Cosmic Web (again)

• The large scale structures are 'seen' in both the all redshift surveys out to the largest redshifts





Large-Scale Structure sample1024

Comparison of dark matter and x-ray cluster and group distribution every bound system visible in the numerical simulation is detected in the x-ray band bright regions are massive clusters, dimmer regions groups,



dark matter simulation

gas simulation

Dark Matter

The existence of dark matter in clusters and groups of galaxies is indicated by

1) high mass-to-light ratio.

estimate the cluster total mass by assuming that the member galaxies have become dynamically relaxed and that they are in an equilibrium configuration-the virial theorem) to obtain the virial mass

2) lensing and x-ray measurements

The observed optical luminosity of the galaxies corresponds to a mass that is much lower than the total cluster mass

- So a large quantity of matter not visible as stars
 - X-ray emitting gas constitutes a portion- $\sim 1/6^{\text{th}}$ of this "missing mass".

In clusters ratio ratio of DM to baryonic matter is ~6:1



How are the Baryons and Dark Matter Partitioned??

- In massive clusters the vast majority of the baryons are in he gas phase (Laganá et al. 2013)
- ~12% of the total mass is in gasindependant of redshift





Bullet Cluster

• Direct evidence (Bullet cluster) that dark matter and baryons can be in different places

Gravitational mass from lensing (blue)

Hot x-ray emitting gas (red) Galaxies – white





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Formation

- Galaxy clusters form through gravitational collapse, driven by dark matter (~80% of their total mass)
- In the hierarchical scenario more massive objects form at later times: clusters of galaxies are produced by the gravitational merger of smaller systems, such as groups and subclusters







R. Wechsler³⁰



X-ray Image of Cluster at z=1.58

- $M_{500}=3.2\times10^{14}M_{\odot}$
- $R_{500} = 560 \text{kpc}$.



Tozzi et al 2015 32



How are they found



What is the "right" survey

• There are many ways to find clusters- we need a uniform approach from which mass can be estimated

So far there are 4 promising techniques

- Large scale x-ray imaging surveys
- Sunyaev-Zeldovich surveys (more later)
- Multi-color deep optical images (Gladders and Yee 2002)
- Lensing surveys

X-ray surveys are a proven technique, luminosity and mass strongly correlated. Works over large mass range to z~1.3. Nongravitational effects may be important at low mass

S-Z surveys working well, PLANCK all sky catalog.Very little redshift bias

Red galaxy survey is surprisingly successful, redshift estimates easy - not clear how complete it can be as a function of mass. Extension to large solid angles takes lots of telescope time

Just starting- so far small number statistics, yield based on detailed studies of x-ray selected clusters not yet clear- direct detection of mass

Finding Clusters

- Clusters are found by
 - optical surveys finding overdensities of galaxies
 - x-ray surveys finding extended x-ray sources
 - S-Z- radio sources
 - 4 *H. Ebeling et al.*



S-Z clusters Bleem et al 2015



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X-ray selected clusters, boxes Rosat image, contours Chandra



Optical Surveys



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Cluster Formation

- Cluster mergers are thought to be the prime mechanism of massive cluster formation in a hierarchical universe (White and Frenk 1991)
- the most energetic events in the universe since the big bang. These mergers with infall velocities of ~2000 km/s and total masses of $10^{15} M_{\odot}$ have a kinetic energy of 10^{65} ergs.
- The shocks and structures generated in the merger have a important influence on cluster shape, luminosity and evolution and may generate large fluxes of relativistic particles

Numerical Simulation of <u>a Merger</u>

• X-ray contours with kT in color, dark matter distribution, velocity vectors and how the two gas components mix (0.3 and 3.5Gyr after closest approach)





Roettiger, Stone and Mushotzky 1998 simulation of a mergertrying to match A754

X-ray Images of Mergers



• A754 (Henry et al 2004) gas pressure and x-ray intensity images





Merger Shocks

Main heating mechanism of intracluster gas

• Most of energy in large clusters due to gravity, conversion of potential energy into heat via merger shocks

> ICM/IGM records thermal history of Universe



Galaxy Cluster Merger

Rubens Machado, Gastão Lima Neto IAG-USP 2012



Binary Galaxy Cluster Merger Simulated using the Flash Code Mass Ratio 1:1, with an Offset Impact

This work was supported in part by the DOE NNSA ASC ASAP and by the NSF. This work also used computational resources at the ALCF at ANL awarded under the INCITE program, which is supported by the DOE Office of Science.



