 trillion** particles

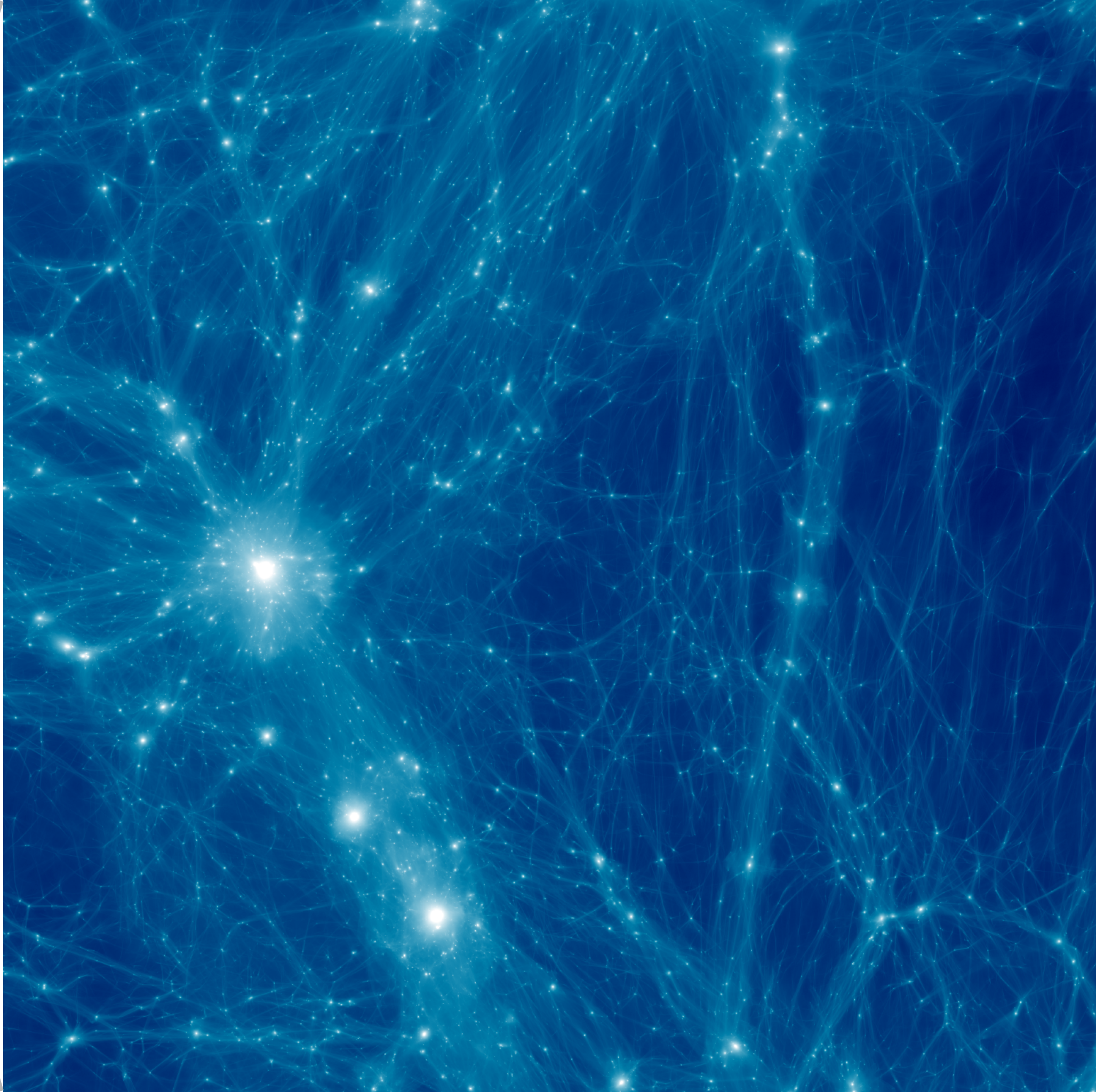
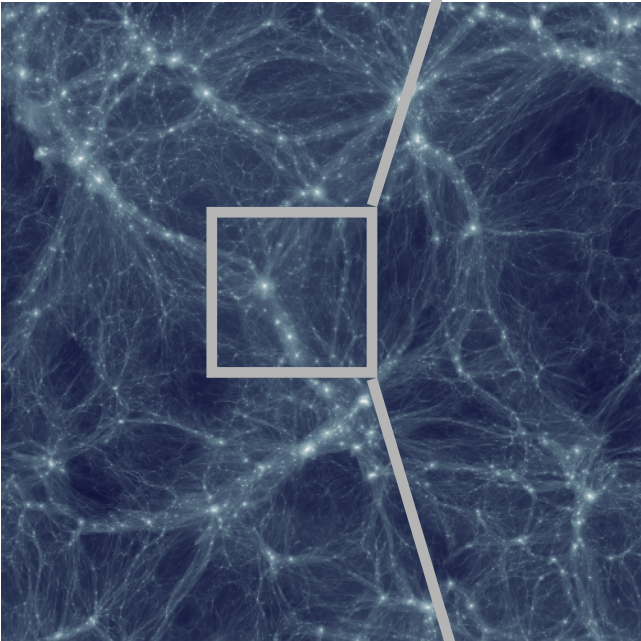
$a = 0.11$
 $t = 0.7 \text{ Gyr}$

$$a=0.1$$

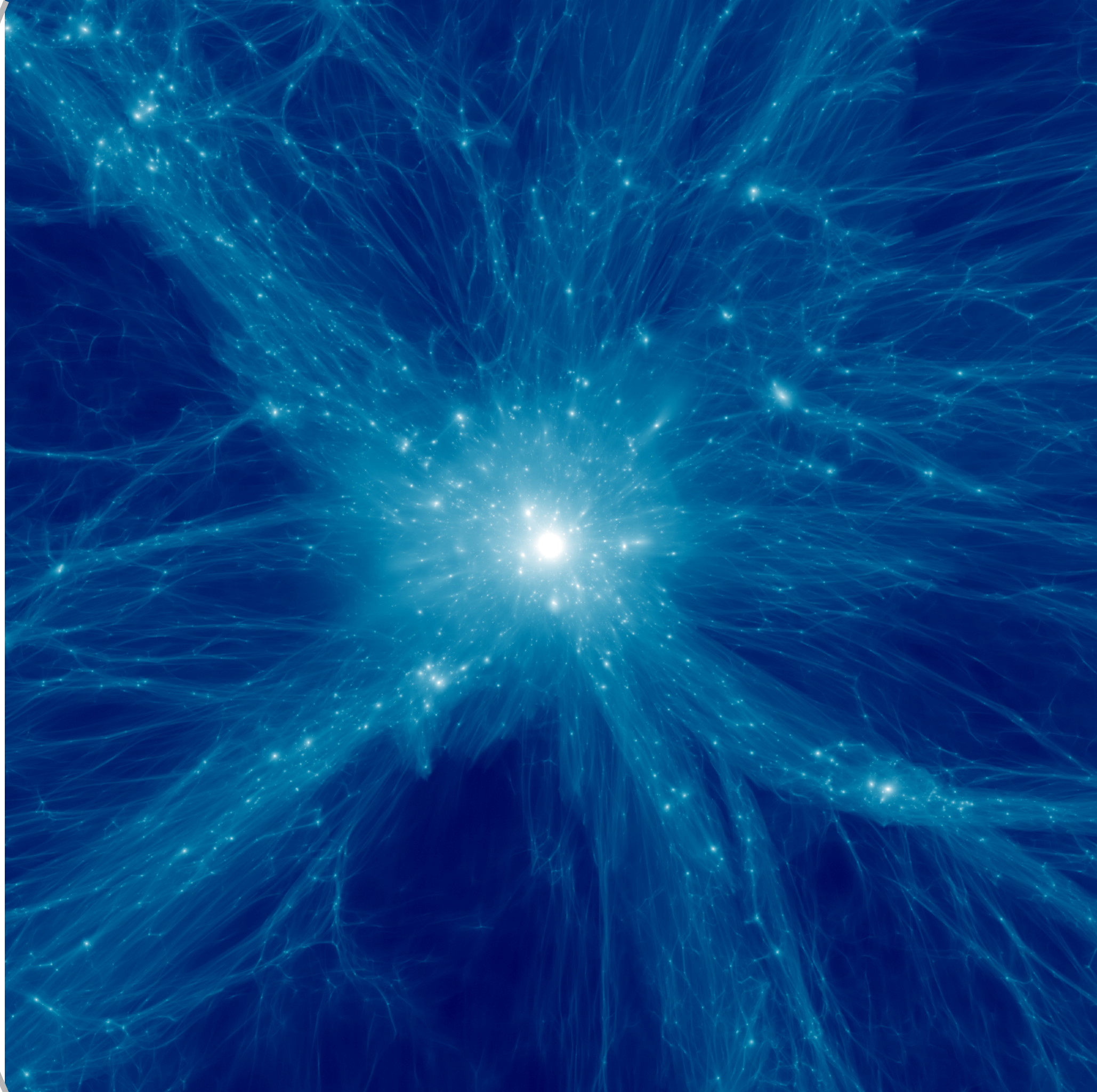
$$t=0.6 \text{ Gyr}$$



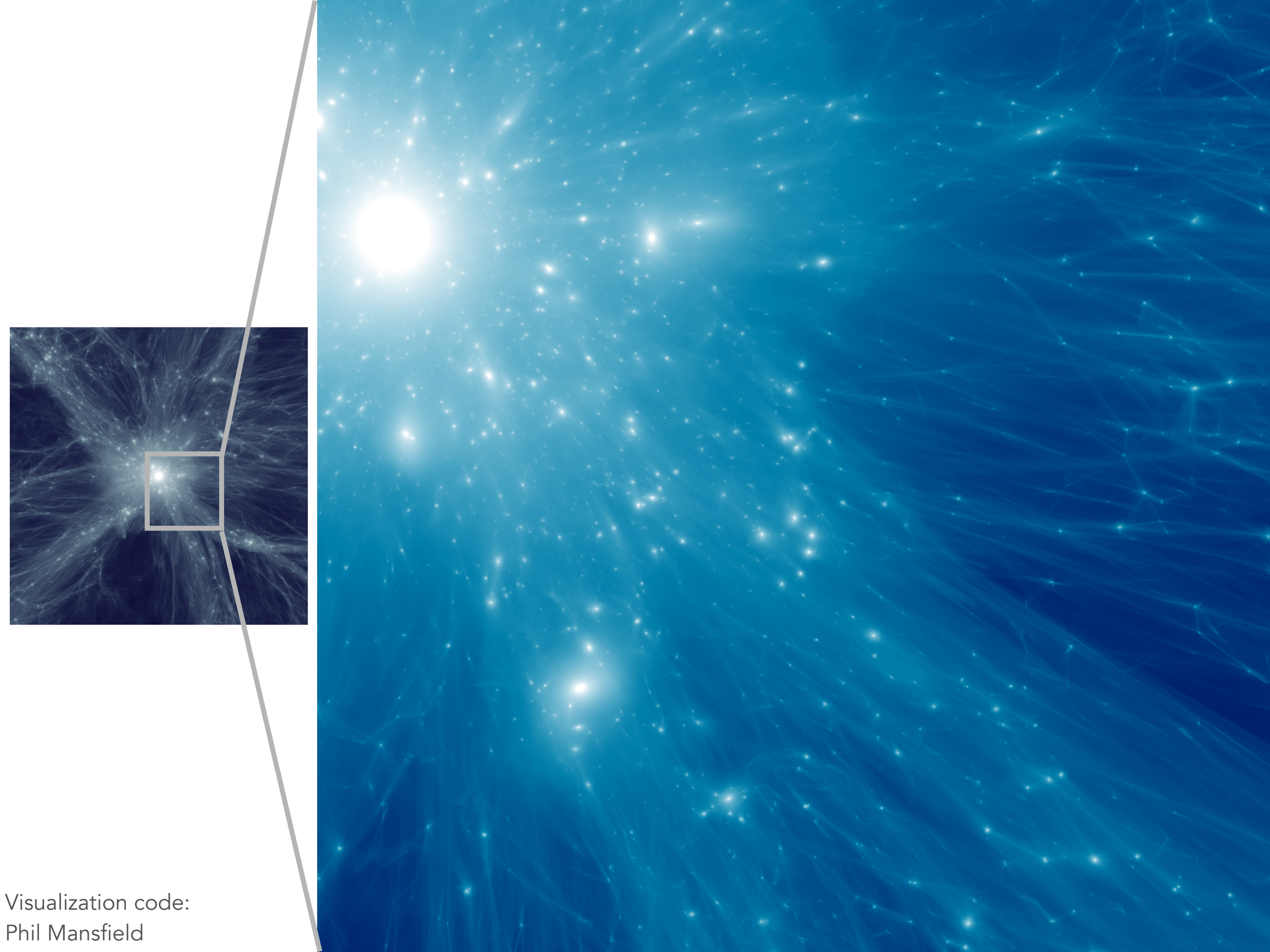
Visualization code:
Phil Mansfield



Visualization code:
Phil Mansfield



Visualization code:
Phil Mansfield

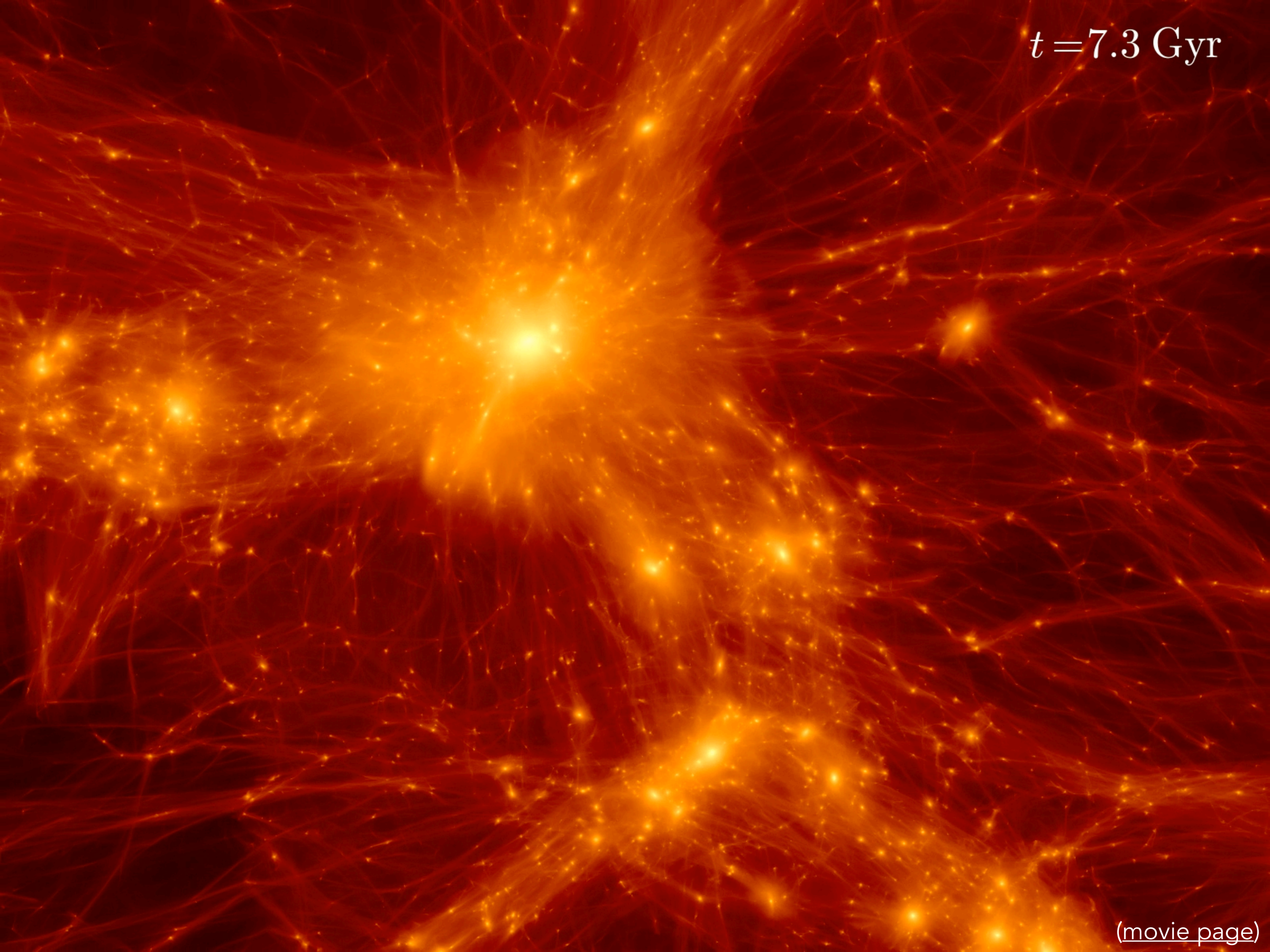


Visualization code:
Phil Mansfield

Formation of halos

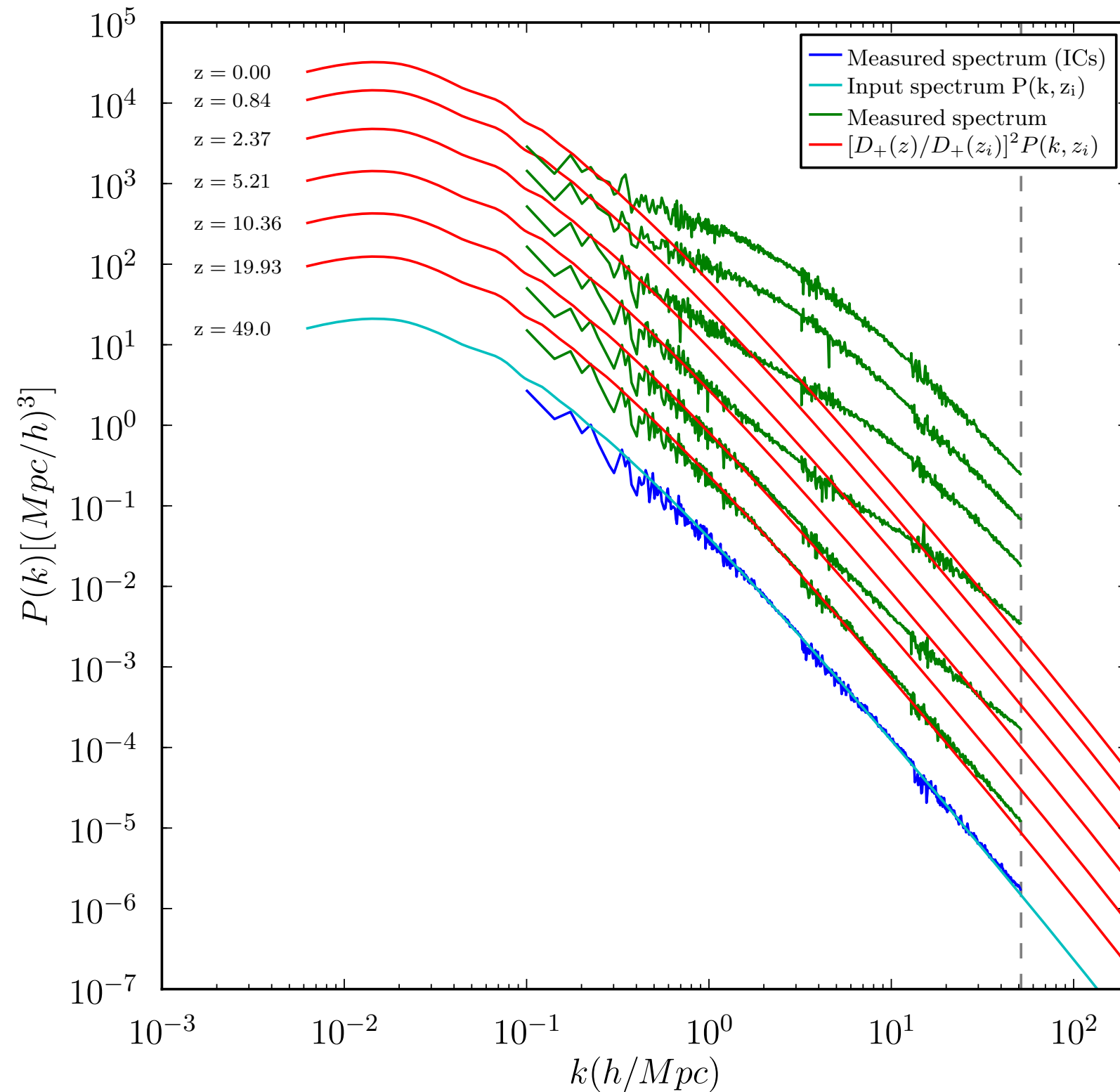
- Could occur...
 - Top-down: Form big structures first, which fragment to make smaller structures
 - Bottom-up: Form small structures first, which merge into big structures

