



Please fill in your course evaluation!

3

<u>www.CourseEvalUM.umd.edu-</u> closes Weds evening May 14!

What did we do that you liked-disliked
How can I improve?

+ Help your fellow students and me.

 Identification numbers are not linked to your feedback in the evaluation reporting system





















+N1 includes special case with v = 0, i.e. a body at rest remains at rest if F = 0, as part of a more general law

Newton

13





Newton Law of Gravity and frames of reference

- For Newton all velocities are relative
- To find a velocity in a new frame of reference use the Galilean velocity addition law,
- Distinction between inertial and accelerated frames, real and fictitious forces

+ <u>Newton's law of Gravitation:</u> A particle with mass m_1 will attract another particle with mass m_2 and distance r with a force F given by

$$F = \frac{Gm_1m_2}{r^2}$$

Weak equivalence principle- mass defined from force 5/6/14 and from gravity are the same





Einstein's postulates of Relativity

19

20

Postulate 1 - The laws of nature are the same in all *inertial* frames of reference

 Postulate 2 - The speed of light in a vacuum is the same in all *inertial* frames of reference.

Time dilation- Muon Experiment

- Clock always ticks most rapidly when measured by observer in its own rest frame (proper time)
- Clock slows (ticks take longer) from perspective of other observers

5/6/14

 When clock is moving at V with respect to an observer, ticks are longer by a factor of

$$\Delta t \div \Delta T = \frac{D/c}{\sqrt{1 - V^2/c^2}} \div \frac{D}{c} = -\frac{1}{\sqrt{1 - V^2/c^2}}$$

+ This slowing factor is called the Lorentz factor, γ $\gamma = \frac{1}{\sqrt{1 - v^2/c^2}}$



Relativistic velocity addition law

 Einstein's theory of special relativity was partly motivated by Galilean velocity transformation (simple adding/subtracting frame velocity) gives incorrect results for electromagnetism

• Once we've taken into account the way that time and distances change in Einstein's theory, there is a new law for adding velocities

For a particle measured to have velocity V_p by an observer in a spaceship moving at velocity V_s with respect to Earth, the particle's velocity as measured by observer on Earth is

$$V = \frac{V_p + V_s}{1 + V_p V_s / c^2}$$

Notice that if V_p and V_s are much less than c, the extra term in the denominator <<1 and therefore V ~ V_p+ V_s

 Thus, the Galilean transformation law is approximately correct when the speeds involved are small compared with the speed of light

This is consistent with everyday experience

 Also notice that if the particle has V_p = c in the spaceship frame, then it has V_p=c in the Earth frame. <u>The speed of light is frame-</u> <u>independent!</u>













General Relativity- Curved Space Time

29

• 4-dimensional space-time is "curved," not flat

- Example: surface of sphere is curved 2D space; surface of football field is flat 2D space
- Free-falling objects move on geodesics through curved space-time
- The curvature (bending) of space-time is produced by matter and energy

"Space-time curvature tells matter/energy how to move.

Matter/energy tells space-time how to curve."







Cosmological redshift, z If galaxies move apart, z describes a Doppler shift from the expansion velocity More fundamentally, it comes from the change in metric scaling, R(t) galaxies are carried apart by the expansion of space itself, not by the forces of an explosion! Since it's relativistic, it affects time as well as length Because this is NOT a velocity effect galaxies can move apart from each other faster than

Einstein 5/6/14

How to Use Einstein's GR Equations

the speed of light- this is **not** a violation of

 make the following assumptions

+ Universe is

homogeneous every place in the universe has the same conditions as every other place, on average.

 Universe is isotropic
 there is no preferred direction in the universe, on

5/6**Average**.

Observational evidence for homogenity and isotropy galaxy distribution cosmic microwave background



33



Friedmann Eq

The general form of the solution follows from homogeneity and isotropy

Einstein's field equations are only needed to derive the scale factor of the universe as a function of time (R(t)).

35



Omega in standard models





- Thus, within context of the standard model:
 - + Ω <1 if k=-1; then universe is hyperbolic and will expand forever
 - Ω=1 if k=0; then universe is flat and will (just manage to) expand forever
 - + Ω >1 if k=+1; then universe is spherical and will recollapse
- Physical interpretation:

If there is more than a certain amount of matter in the universe ($\rho > \rho_{critical}$), the attractive nature of gravity will ensure that the Universe recollapses! ₃₇

Curvature of Universe

3 types of general shapes: flat surface at the left :zero curvature, the spherical surface : positive curvature, and the saddle-shaped surface : negative curvature.
Each of these possibilities is tied to the amount of mass (and thus to the total strength of gravitation) in the universe, and each implies a different past and future for the universe.



+ In GR space itself is 'curved'





 All models begin with R→0 at a <u>finite</u> time in the past

- This time is known as the BIG BANG
- Space and time come into existence at this moment... there is no time or space before the big bang!
- The big bang happens everywhere in space... not at a point!

+ Concept of the Hubble time- t_H =1/H gives an estimate of the age of the Universe $1 \Delta R = 1 dR$

+Hubble 'constant'

 $H = \frac{1}{R} \frac{\Delta R}{\Delta t} = \frac{1}{R} \frac{dR}{dt}$

40

There is a connection between the geometry and the dynamics

 Closed solutions for universe expand to maximum size then re-collapse

- +Open solutions for universe expand forever
- +*Flat* solution for universe expands forever (but only just barely...).
- +Definition of the density parameter $\Omega = \rho / \rho_{crit}$

$$\Omega_B = \frac{\rho_B}{\rho_{crit}} = \frac{\rho_B}{3H_0^2/(8\pi G)}$$

41

+With no cosmological constant if $\rho = \rho_{crit}$ (amount of matter in the universe), the Universe is flat









Dark Matter Dominates	s the Universe and the Outer Parts of
 The further out one moves from the center of the galaxy the more 'mass is missing'- lots of mass and no light from stars or indication of gas The material that accounts for the 'extra' velocity is DARK 	Galaxies + Nucleosynthesis arguments constrain the density of baryons (Ω _B ≈0.037) + But there seems to be much more mass in galaxy and cluster halos (Ω~0.1-0.3) + So, most of the matter in the Universe is not baryonic- its dark matter
 Dark matter is a way of expressing our ignorance- the stars and gas do not move like we 'expect' gravitational lensing dynamics of stars and gas confirm the existence of dark matter 5/6/14 	Velocity of stars/gas in galaxy vs radius Rotation speed expected Distance from center















Where did the galaxies come from

 From homogeneity to structure...

- Gravitational evolution of dark matter
- Formation of dark matter halos

Galaxy formation



© Sidney Harris

54

+Denser parts of the universe collapse under their own gravity (dark matter)

- +Normal matter falls into halo, cools, settles to center
- + Once cool dense clouds form, can get star formation
- Through this process, a galaxy is built up 5/6/14





How Things Form

 Gravity acts on overdensities in the early universe making them collapse.

 As time goes on these collapsed regions grow and merge with others to make bigger things



•Hierarchical clustering (or hierarchical merging) is the process by which larger structures are formed through the continuous merging of smaller structures.

•The structures we see in the Universe today (galaxies, clusters, filaments, sheets and voids) are predicted to have formed by the combination of collapse and mergers according to Cold Dark Matter cosmology (the current concordance model).



Here we are

• A consistent picture of the history and future evolution of the Universe

- Supported by observations and experimentation
- Profoundly surprising: most of the Universe is made of something else (dark matter, dark energy) !

 Many open avenues for new observations and theory: this will get even better and more
 5/6/interesting SOON ! 59