An Advanced Simulation and Computation (ASC) Academic Strategic Alliances Program (ASAP) Center at The University of Chicago

Brightest Cluster Galaxies

- most luminous and most massive galaxies in the Universe at the present epoch.
- At low redshift, these objects exhibit a small dispersion in their luminosities
- lie close to the peaks of the X-ray emission
- Have small relative velocity to cluster average
- Different luminosity profiles than typical cluster elliptical galaxies- show a shallow very large 'envelope'
- Very large number of globular clusters



Figure 1. BCG merger tree. Symbols are colour-coded as a function of B - V colour and their area scales with the stellar mass. Only progenitors more massive than 10¹⁰ Mc, h^{-1} are shown with symbols. Circles are used for galaxies that reside in the FOF group inhabited by the main branch. Triangle shows galaxies that have not yet joined this TOF group.





Cosmology



Mass Function The number of clusters per unit mass

- The number of clusters per unit mass (optical luminosity, x-ray luminosity, velocity dispersion, x-ray temperature)
- Is a strong function of cosmology
- One of the main areas of research is to determine this function over a wide range in redshift.
- One of the main problems is relating observables to mass.





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The Galaxy Cluster Redshift Distribution



Redshift distribution of clusters for 3 sets of cosmological parameters

Notice for for a 'low' Ω universe with no cosmological constant there are many more clusters in the high z universe

Mass Estimation- Girardi et al 1998

In principle, one can estimate the cluster mass within a radius r, $M_J(< r)$, by using the Jeans equation, coupled with the equation which links the two observable quantities $\Sigma(R)$ and $\sigma_P(R)$, i.e. the projected galaxy number density and the projected velocity dispersion as a function of the projected radius R:

$$\frac{d(\rho\sigma_r(r)^2)}{dr} + \frac{2\rho(r)\beta\sigma_r^2}{r} = -\frac{G\rho(r)M_J(< r)}{r^2},\qquad(1)$$

$$\sigma_P^2(R)\Sigma(R) = 2\int_R^\infty \rho(r)\sigma_r^2(r)(1-\beta\frac{R^2}{r^2})\frac{r}{\sqrt{r^2-R^2}}dr \quad (2)$$

where r is the distance from the cluster center, $\rho(r)$ is the spatial number density of galaxies linked to $\Sigma(R)$ via the Abel integral, $\sigma_r(r)$ is the radial component of velocity dispersion $\sigma(r)$, and $\beta(r) = 1 - \sigma_{\theta}^2/\sigma_r^2$ is the velocity anisotropy parameter (e.g., Binney & Tremaine 1987).

Unfortunately, there are three unknowns $(M(\langle r), \sigma(r), \beta(r))$ and only two equations. In order to solve these equations it is therefore necessary to make some assumptions.

The virial theorem derives from the Jeans equation via an integration step. It relates the global kinetic energy with the potential one (2T + U = 0, e.g. Binney and Tremaine 1987) and is usually used to compute virial masses.

Mass Estimation- Girardi et al 1998

3.2 THE MASS DERIVED FROM THE VIRIAL THEOREM

The total virial mass of the cluster, M_V , depends on the global velocity dispersion, σ and the spatial distribution of the galaxy population (e.g., Merritt 1988):

$$M_V = \frac{\langle v^2 \rangle}{G \langle r^{-1}F \rangle},$$
 (3)

where the brackets indicate spatial averages over the observed sample of N galaxies, r are the galaxy distances from the cluster center, and v are the galaxy velocities referred to the cluster mean velocity. The function F(r) is the mass fraction within r and depends on the (generally) unknown form of mass distribution.