$t = 7.3$ Gyr

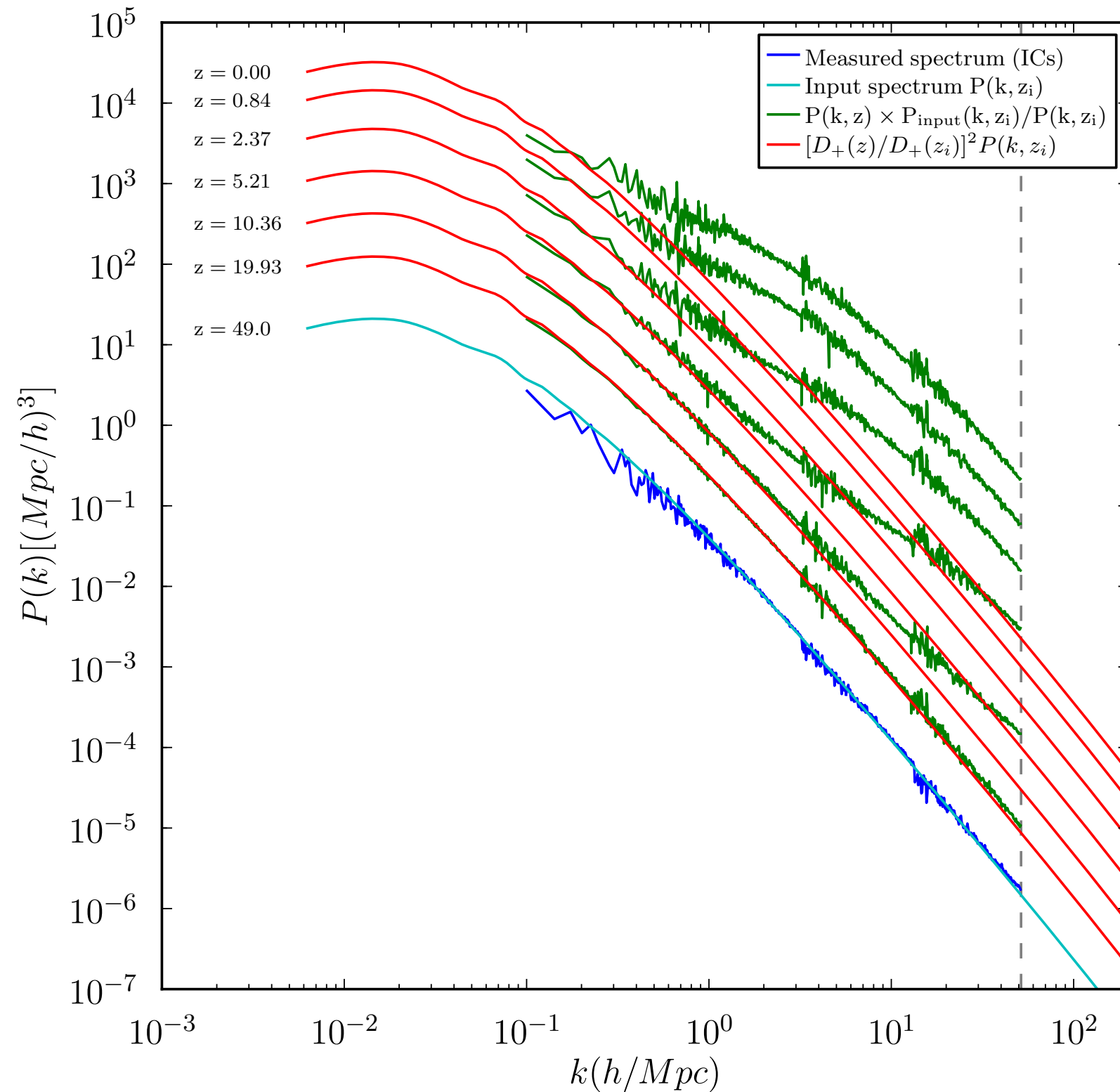


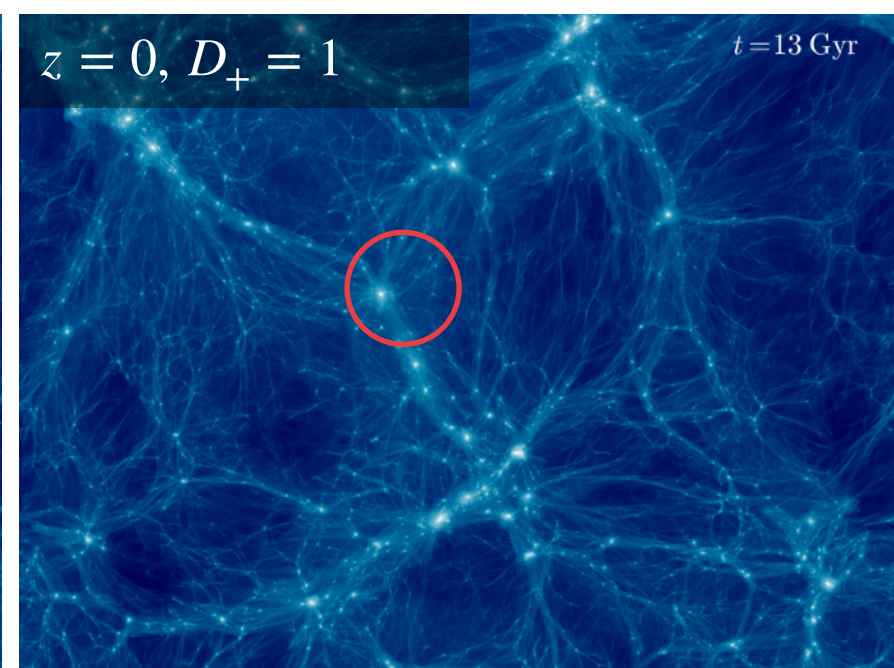
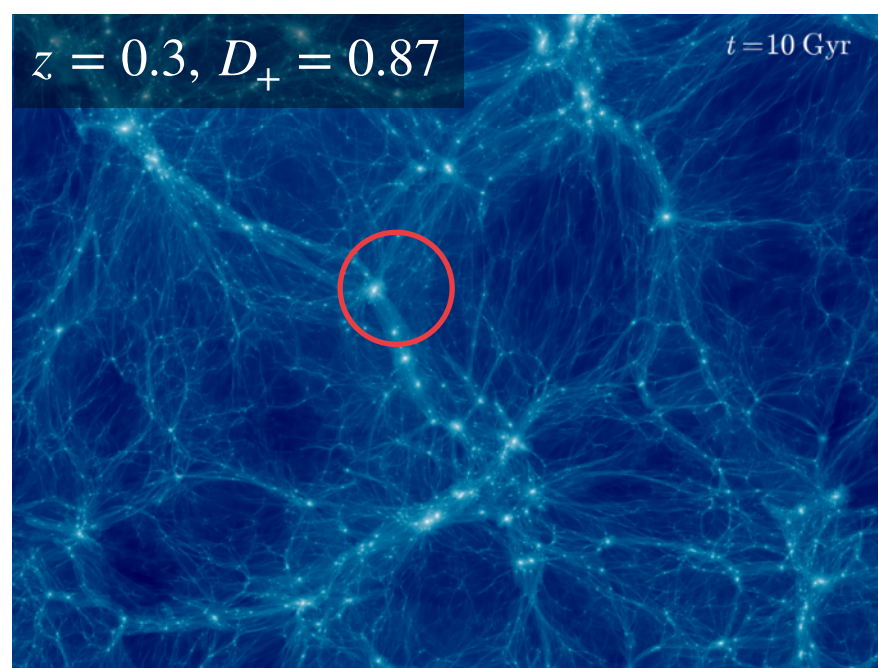
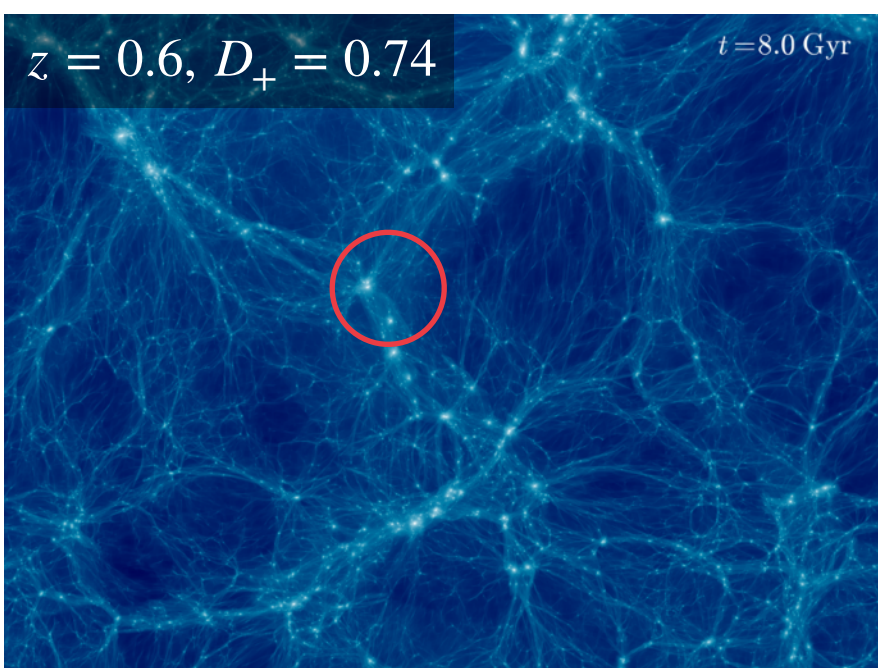
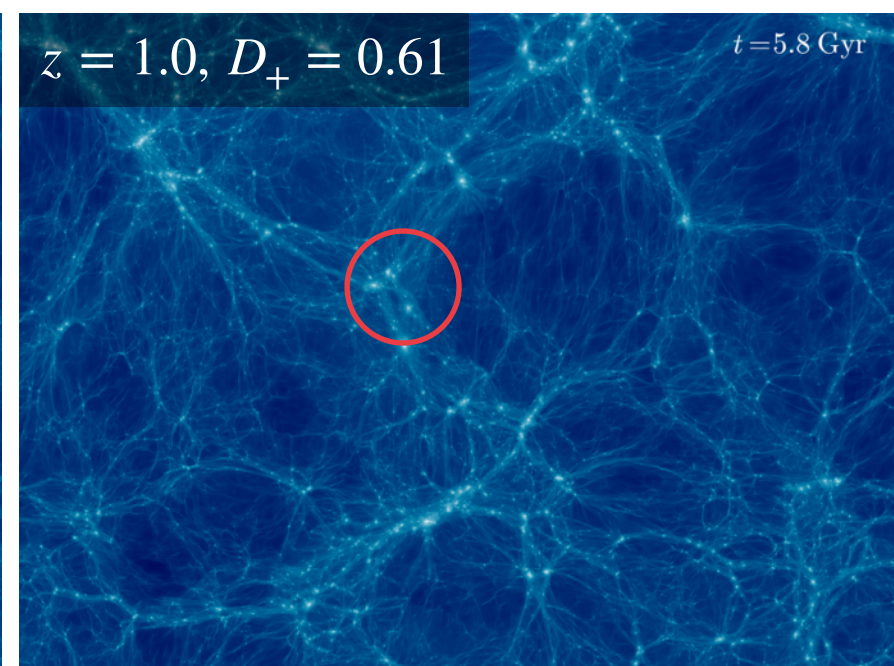
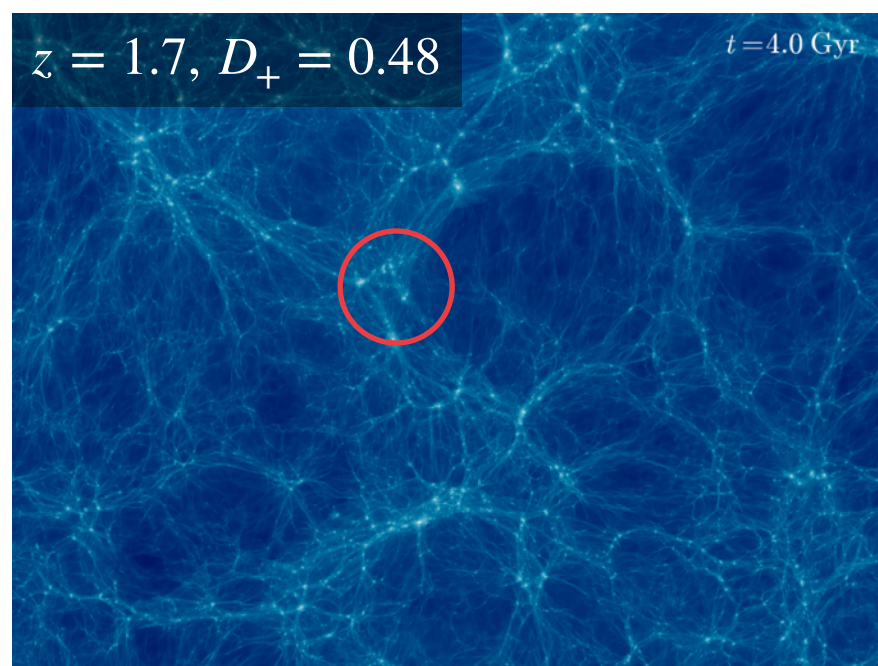
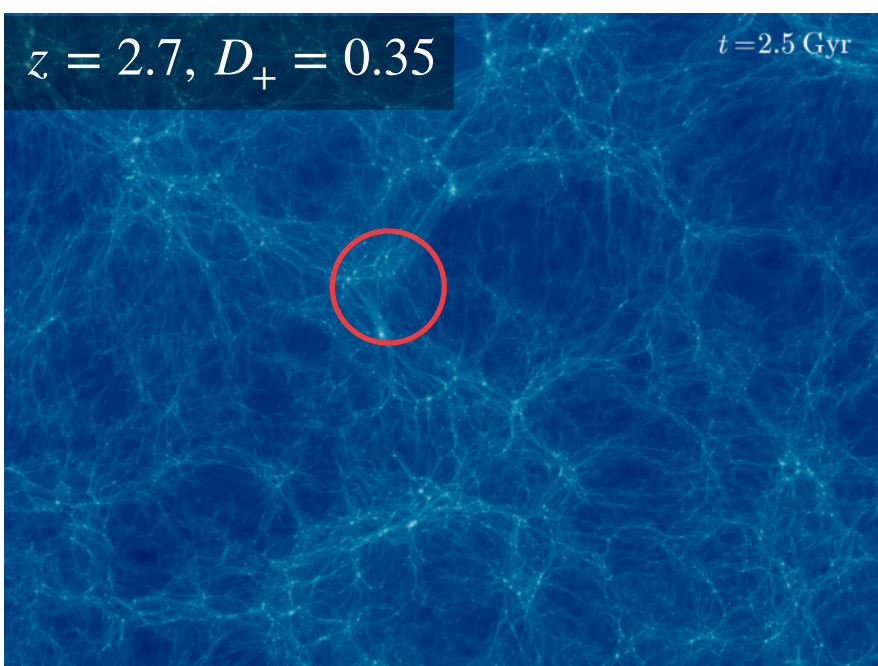
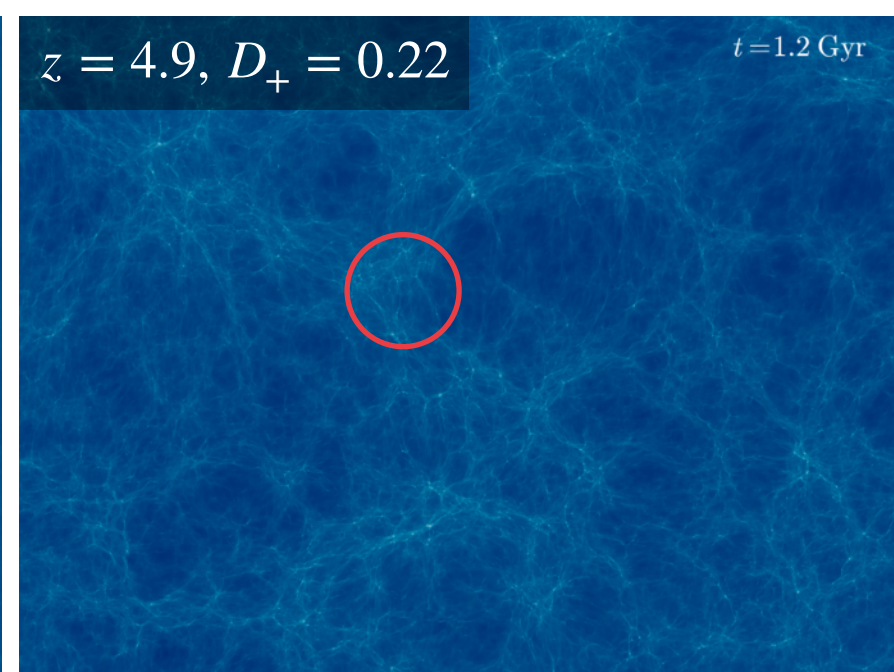
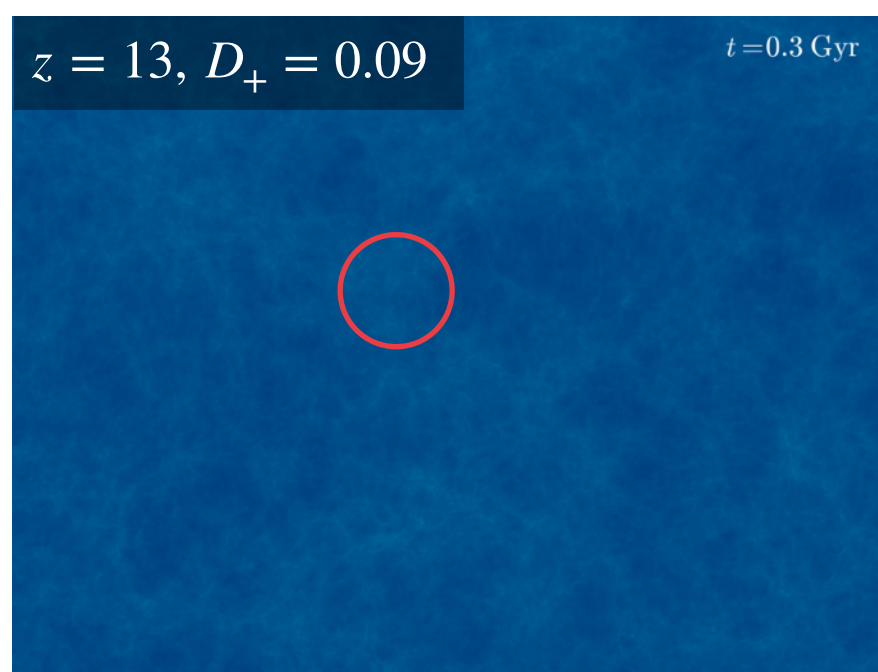
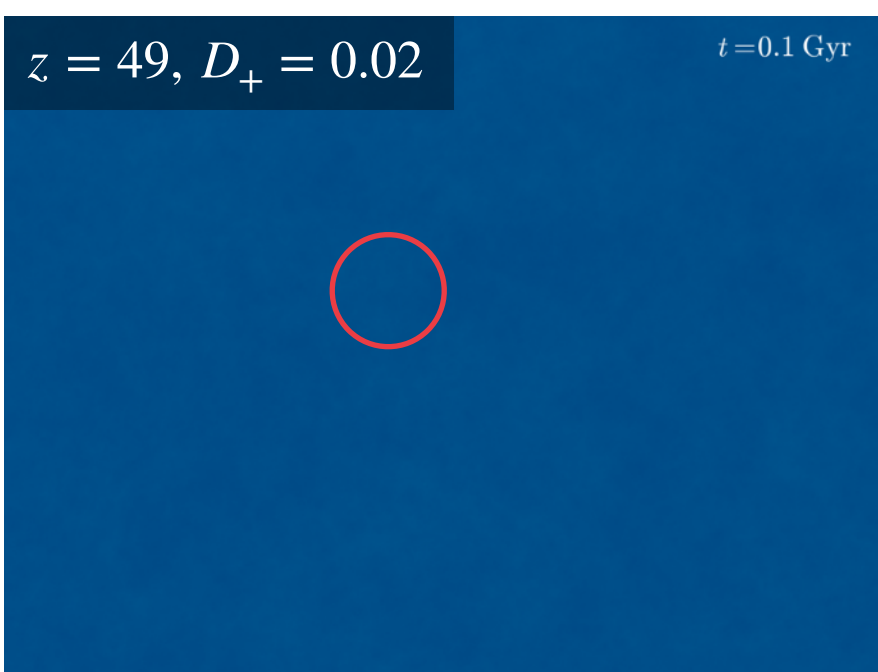
(movie page)

Evolution of power spectrum in simulation



Evolution of power spectrum in simulation





§4.1.1 • The tophat collapse model

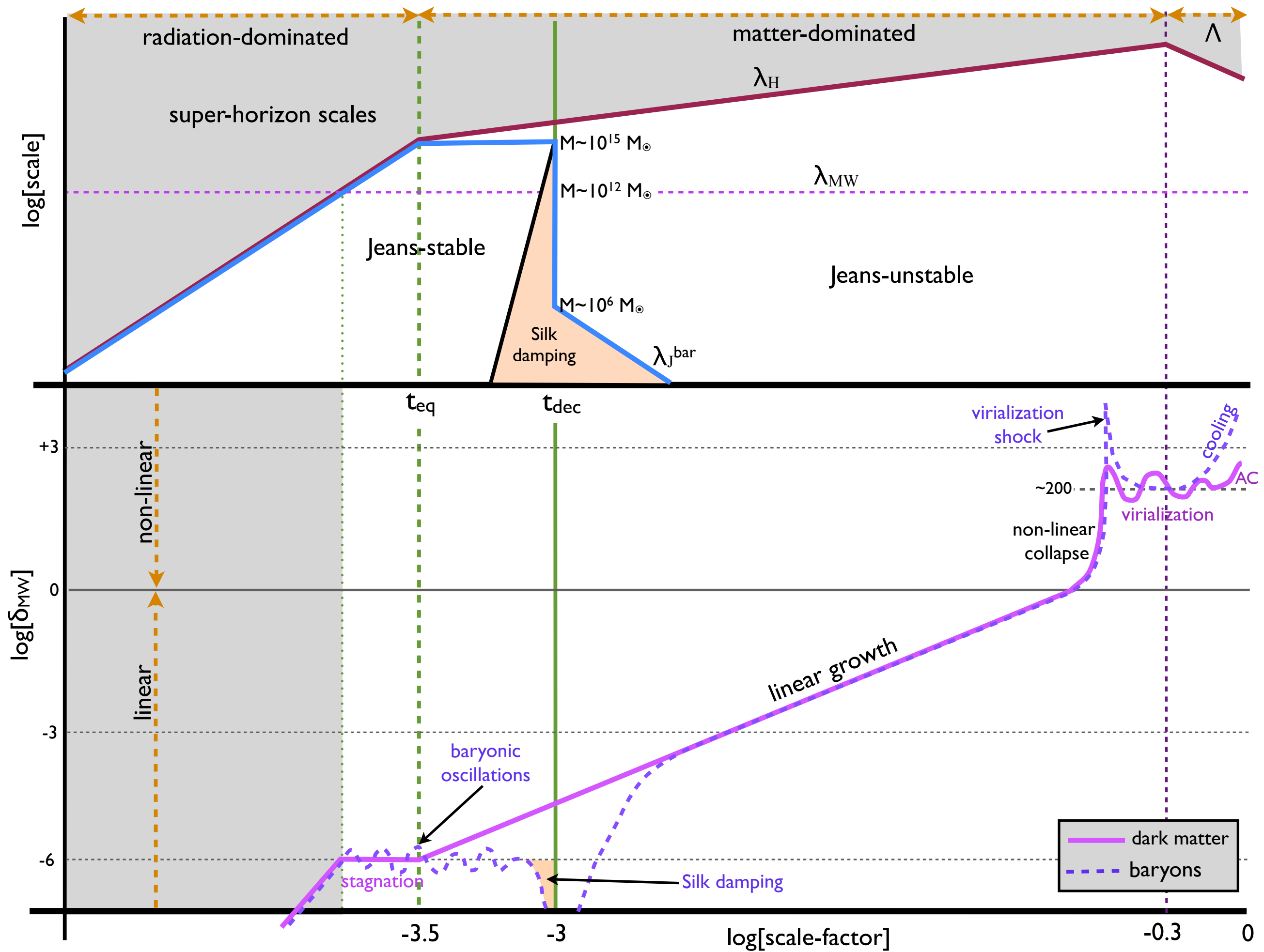
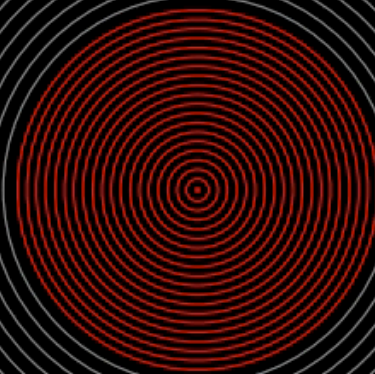


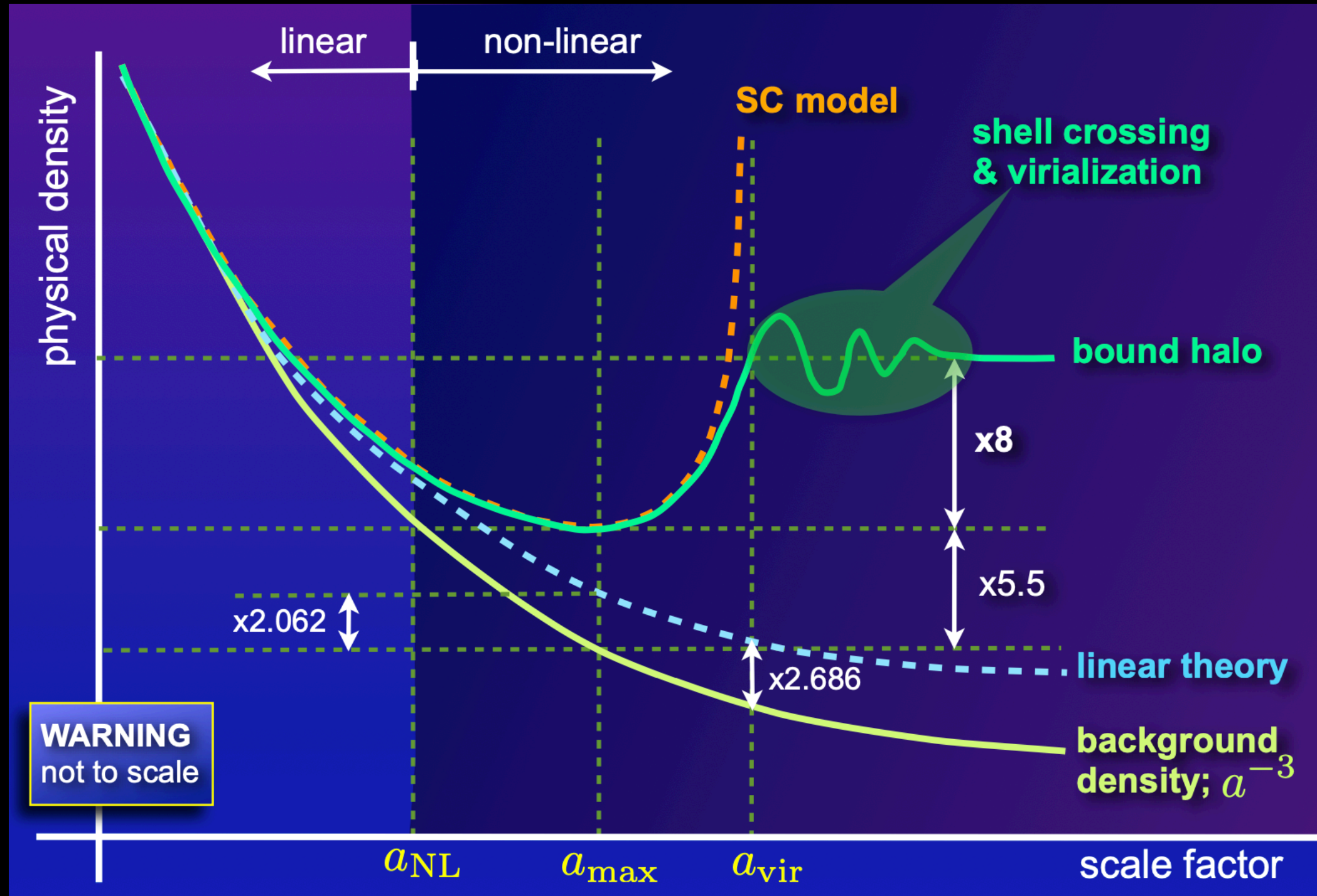
Figure by Frank van den Bosch

$$r/r_{\text{ta}} = 0.35$$

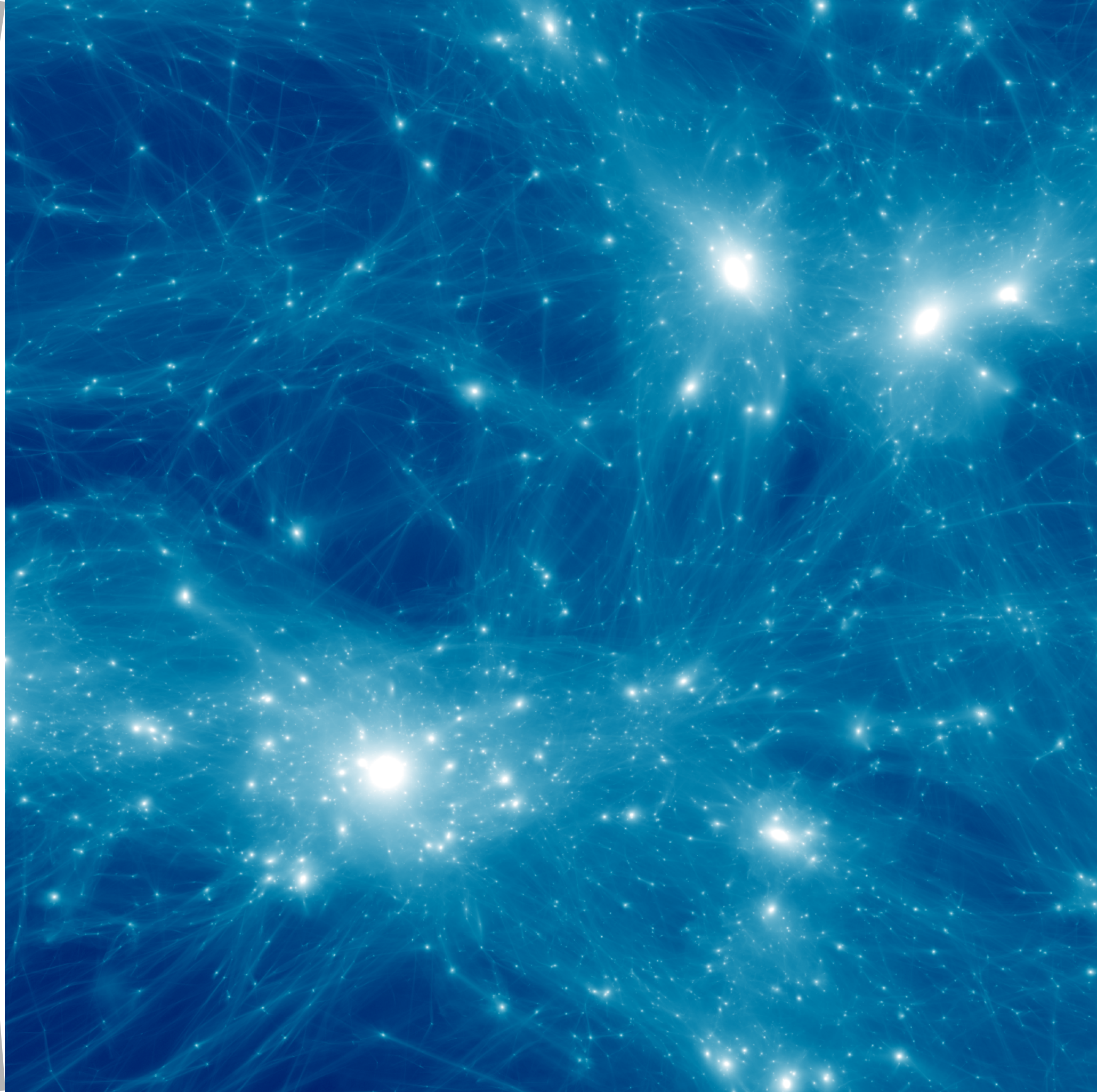
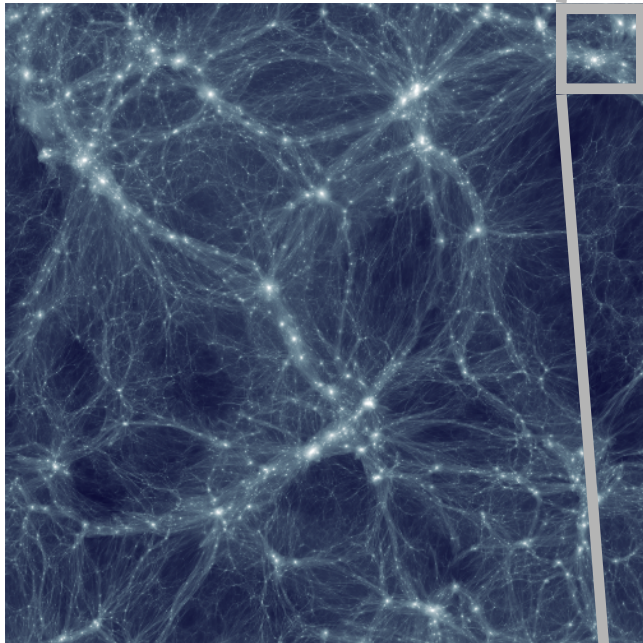
$$1 + \Delta = \rho_{\text{th}}/\rho_{\text{m}} = 1.3$$