If mass is distributed like the observed galaxies (i.e., $\rho_{mass} \propto \rho$), then the appropriate form of eq. 3 is (Limber & Mathews 1960):

$$M_V = \frac{\langle v^2 \rangle}{G \langle r_{ij}^{-1} \rangle} = \sigma^2 R_V / G \tag{4}$$

where R_V is the virial radius which depends on r_{ij} , i.e. the distance between any pair of galaxies.

From the observational point of view, the large advantage of the virial theorem is that the global projected velocity dispersion σ_P and, consequently, the total mass are independent of possible anisotropy of galaxy velocities, always being $\sigma^2 = 3\sigma_P^2$ for spherical systems (e.g., The & White 1986; Merritt 1988). Therefore, in the case of spherical systems, for the respective projected quantities σ_P and R_{PV} , eq. 4 becomes:

$$M_V = 3\pi/2 \cdot \frac{\langle V^2 \rangle}{G \langle R_{ij}^{-1} \rangle} = 3\pi/2 \cdot \sigma_P^2 R_{PV}/G.$$
(5)

X-ray Mass Estimates

• use the equation of hydrostatic equilibirum

•

$$\frac{dP_{\text{gas}}}{dr} = \frac{-G\mathfrak{M}_{*}(r)\rho_{\text{gas}}}{r^{2}}$$
(3)

where P_{gas} is the gas pressure, ρ_{gas} is the density, G is the gravitational constant, and $\mathfrak{M}_{\bullet}(r)$ is the mass of M87 interior to the radius r.

$$P_{\rm gas} = \frac{\rho_{\rm gas} K T_{\rm gas}}{\mu \mathfrak{M}_{\rm H}} \tag{4}$$

where μ is the mean molecular weight (taken to be 0.6), and \mathfrak{M}_{H} is the mass of hydrogen atom.

$$\frac{KT_{\text{gas}}}{\mu\mathfrak{M}_{\text{H}}}\left(\frac{d\rho_{\text{gas}}}{\rho_{\text{gas}}} + \frac{dT_{\text{gas}}}{T_{\text{gas}}}\right) = \frac{-G\mathfrak{M}_{\bullet}(r)}{r^2}dr, \qquad (5)$$

which may be rewritten as:

$$-\frac{KT_{gas}}{G\mu\mathfrak{M}_{\rm H}}\left(\frac{d\log\rho_{gas}}{d\log r}+\frac{d\log T_{gas}}{d\log r}\right)r=\mathfrak{M}_{\bullet}(r) \quad (6)$$

Putting numbers in gives

$$M(r) = -3.71 \times 10^{13} M_{\odot} T(r) r \left(\frac{d \log \rho_{\beta}}{d \log r} + \frac{d \log T}{d \log r}\right)$$

ere T is in units of keV and r is in units of Mnc. (



Intracluster Gas

- Majority (75%) of observable cluster mass (majority of baryons) is hot gas
- Temperature $T\sim 10^{7_8}~K\sim 1\text{--}10~keV$
- Electron number density $n_e \sim 10^{-3} \text{ cm}^{-3}$
- Mainly H, He, but with heavy elements (O, Fe, ..)
- Mainly emits X-rays
- $L_X \sim 10^{45}$ erg/s, most luminous extended X-ray sources in Universe
- Age \sim 2-10 Gyr

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The Intracluster Medium as a Fluid

$$\lambda_{p} \approx \lambda_{e} = \frac{3^{3/2} (kT)^{2}}{8\sqrt{\pi} n_{e} e^{4} \ln \Lambda} \qquad \text{mean free path of a particle}$$
$$\approx 23 \left(\frac{T}{10^{8} \text{ K}}\right)^{2} \left(\frac{n_{e}}{10^{-3} \text{ cm}^{-3}}\right)^{-1} \text{ kpc}$$

galaxies, or at shocks and cold fronts)

Sarazin

Physical State of Intracluster Gas: Local Thermal State

- Mainly ionized, but not completely
- Coulomb collision time scales

 $\begin{aligned} \tau(e,e) &\sim 10^5 \text{ yr} \\ \tau(p,p) &\sim 4 \text{ x } 10^6 \text{ yr} \\ \tau(p,e) &\sim 2 \text{ x } 10^8 \text{ yr} \\ \text{all } < \text{age } (>10^9 \text{ yr}) \\ \text{Kinetic equilibrium, Maxwellian at T} \\ \text{Equipartition } T_e = T_p \\ (\text{except possibly at shocks}) \end{aligned}$