Tophat collapse model

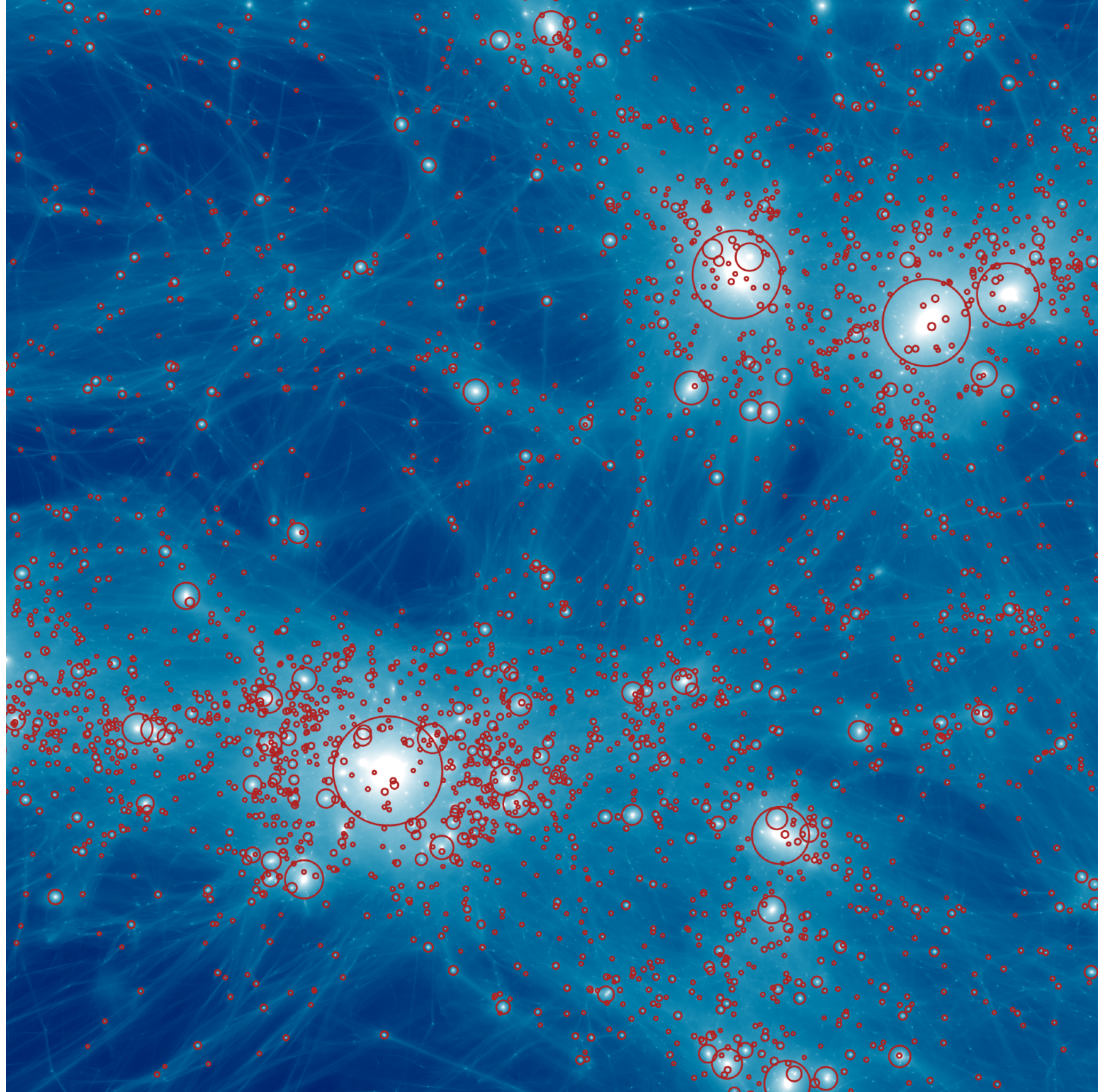


11 Mpc



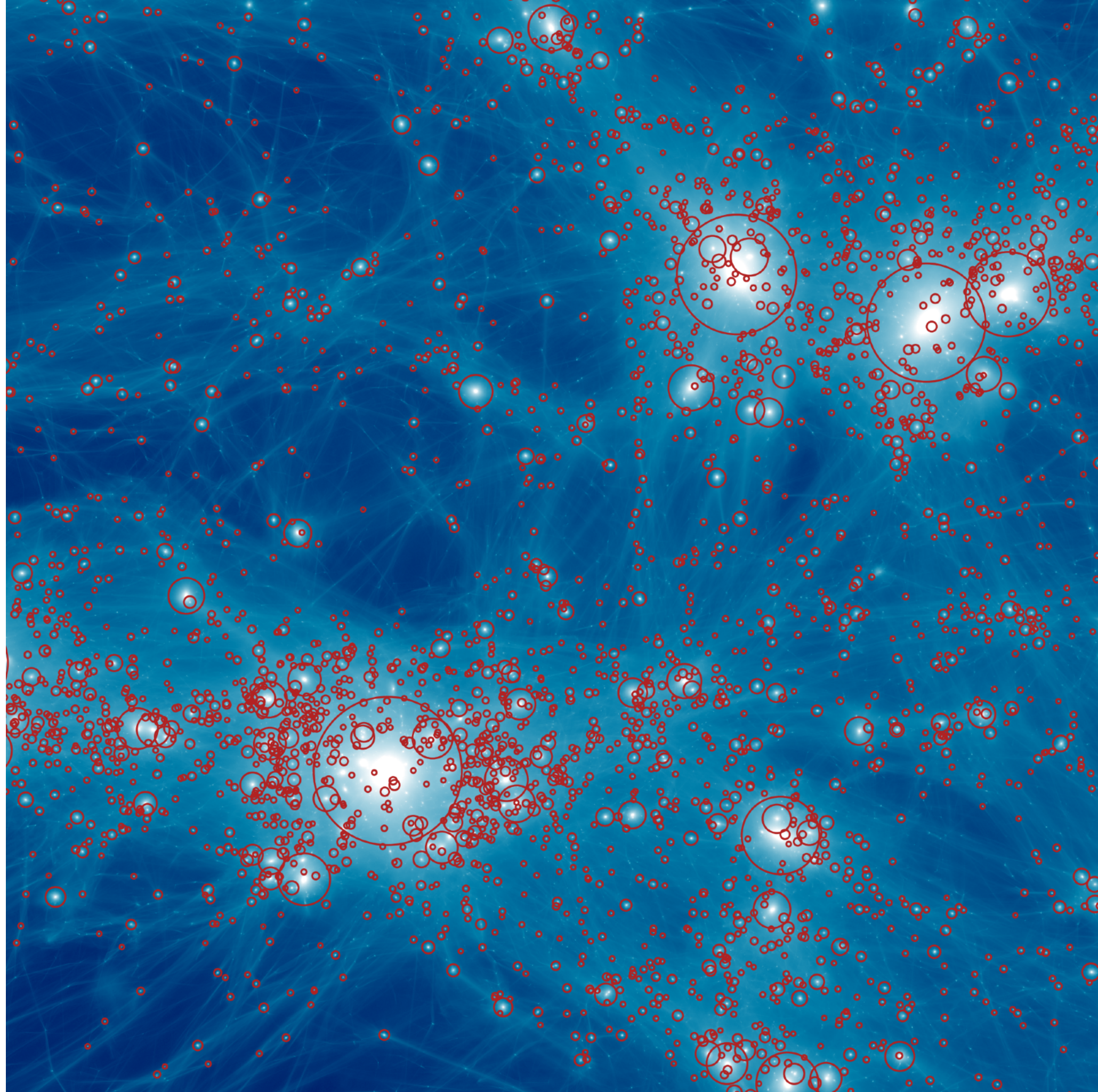
Visualization code:
Phil Mansfield

R_{500c}



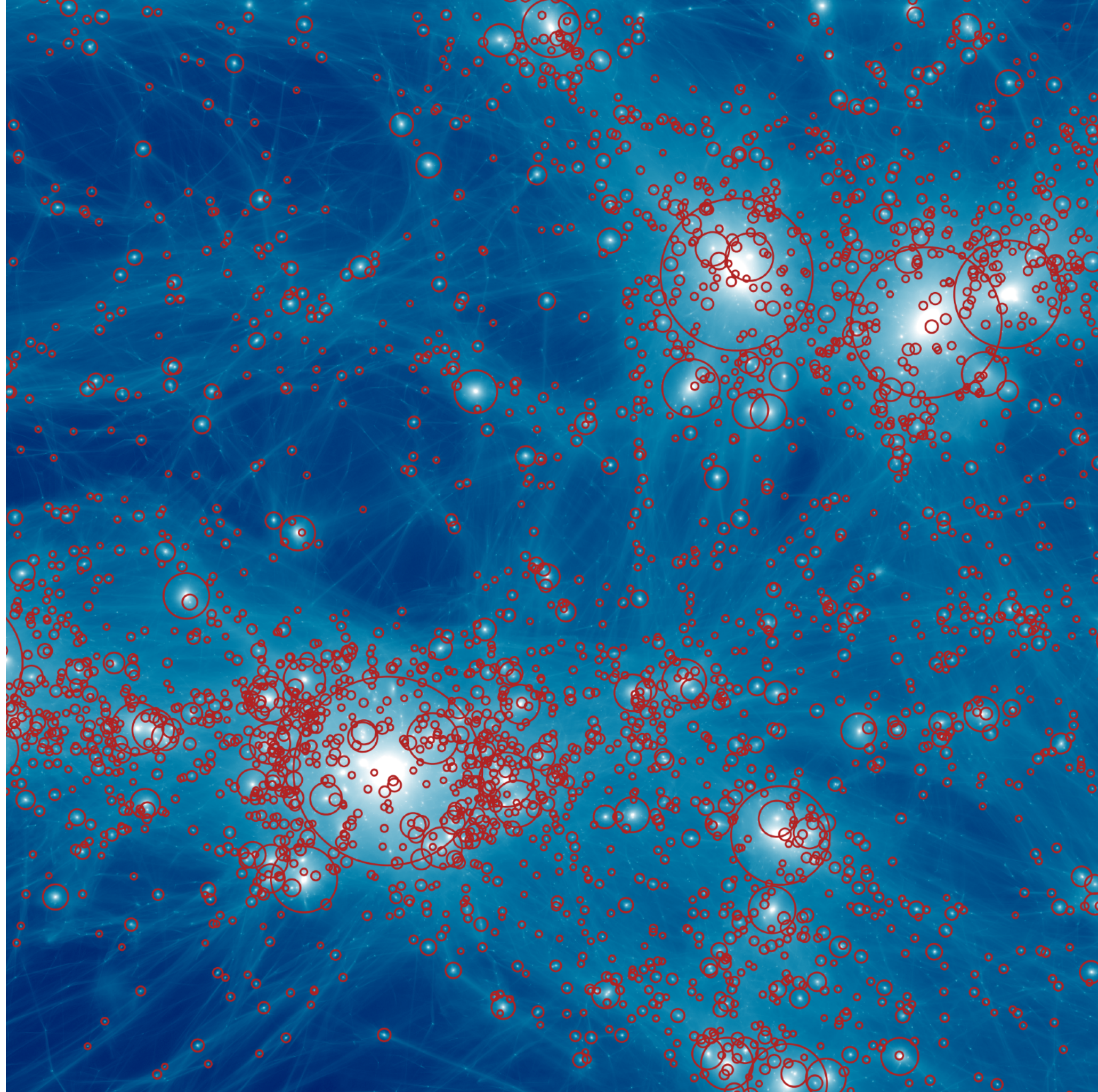
Halo finder: Rockstar
(Behroozi et al. 2013)

R_{200c}

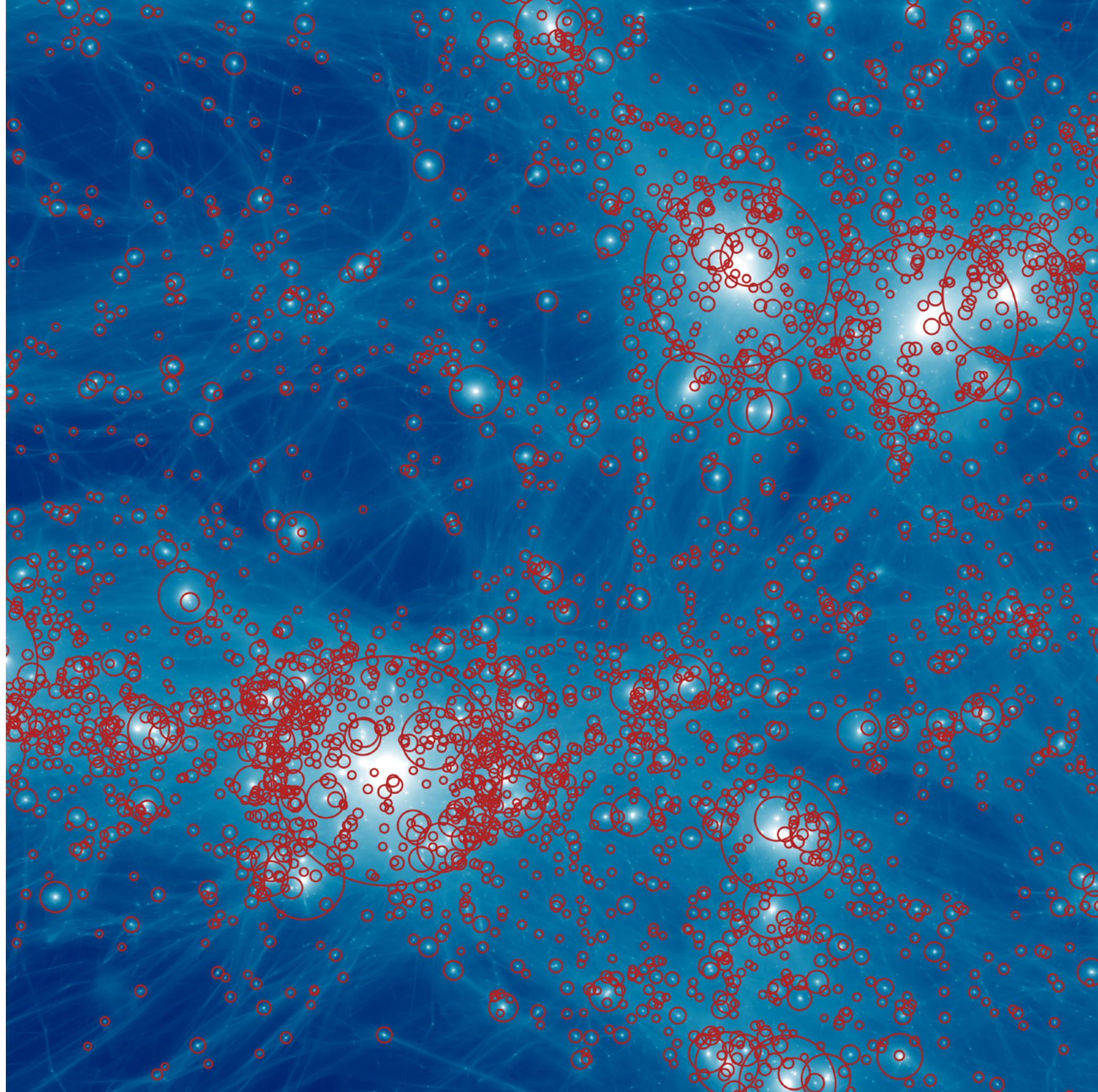


Halo finder: Rockstar
(Behroozi et al. 2013)

R_{vir}



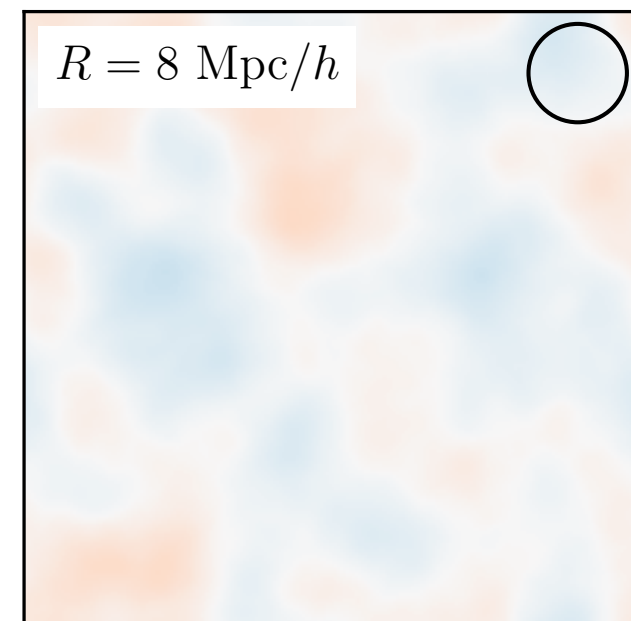
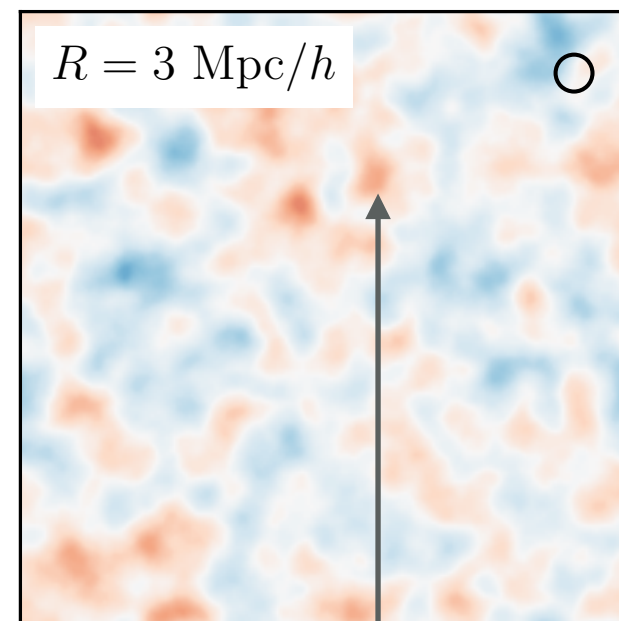
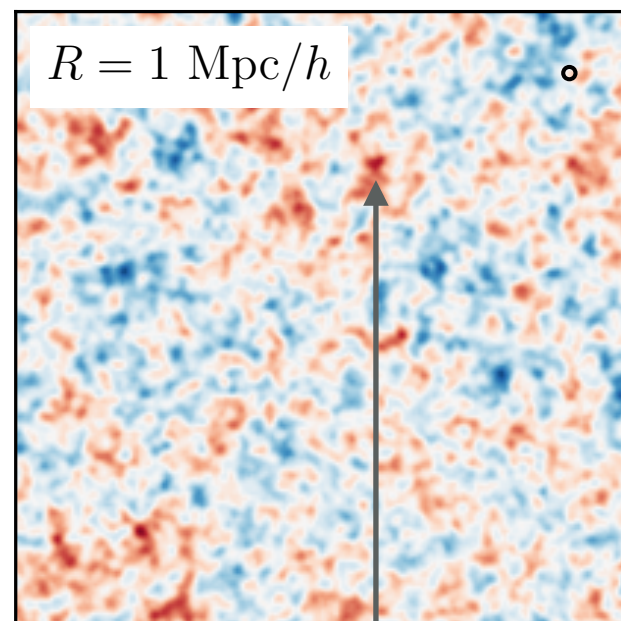
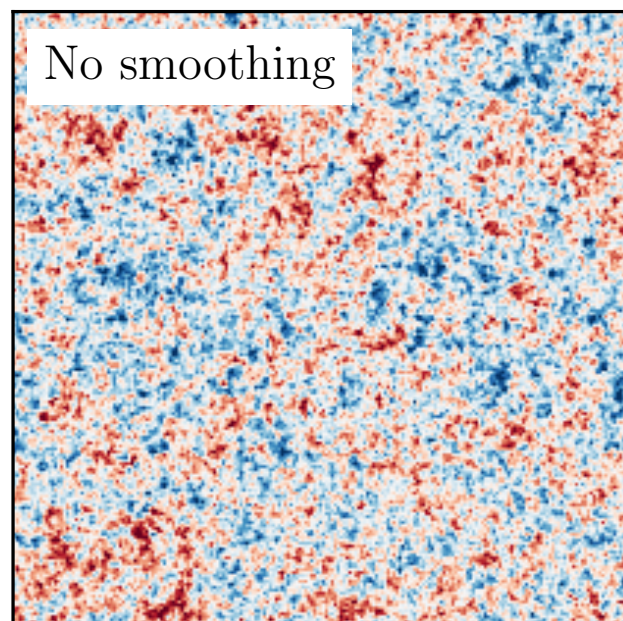
R_{200m}



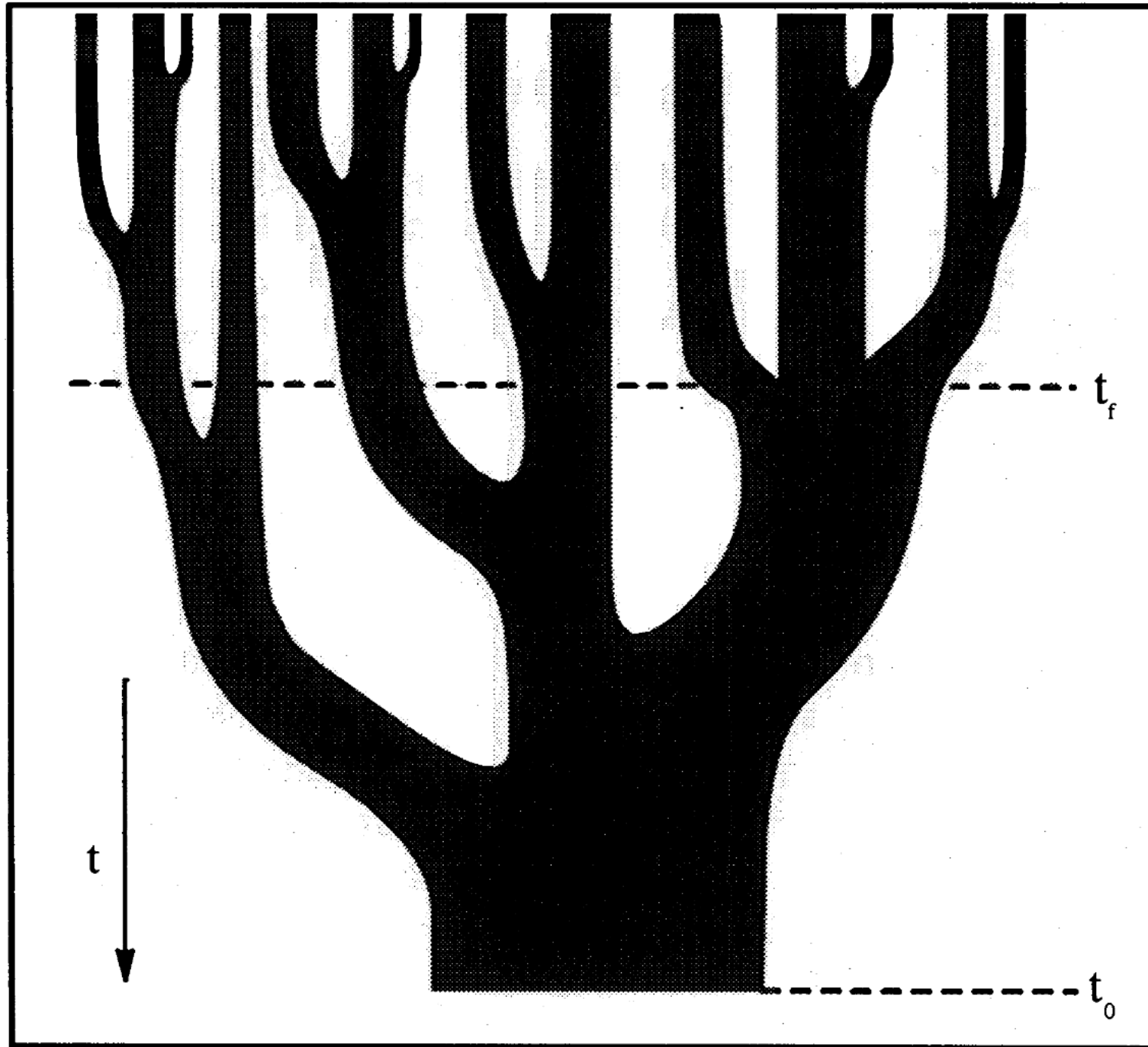
Halo finder: Rockstar
(Behroozi et al. 2013)

**§4.1.2 • The non-linear mass
and hierarchical structure formation**

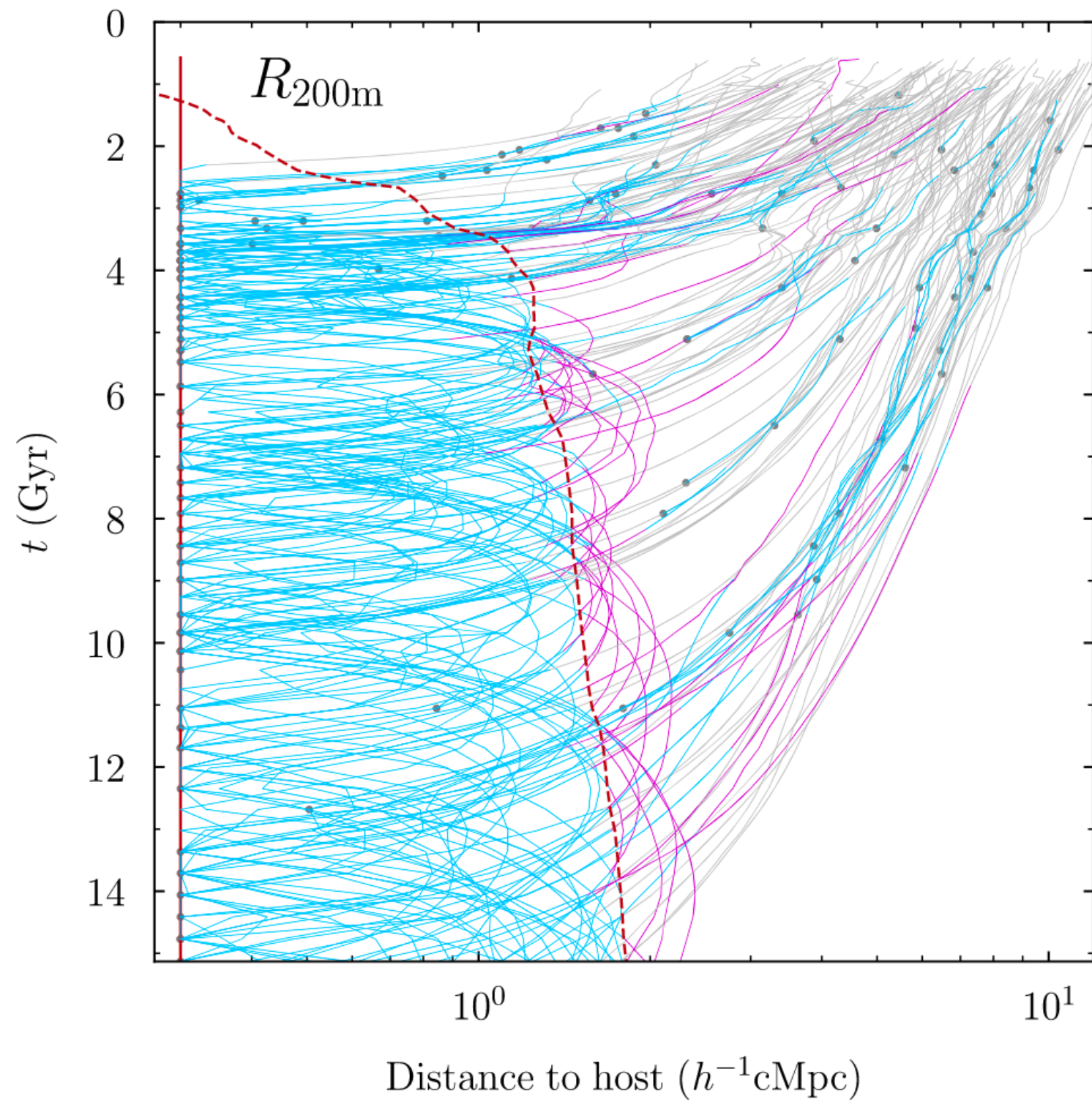
Smoothed density fields



Merger tree

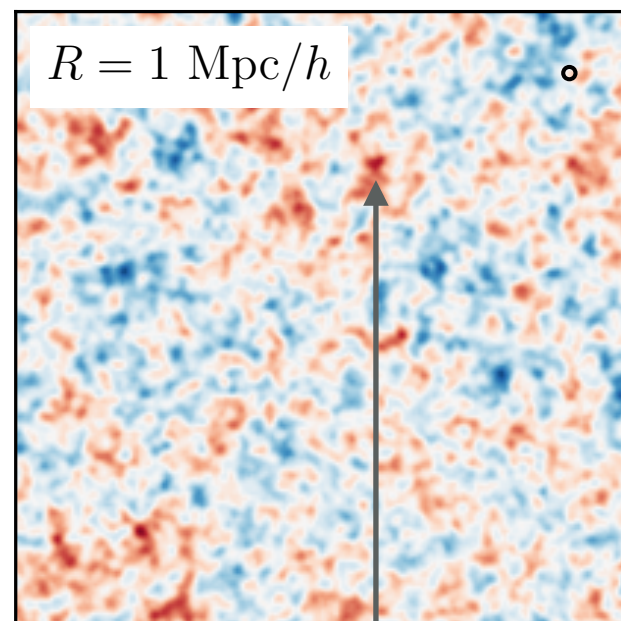
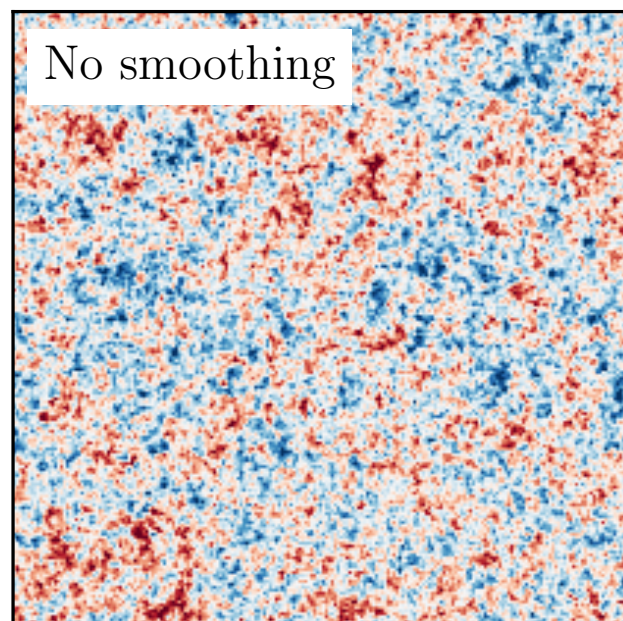


Merger tree

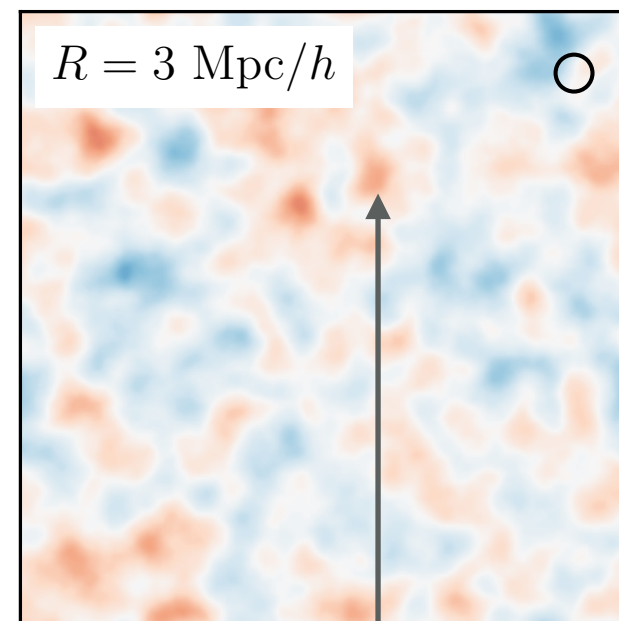


§4.2 • The halo mass function

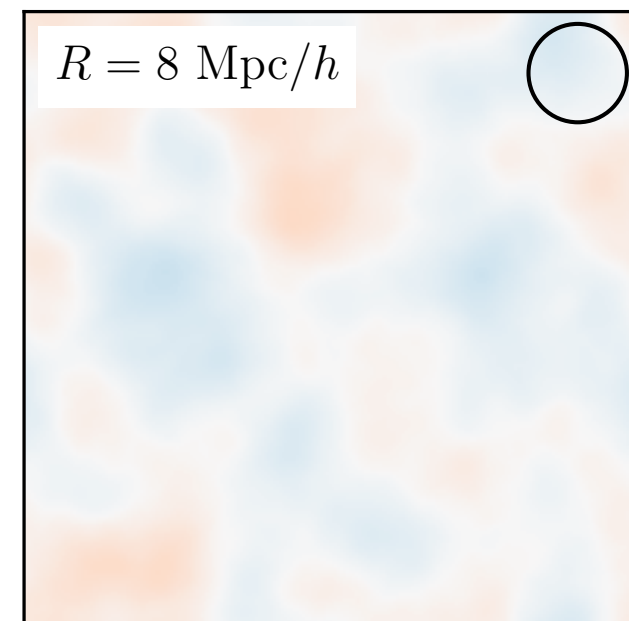
Smoothed density fields



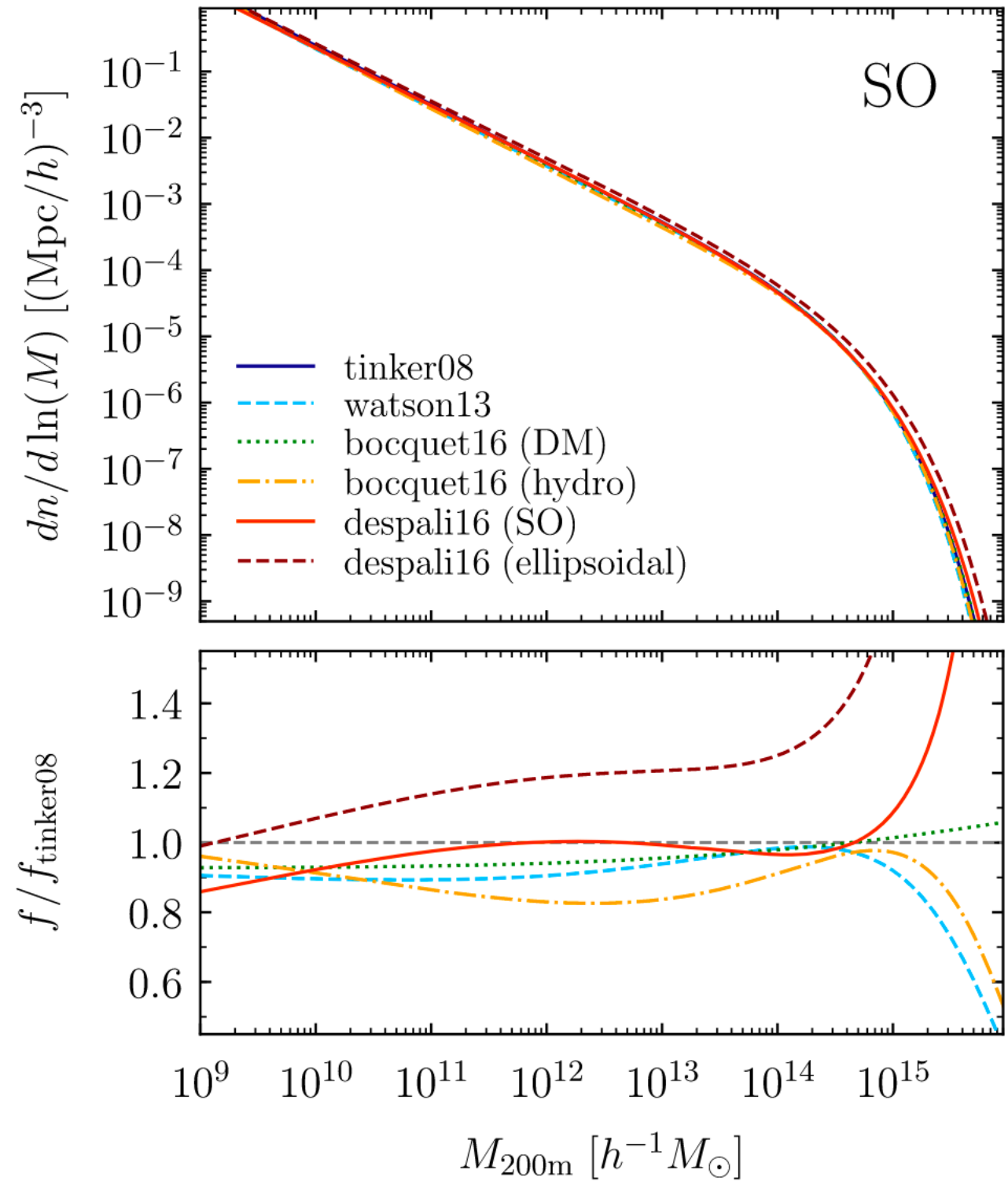
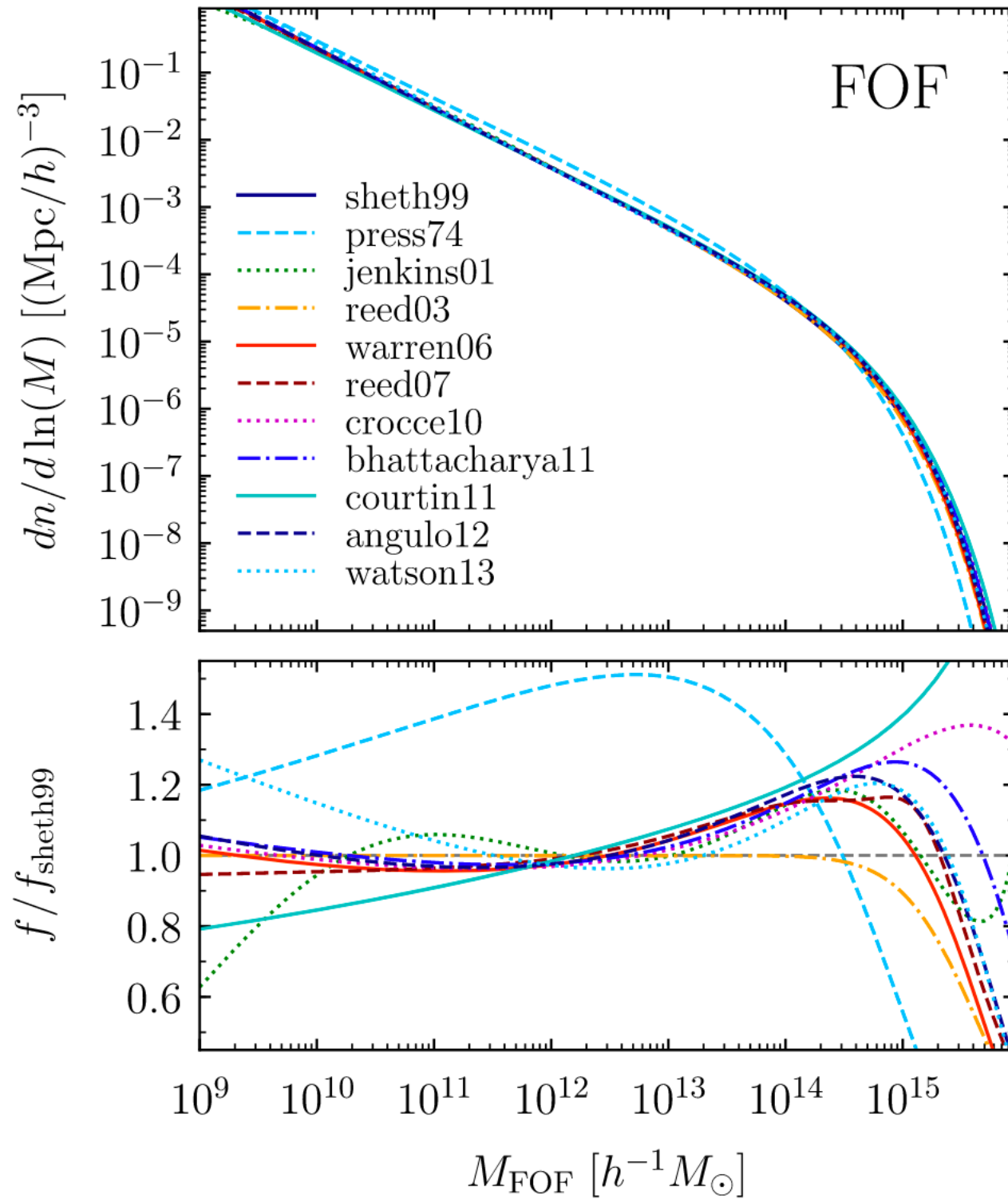
$$\delta_s > \delta_c$$