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X-ray Emission Processes

- Continuum emission
 - Thermal bremsstrahlung, ~exp(-hv/kT)
 - Bound-free (recombination)
 - Two Photon
- Line Emission

(line emission)

 $\square \hspace{-0.1cm} \square \hspace{-0.1cm} \searrow \hspace{-0.1cm} L_{\nu} \hspace{0.1cm} \backsim \hspace{-0.1cm} \underset{\nu}{ \hspace{-0.1cm} \leftarrow} \hspace{-0.1cm} (T, abund) \hspace{0.1cm} (n_e^2 \hspace{0.1cm} V)$



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Chemical Abundances

Hitomi has the possibility to produce extremely precise chemical abundances which allow constraints on the ratio of double degenerate to single degenerate SNIa models





Heating and Cooling of ICM

- What determines temperature T?
- Why is ICM so hot?
- What are heating processes?
 - gravitational heating
 - nongravitational heating (SNe, AGNs)
- What are cooling processes?

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Why is gas so hot?

- Clusters have huge masses, very deep gravitational potential wells
- Any natural way of introducing gas causes it to move rapidly and undergo fast shocks



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Simple Scaling Laws for Gravitational Heating (Kaiser 1986)

- Gas hydrostatic in gravitational potential $kT \sim \mu m_p GM/R$
- Clusters formed by gravitational collapse $\langle \rho_{cluster} \rangle \sim 180 \ \rho_{crit} \ (z_{form})$
- Most clusters formed recently, $z_{form} \sim now$
- Baryon fraction is cosmological value, most baryons in gas

$$\begin{split} & R \varpropto (M \ / \ \rho_{crit0})^{1/3} \varpropto M^{1/3} \\ & T \varpropto M^{2/3} \\ & L_X \varpropto T^2 \end{split}$$

Radiative Cooling of ICM

• Main cooling mechanism is radiation, mainly X-rays

 $L = \Lambda$ (T,abund) n_e^2 ergs/cm³/s

 $T \gtrsim 2 \text{ kev}, \Lambda \propto T^{1/2}$ Thermal bremsstrahlung $T \lesssim 2 \text{ keV}, \Lambda \propto T^{-0.4}$ X-ray lines





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Sound Crossing Time

• Sound speed

$$c_s^2 = \gamma \frac{P}{\rho} = \frac{5}{3} \frac{P}{\rho}$$
$$c_s \approx 1500 \left(\frac{T}{10^8 \text{ K}}\right)^{1/2} \text{ km/s}$$

• Sound crossing time

$$t_s \approx 6.6 \times 10^8 \left(\frac{T}{10^8 \,\mathrm{K}}\right)^{-1/2} \left(\frac{D}{\mathrm{Mpc}}\right) \mathrm{yr}$$

Less than age \rightarrow unless something happens (merger, AGN, ...) gas should be nearly hydrostatic

• Sarazin





Sunyaev-Zel'dovich Effect

Single Clusters

- Measure of integrated pressure (total thermal energy)
- Distances, H_o, H(z)
- Cluster gas mass fractions, cluster structure, evolution studies
- Peculiar velocities at high z

SZ Cluster Surveys

- Exploit SZ redshift independence
- Measure growth of structure and large scale velocity fields to constrain Dark Energy