$$\delta_s < \delta_c$$



Mass function models



**§4.3 • Halo structure
and its connection to formation history**

Erebos N-body simulations

2000 Mpc/h

Density at $z = 0$

1000 Mpc/h

500 Mpc/h

250 Mpc/h

125 Mpc/h

62.5 Mpc/h

2000 Mpc/h

1000 Mpc/h

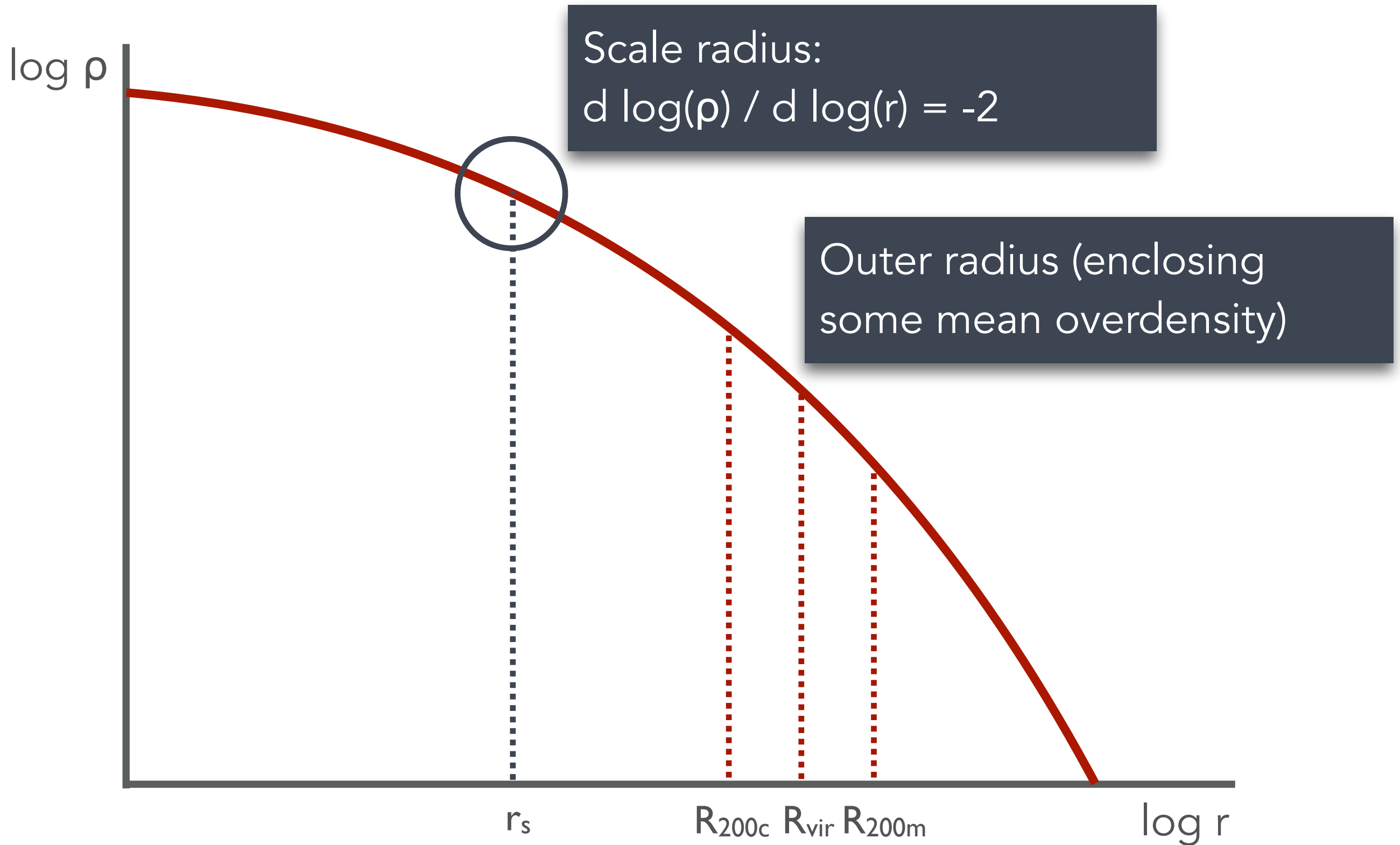
500 Mpc/h

250 Mpc/h

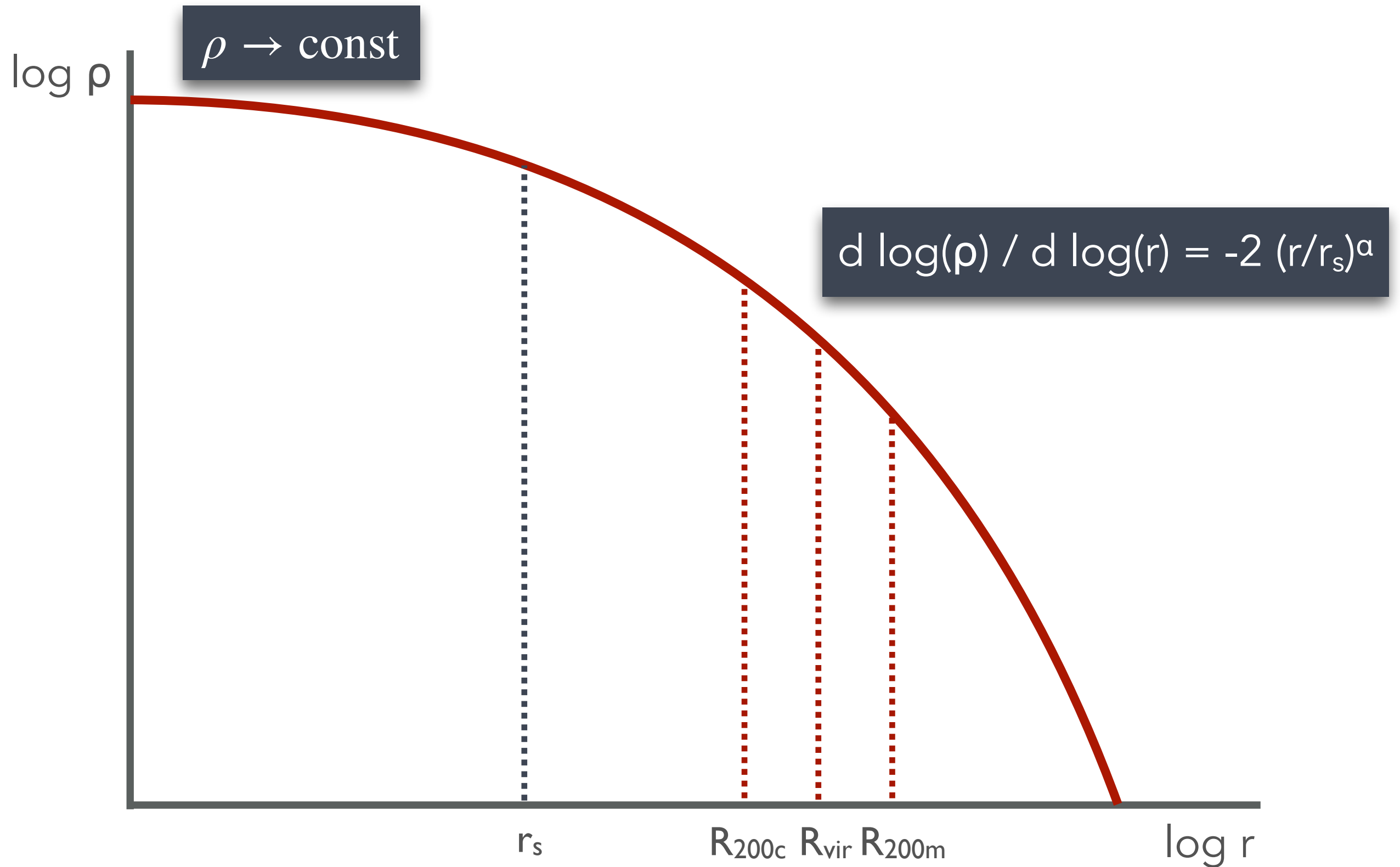
125 Mpc/h

62.5 Mpc/h

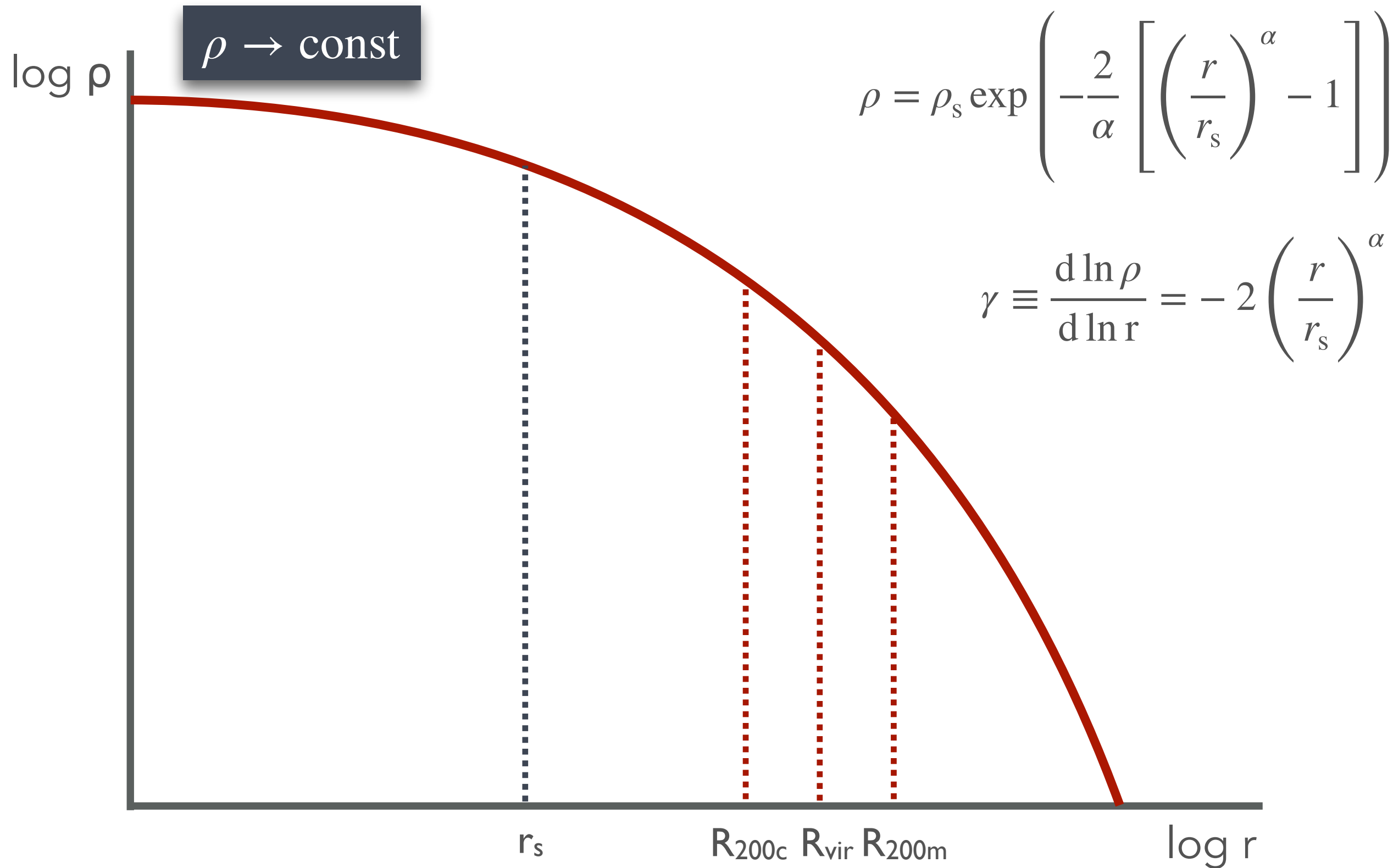
Density profile



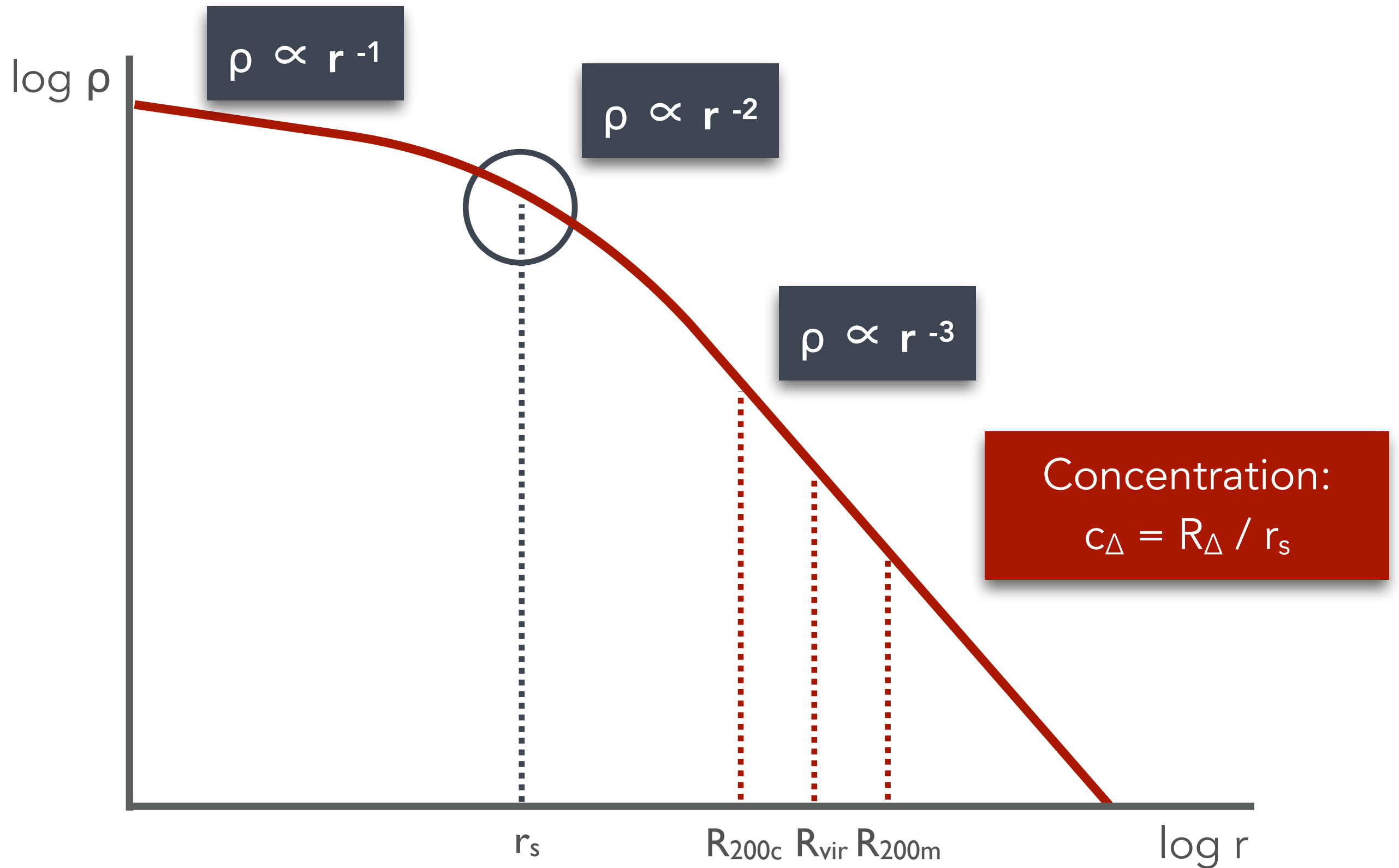
Einasto profile



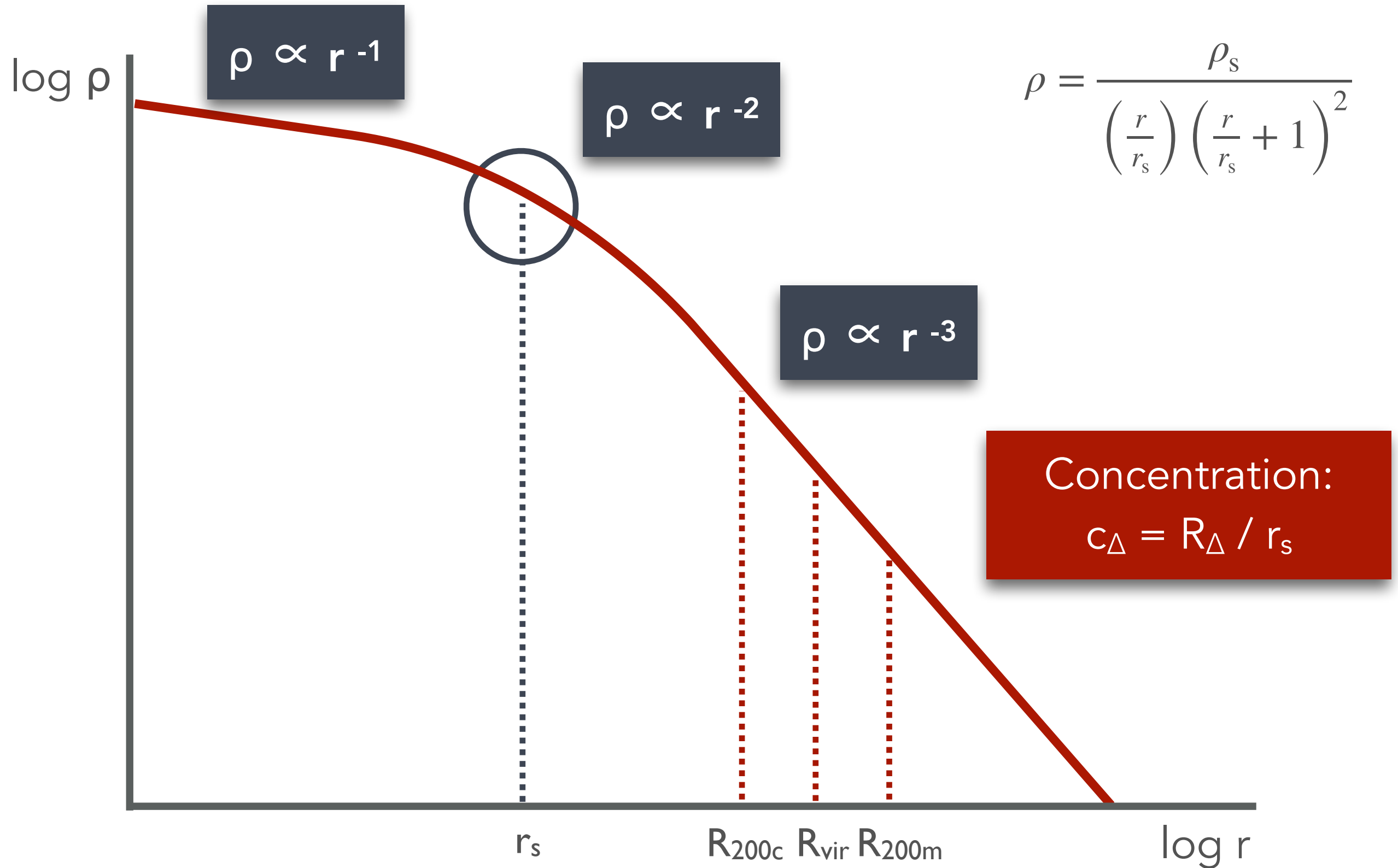
Einasto profile



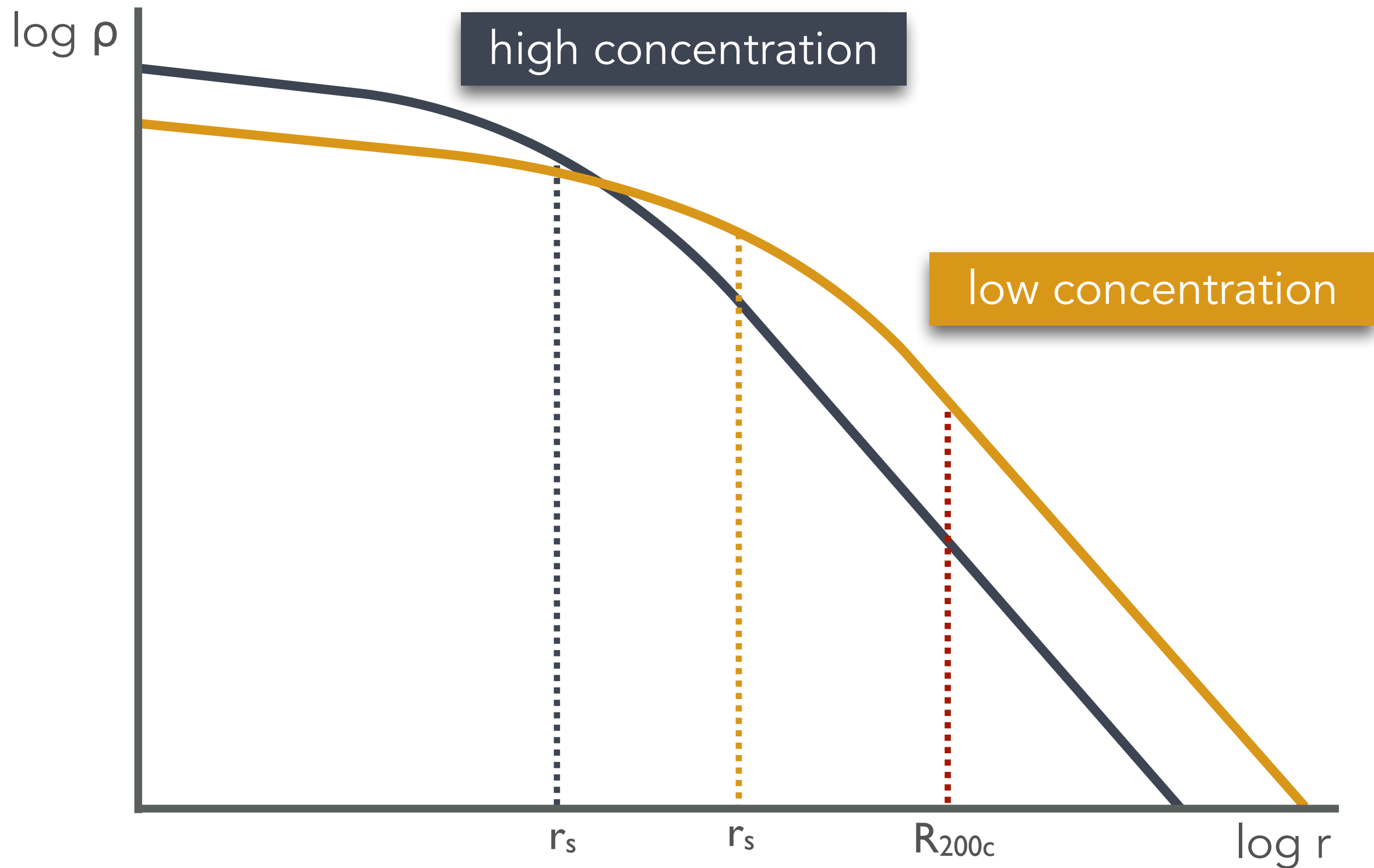
Navarro-Frenk-White profile

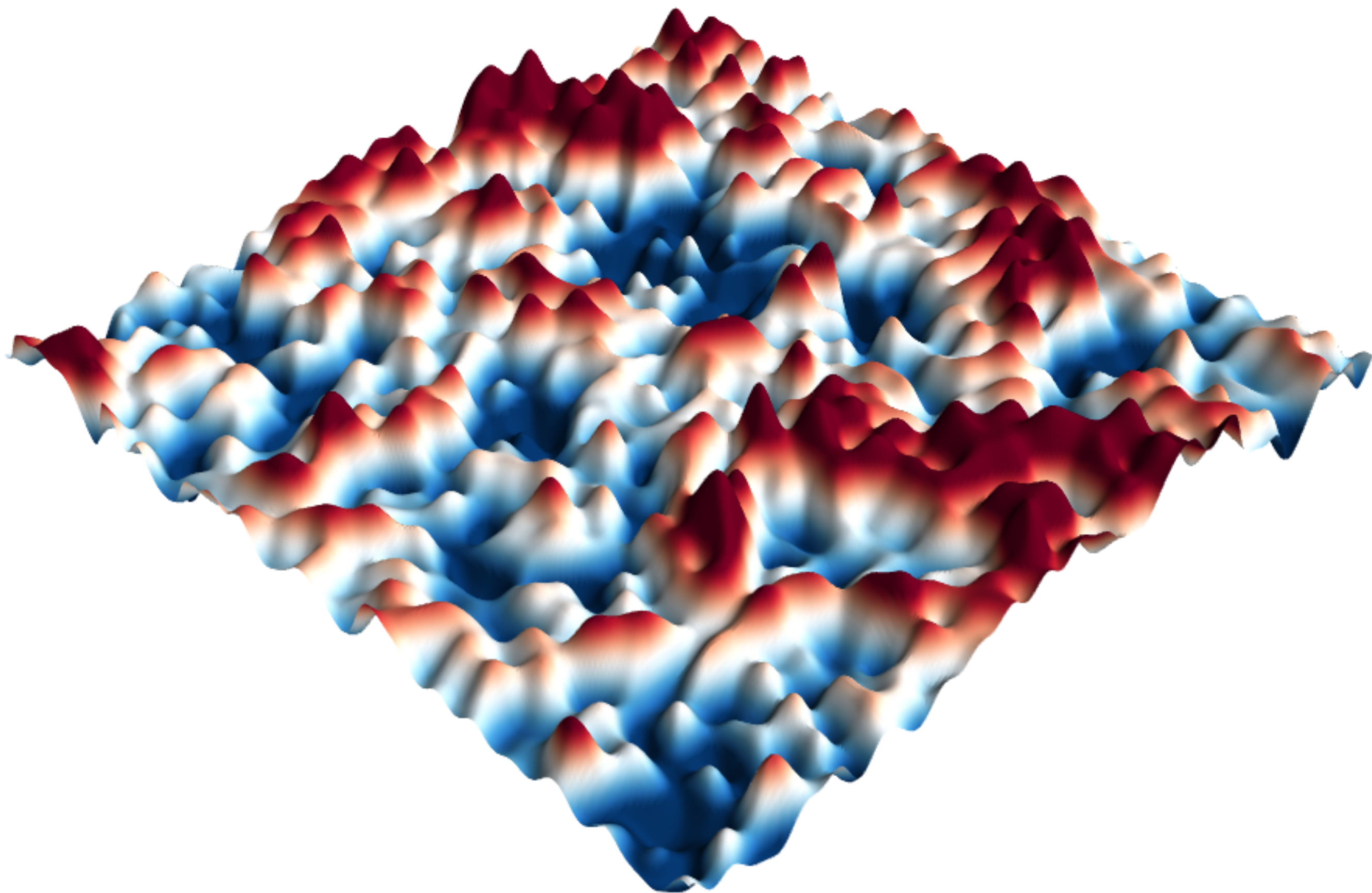


Navarro-Frenk-White profile

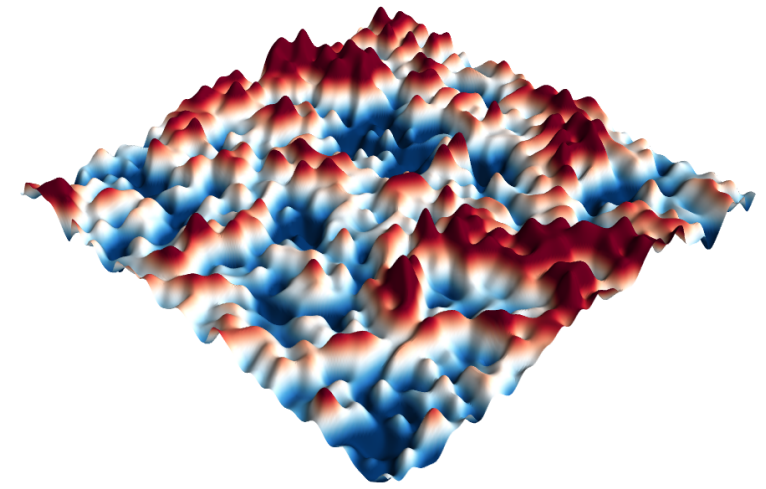


Navarro-Frenk-White profile

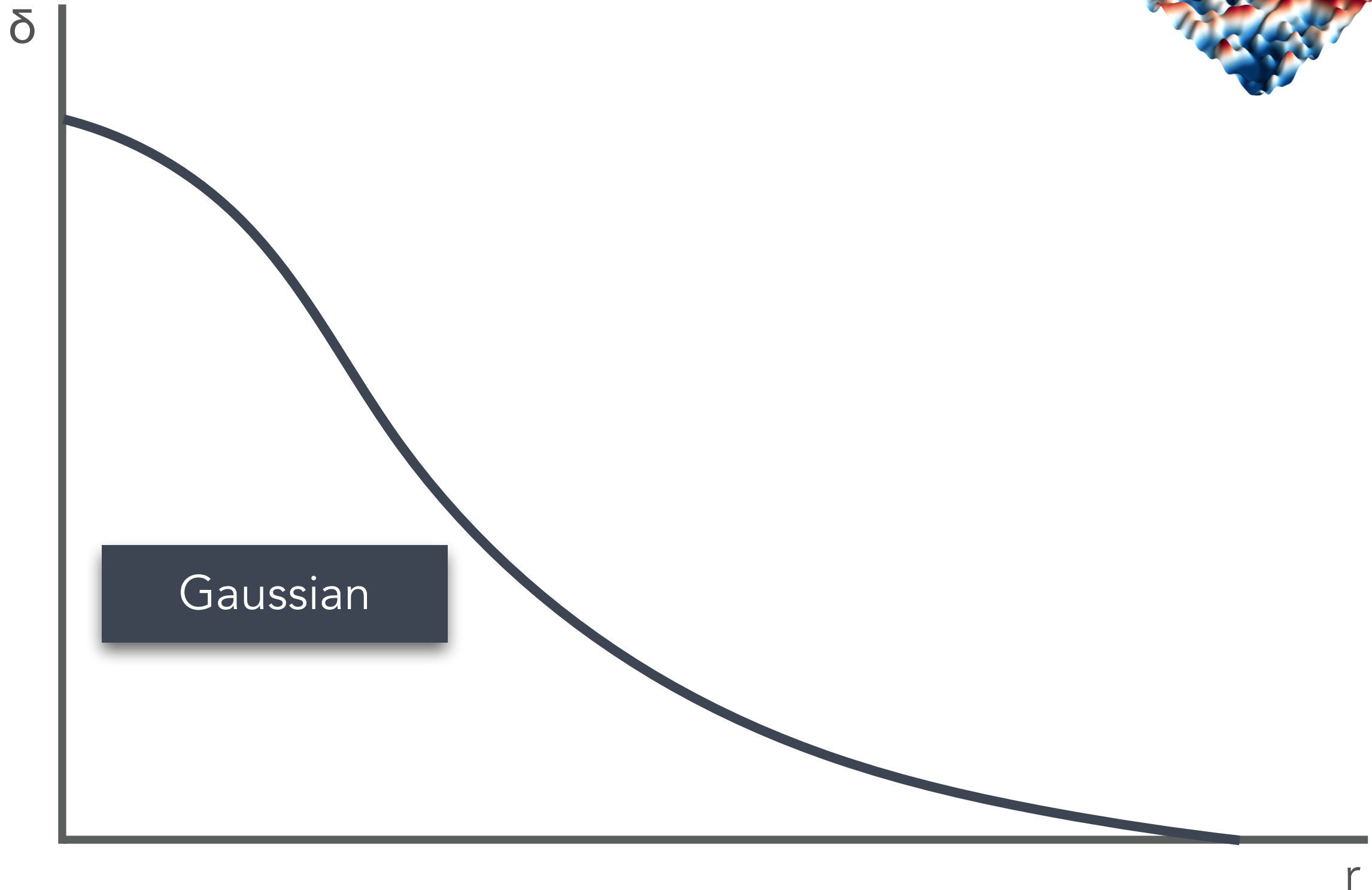
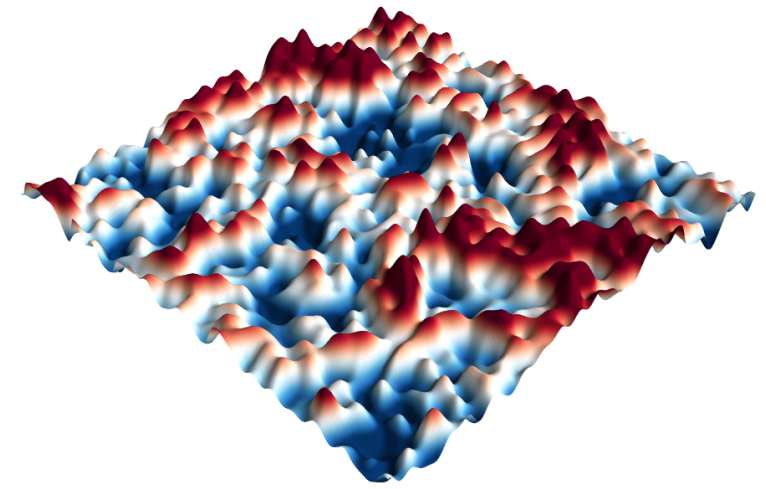




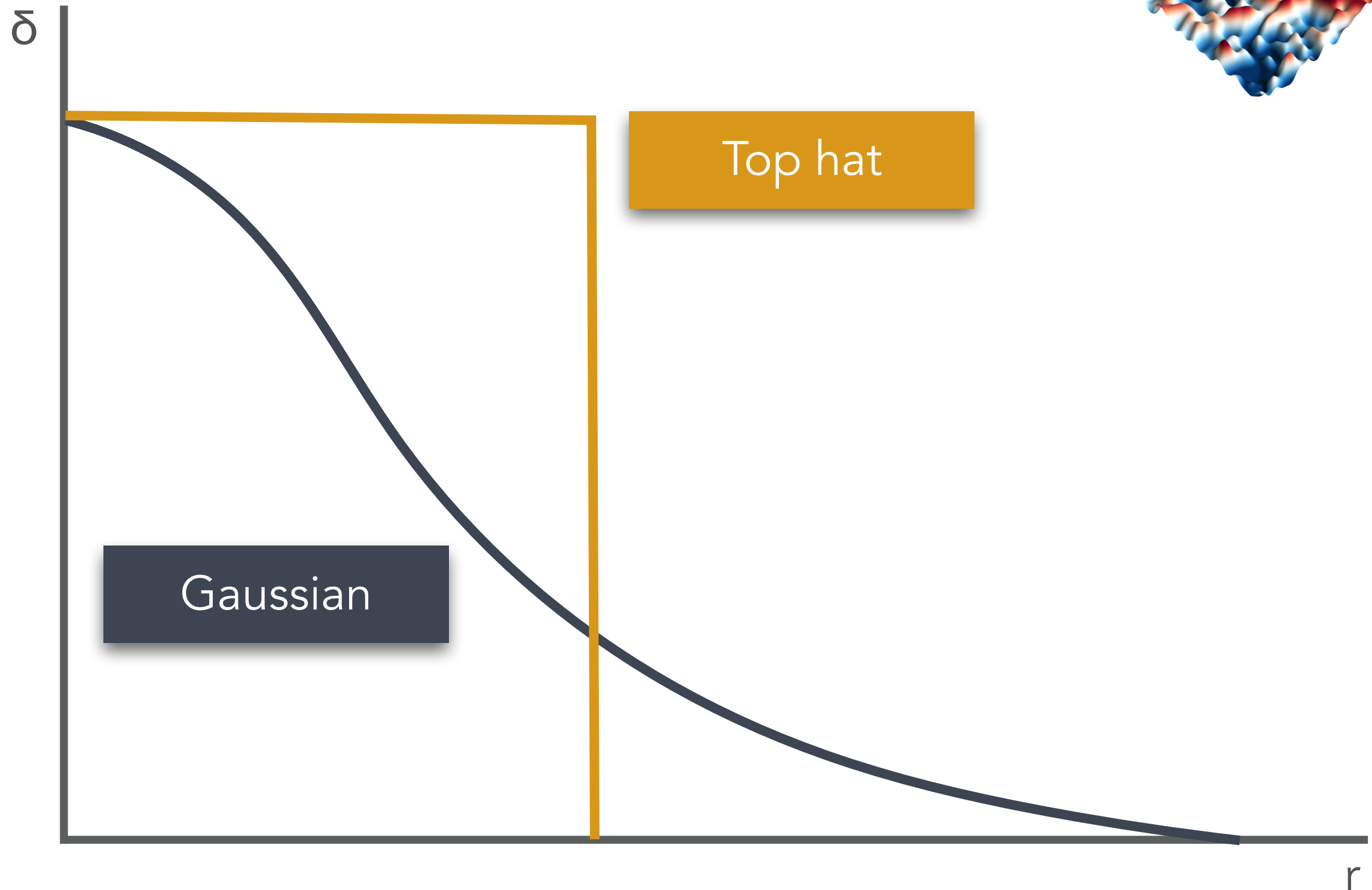
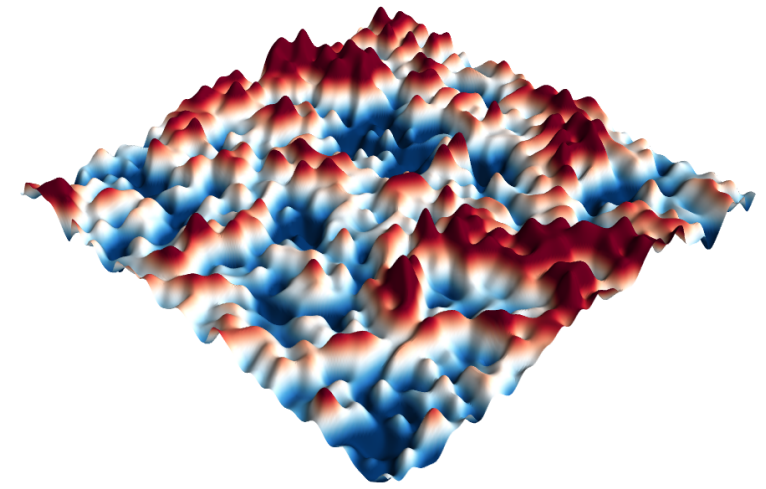
Initial peaks



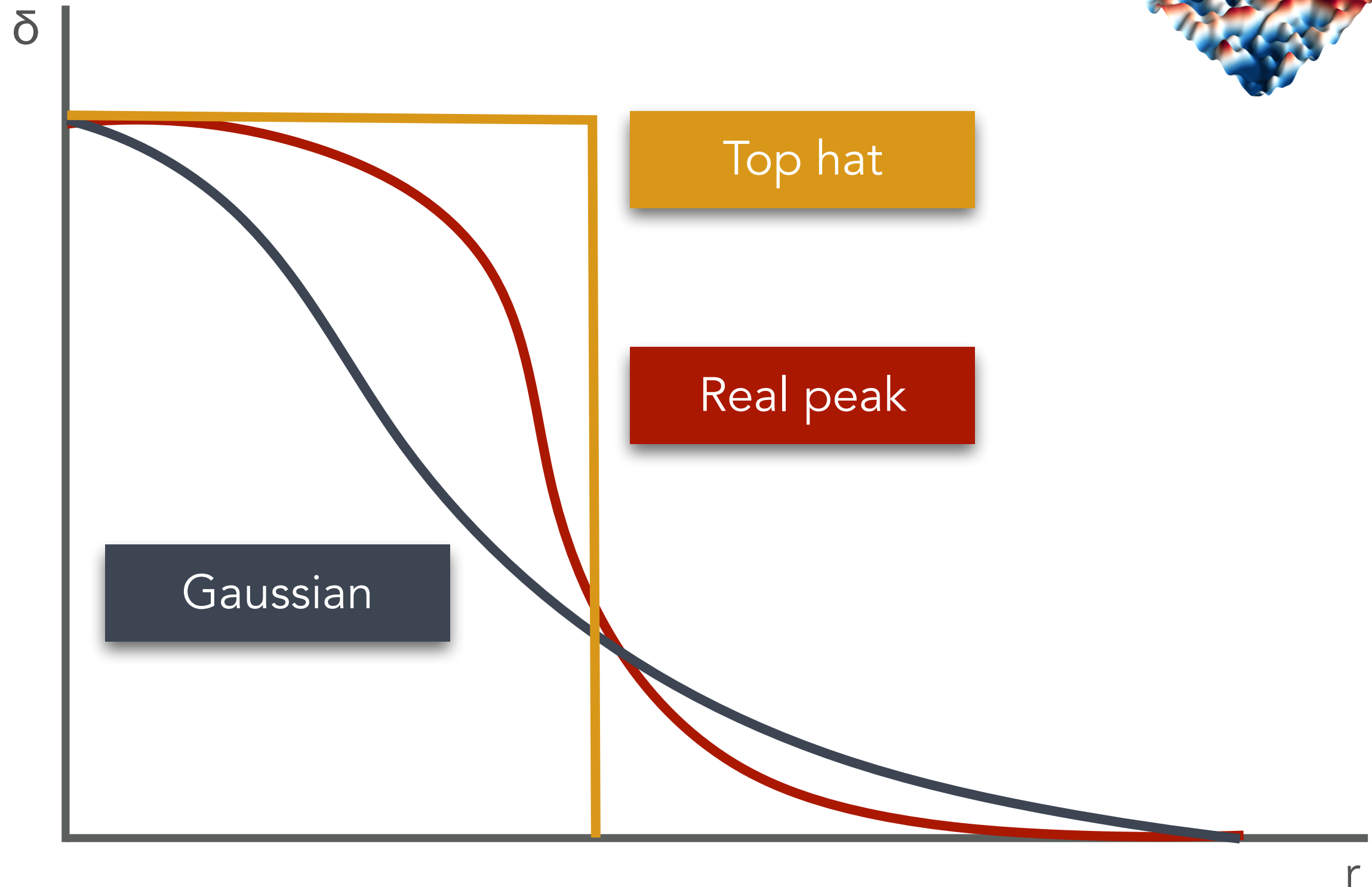
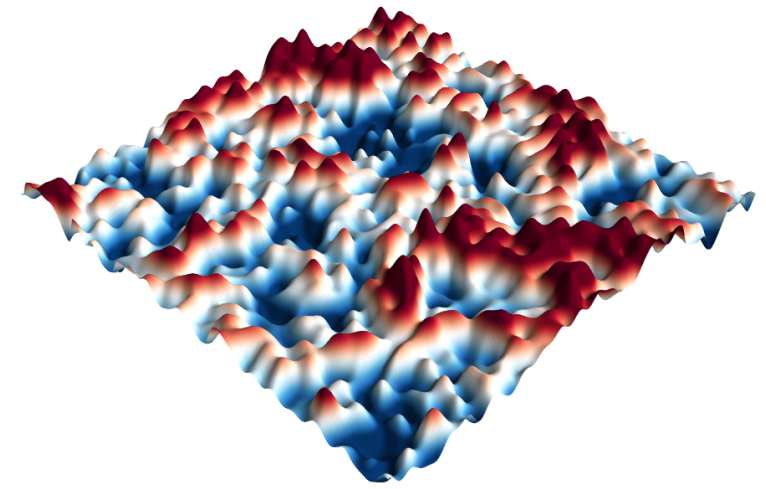
Initial peaks