 $\frac{\Delta T_{SZE}}{T_{CMB}} \propto \int n_e T_e dl$

$$S \propto \int \Delta T_{SZE} d\Omega$$

 $\propto \frac{1}{D_A(z)^2} \int n_e T_e dV$

Carlstrom

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S-Z Simple Physics

- The optical depth for the S-Z effect is small
- the density of electrons is of order $n_e \sim 10^{-3}$ cm⁻³, the path length ` through a cluster medium ~ several Mpc. With a Thomson cross section σ = 6.65 x10 ⁻²⁵ cm²,

optical depth $\tau = n_e \sigma l \sim 0.005; ~ \sim 1\%$

- probability that a CMB photon crossing a rich cluster is scattered by an electron.
- Since the electron energy is much larger that the energy of the photon, to first order $\delta v/v \sim kTe/m_ec^2 = 1\%$. The resulting fractional temperature change of the CMB is of the order of 10^{-4} ,~ $300\mu k$
- For a review see *Carnegie Observatories Astrophysics Series, Vol. 3: Clusters of Galaxies: Probes of Cosmological Structure and Galaxy Evolution, 2004* Using the Sunyaev-Zelídovich Effectto Probe the Gas in Clusters MARK BIRKINSHAW

The spectrum of the thermal SZE has a characteristic shape all interacting CMB photons get approximately a 1% boost in energy, the result is a transfer of photons in the CMB spectrum from lower to higher frequencies, resulting in a decrease of brightness at low frequencies



A Strange Fact

- As clusters are observed at higher redshifts the solid angle which scatters the CMB gets smaller- however the CMB gets brighter in the past
- These two terms almost cancel IF the cluster hot gas were the same at higher redshifts.
- Since we expect the cluster hot gas to evolve with z it is not clear what the total effect will be .
- The amplitude of the S-Z effect is t independent of D_A the angular distance



Fig.1. Map of Abell 2163 at 150 GHz, overlaid with XMM-Newton X-ray contours (see Fig. 3) in units of 10^{-13} erg s⁻¹cm⁻²arcmin⁻². Because the correlated-noise re-

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Sunyaev-Zeldovich Distances

- The Sunyaev-Zeldovich effect is the Compton scattering of microwave background photons off the hot electrons in the IGM in the cluster
- At present ~400 clusters have measured S-Z effect "decrements" and x-ray temperatures (Primarily from Planck and the South Pole Telescope and the Atacama Cosmology telescope)

Angular distance $D_A:\Delta T_0$ is the S-Z decrement, S_{X0} the x-ray surface brightness, T_{e0} the x-ray temperature, θ an angular size and Λ the cooling function



All quantities are directly measurable with an x-ray image, temperature map and S-Z image

Sunyaev-Zeldovich effect

- Compton scattering changes both the angular and energy distribution of the microwave background
- At low frequencies the result is a diminution (decrement) in the surface brightness of the MWB whose amplitude and shape depends on the Compton optical depth, the 3-D distribution of the hot electrons and their temperature



Fig. 1.— The spectrum of the microwave background radiation, and the microwave background radiation after passage through an (exaggerated) scattering atmosphere with y = 0.1 and $\tau \beta = 0.05$ (as defined in Section 3 and 6), compared with the integrated



[—] The scattering geometry, in the frame of rest of the electron before the interaction. ming photon, at angle θ relative to the $x_{\rm e}$ axis, is deflected by angle ϕ_{12} and emerges

Sunyaev-Zeldovich effect

- The main technical limits are the long exposures required in both the x-ray band and the milli-meter (~1 day each for the highest z clusters)
- The S-Z decrement is independent of redshift, while the x-ray surface brightness drops as $(1+z)^4$

Setting a practical limit to z~1.3 for the x-ray measurements

• In a massive cluster the typical optical depth is $\tau \sim 0.1$



X-ray image with S-Z contours for z=0.54 cluster



S-Z contours images for a sample of clusters from $z\sim0.3-0.9$ 7

Clusters of Galaxies

Probes of the history of structure formation

Dynamical timescales are not much shorter than the age of the universe

• Studies of their evolution, temperature and luminosity function can place strong constraints on all theories of large scale structure

• and determine precise values for many of the cosmological parameters

Provide a record of nucleosynthesis in the universe- as opposed to galaxies, clusters probably retain all the enriched material created in them

•Measurement of the elemental abundances and their evolution provide fundamental data for the origin of the elements

•The distribution of the elements in the clusters reveals how the metals were removed from stellar systems into the IGM

Clusters should be "fair" samples of the universe"

•Studies of their mass and their baryon fraction reveal the "gross" properties of the universe as a whole

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