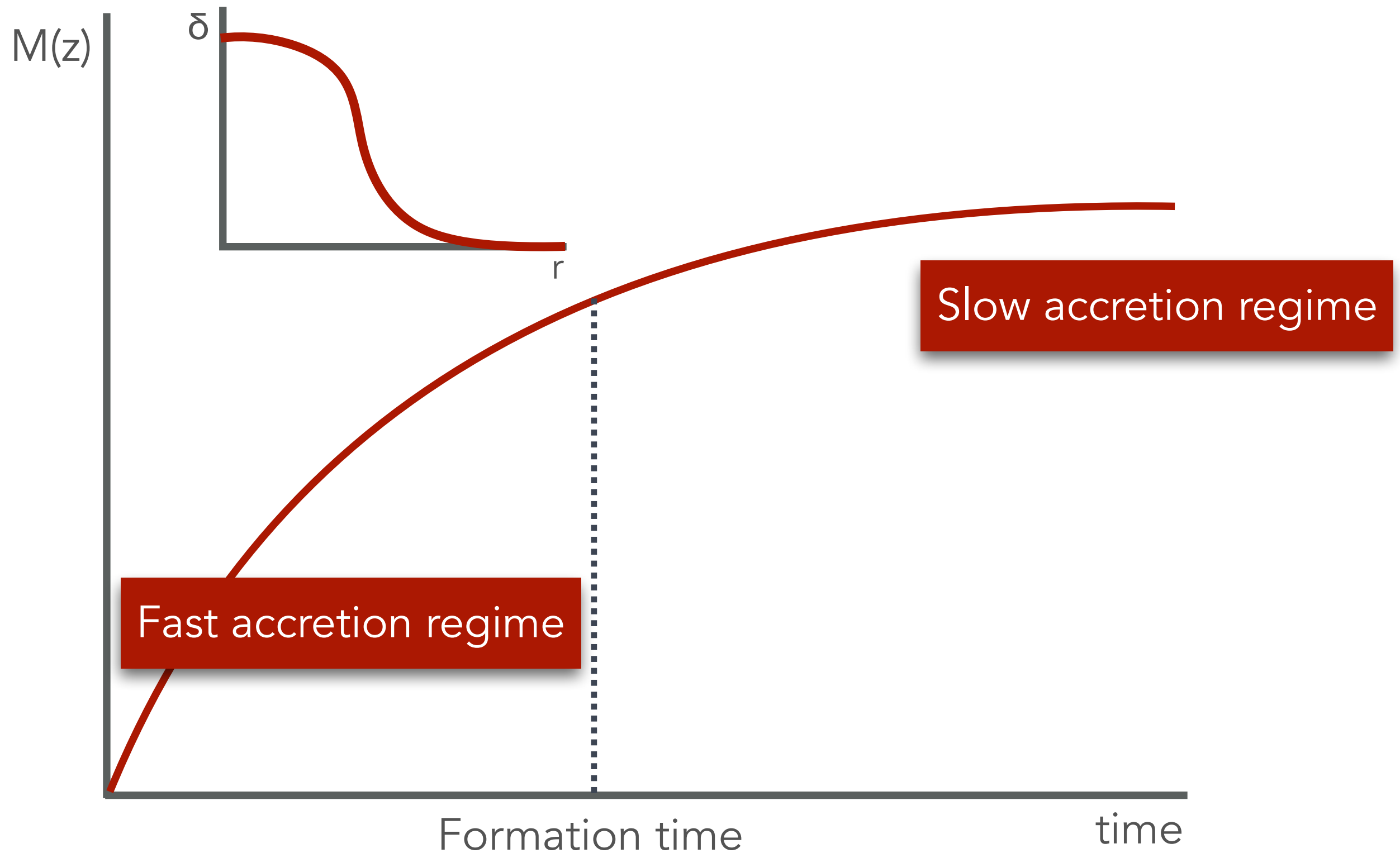
Initial peaks



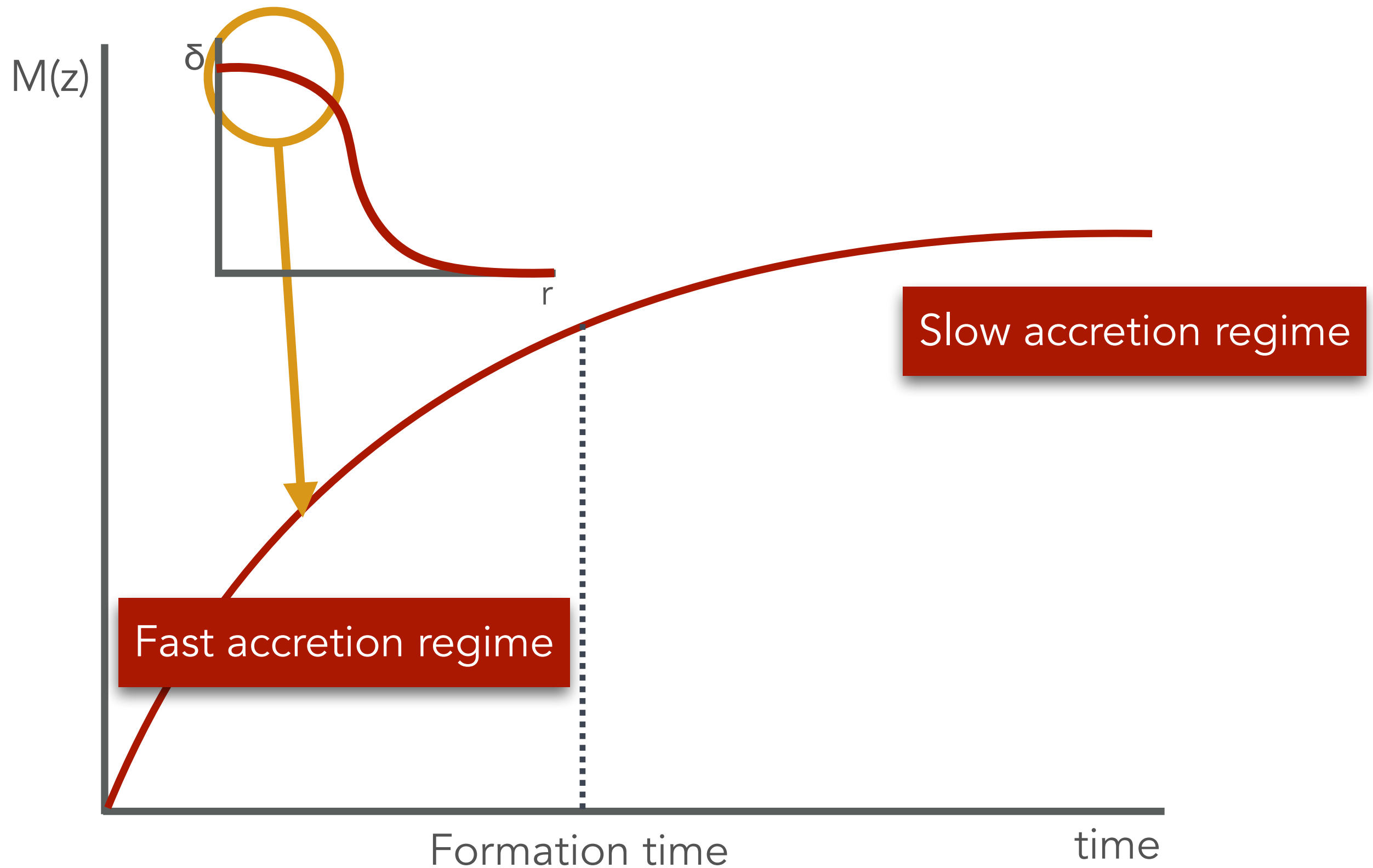
Initial peaks



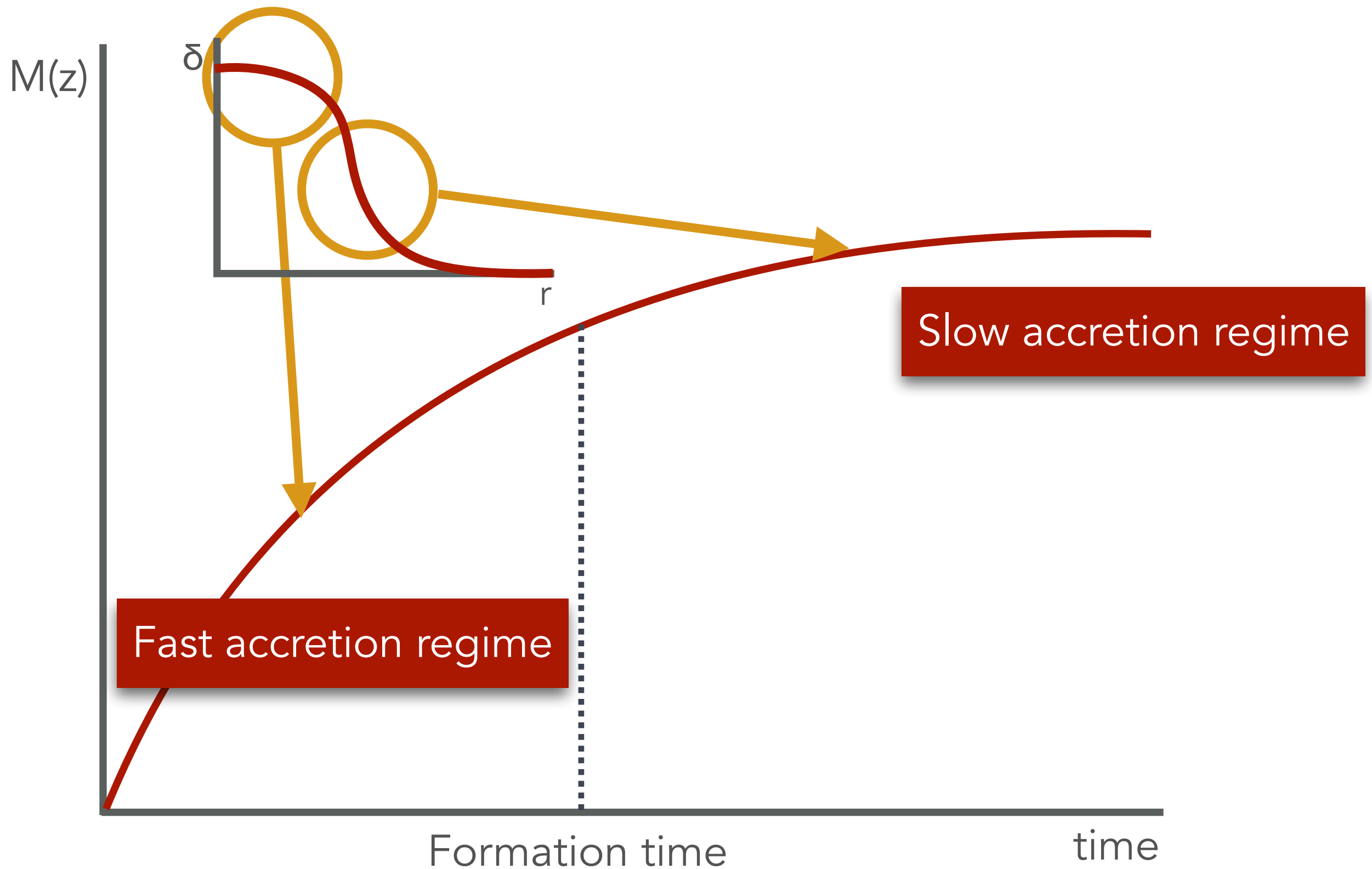
Mass accretion history



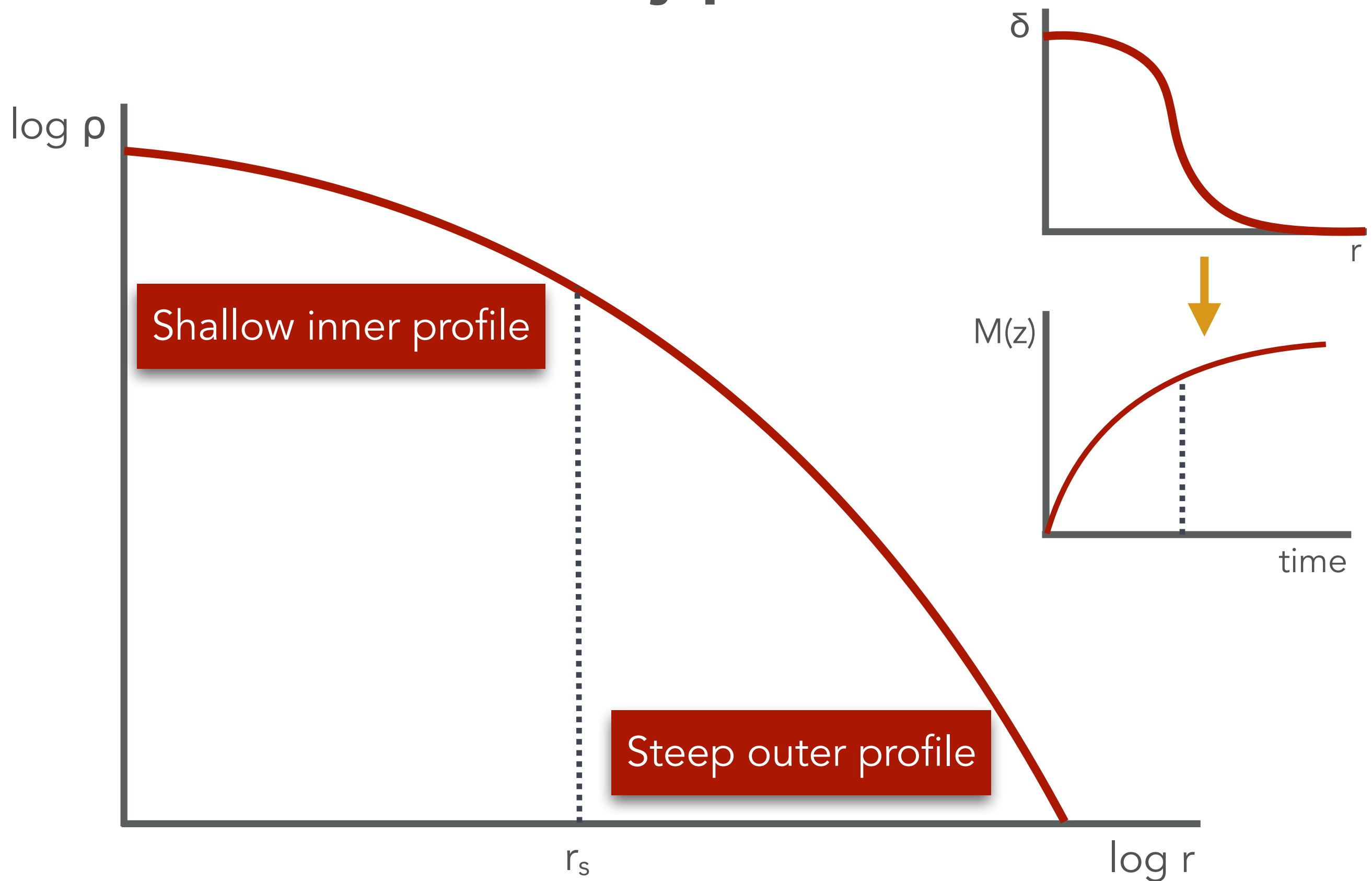
Mass accretion history



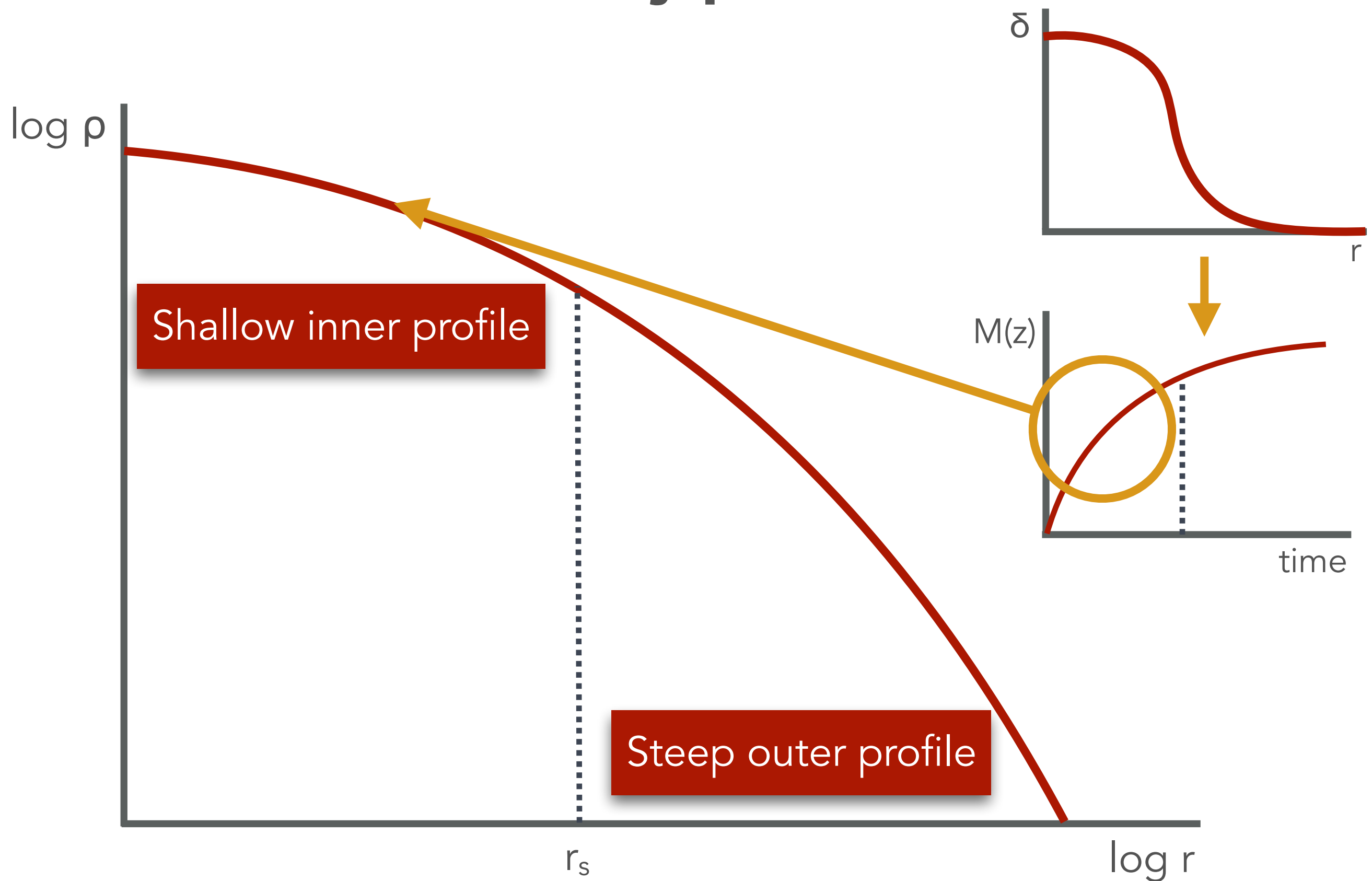
Mass accretion history



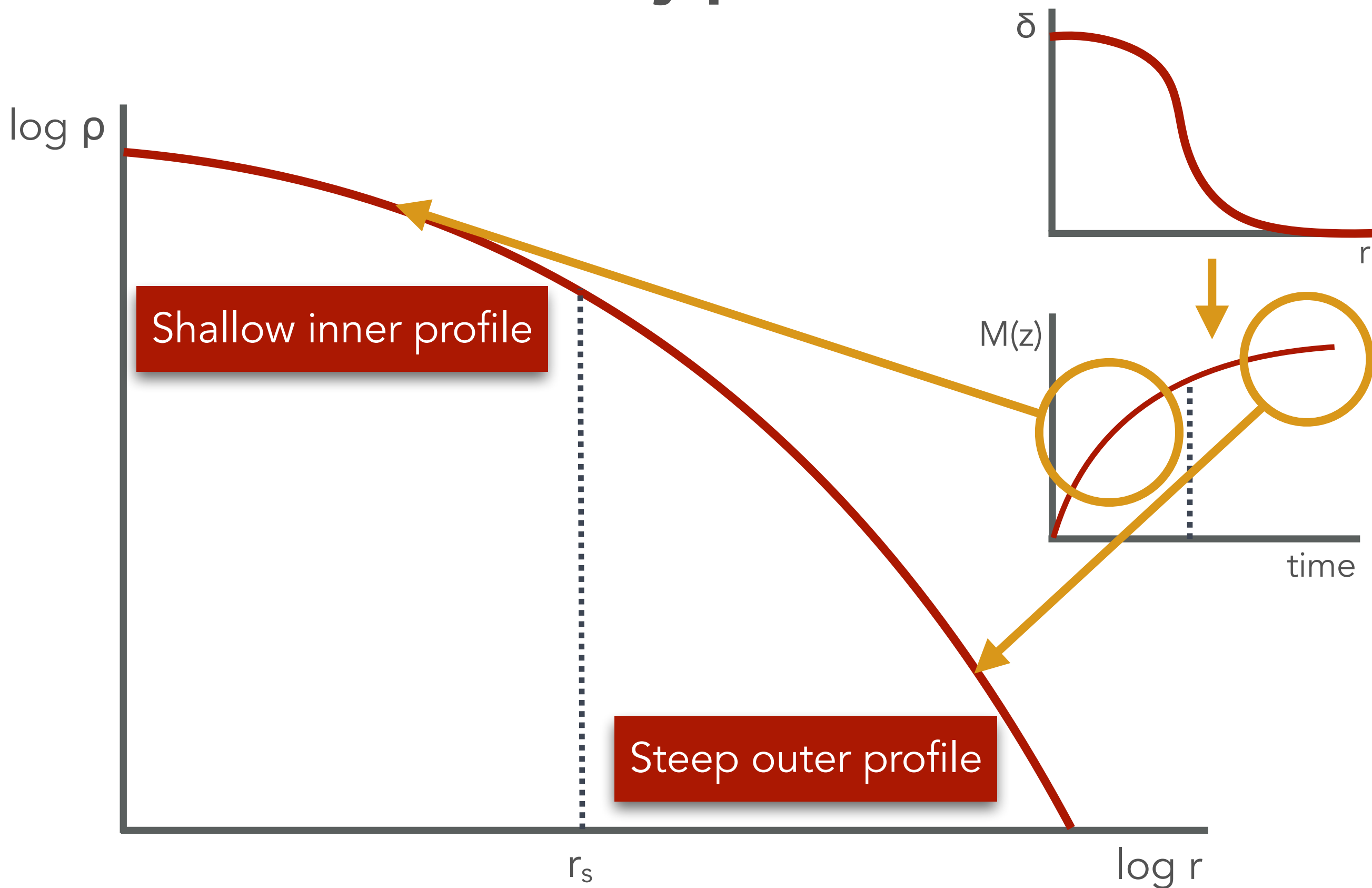
Density profile



Density profile



Density profile



Reading

- CFN §7.3.2, §7.4.3-§7.4.4, §7.5.2
- MvdBW §5.1, §5.4.4, §7.2, §7.5.1