How Old are the Galaxies

- One of the major issues is when did clusters form and what does that mean?
- CDM simulations indicate when the dark matter mass concentrations formed- but how were they populated with galaxies and gas?
- The oldest average age for a stellar population is found in the most massive galaxies in clusters



ario proposed by Thomas et al. (2005) for the average star formation lifferent masses, from $5\times 10^9 M_{\odot}$ up to $10^{12} M_{\odot}$, corresponding to r the highest and lowest environmental densities, respectively, in the

Cosmic Web

• large scale structure of the universe consists of sheets and filamentsclusters occur at the intersection of these structures



Cosmic Web (again)

• The large scale structures are 'seen' in both the all redshift surveys out to the largest redshifts





Blanton et al. (2003) (astro-ph/0210215)

Large-Scale Structure sample10 $_{23}$

Comparison of dark matter and x-ray cluster and group distribution every bound system visible in the numerical simulation is detected in the x-ray band bright regions are massive clusters, dimmer regions groups,



dark matter simulation

gas simulation

Dark Matter

The existence of dark matter in clusters and groups of galaxies is indicated by

1) high mass-to-light ratio.

estimate the cluster total mass by assuming that the member galaxies have become dynamically relaxed and that they are in an equilibrium configuration-the virial theorem) to obtain the virial mass

2) lensing and x-ray measurements

The observed optical luminosity of the galaxies corresponds to a mass that is much lower than the total cluster mass

- So a large quantity of matter not visible as stars
 - X-ray emitting gas constitutes a portion- ~1/6th of this "missing mass".

In clusters ratio ratio of DM to baryonic matter is ~6:1



How are the Baryons and Dark Matter Partitioned??

- In massive clusters the vast majority of the baryons are in the gas phase (Laganá et al. 2013)
- ~12% of the total mass is in gas (f_{gas})independant of redshift





How Do We Know This

- X-ray images give the flux and surface brightness of the x-rays
- The xray flux is due to thermal bremmstrahlung whose emissivity is related to the density squared and the square root of the temperature
 The total flux is the emissivity x volume
- X-ray luminosity ~10⁴³-10^{45.5} erg/sec, average density ~10⁻³ with $n \sim r^{-2}$

$$\epsilon_{\nu} = \mathbf{C} \qquad \qquad \underline{T^{-1/2}} Z^2 n_e n_i \exp[-h\nu/(k_B T)] \bar{g}_{ff}(\nu)$$

T= temperature, n_e is electron density , n_i is the ion density $(n_e \sim n_i)$ g_{ff} is a function from quantum mechanics (Gaunt function), Z is the atomic number

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Bullet Cluster

• Direct evidence (Bullet cluster) that dark matter and baryons can be in different places

Gravitational mass from lensing (blue) Hot x-ray emitting gas (red) Galaxies – white (Bullet shape is due to a Mach cone)





Formation

- Galaxy clusters form through gravitational collapse, driven by dark matter (~80% of their total mass)
- In the hierarchical scenario more massive objects form at later times: clusters of galaxies are produced by the gravitational merger of smaller systems, such as groups and subclusters





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What is a Merger Tree

- In LCDM cosmology structure grows by the merging of bound systems + infall
- The fraction of contribution of each component depends on time and mass.



n



X-ray Image of Cluster at z=1.58

- $M_{500} = 3.2 \times 10^{14} M_{\odot}$
- R₅₀₀=560kpc
 - 500 subscript is the location where the density is 500x the average of the universe at the relevant epoch





What is the "right" survey

• There are many ways to find clusters- we need a uniform approach from which mass can be estimated

So far there are 4 promising techniques

- Large scale x-ray imaging surveys
- Sunyaev-Zeldovich surveys (more later)
- Multi-color deep optical images (Gladders and Yee 2002)
- Lensing surveys

X-ray surveys are a proven technique, luminosity and mass strongly correlated. Works over large mass range to z~1.3. Nongravitational effects may be important at low mass

S-Z surveys working well, PLANCK all sky catalog.Very little redshift bias

Red galaxy survey is surprisingly successful, redshift estimates easy - not clear how complete it can be as a function of mass. Extension to large solid angles takes lots of telescope time

Just starting- so far small number statistics, yield based on detailed studies of x-ray selected clusters not yet clear- direct detection of mass

Finding Clusters

- Clusters are found by
 - optical surveys finding overdensities of galaxies
 - x-ray surveys finding extended x-ray sources
 - S-Z- radio sources
 - 4 *H. Ebeling et al.*



S-Z clusters Bleem et al 2015



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X-ray selected clusters, boxes Rosat image, contours Chandra

How are they found



X-ray data

- Clusters have a narrow range of x-ray spectra compared to AGN and Stars (Bohringer et al 2017)
- Lots of clusters to be found eRosita launch 2019





X-ray Detection -eRosita

~8.25 ster.

- 100,000 clusters *eROSITA* Cluster Redshift Distribution
 total
- most clusters around
- z~0.3, M_{500} ~10¹⁴ M_{\odot}



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Optical Surveys



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Abell2219

• Ground, HST





Cluster Formation

- Cluster mergers are thought to be the prime mechanism of massive cluster formation in a hierarchical universe (White and Frenk 1991)
- the most energetic events in the universe since the big bang. These mergers with infall velocities of ~2000 km/s and total masses of $10^{15} M_{\odot}$ have a kinetic energy of 10^{65} ergs.
- The shocks and structures generated in the merger have a important influence on cluster shape, luminosity and evolution and may generate large fluxes of relativistic particles

Cluster Mergers

Clusters from hierarchically, smaller things form first, gravity pulls them together



Abell 85 Chandra

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Numerical Simulation of <u>a Merger</u>

• X-ray contours with kT in color, dark matter distribution, velocity vectors and how the two gas components mix (0.3 and 3.5Gyr after closest approach)





Roettiger, Stone and Mushotzky 1998 simulation of a mergertrying to match A754

X-ray Images of Mergers



• A754 (Henry et al 2004) gas pressure and x-ray intensity images



Merger Shocks

→ Main heating mechanism of intracluster gas

 Most of energy in large clusters due to gravity, conversion of potential energy into heat via merger shocks

> ICM/IGM records thermal history of Universe



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The Center for Astrophysical Thermonuclear Flashes

Binary Galaxy Cluster Merger Simulated using the Flash Code Mass Ratio 1:1, with an Offset Impact

This work was supported in part by the DOE NNSA ASC ASAP and by the NSF. This work also used computational resources at the ALCF at ANL awarded under the INCITE program, which is supported by the DOE Office of Science.



An Advanced Simulation and Computation (ASC) Academic Strategic Alliances Program (ASAP) Center at The University of Chicago



Galaxy Cluster Merger

Rubens Machado, Gastão Lima Neto IAG-USP 2012

Brightest Cluster Galaxies

- most luminous and most massive galaxies in the Universe at the present epoch.
- At low redshift, these objects exhibit a small dispersion in their luminosities
- lie close to the peaks of the X-ray emission
- Have small relative velocity to cluster average
- Different luminosity profiles than typical cluster elliptical galaxies- show a shallow very large 'envelope'
- Very large number of globular clusters



Figure 1. BCG merger tree. Symbols are colour-coded as a function of B - V colour and their area scales with the stellar mass. Only progenitors more massive than 10^{10} Mo h^{-1} are aboven with symbols. Grads are used for galaxies that reside in the FOF group inhabited by the main branch. Triangles above galaxies that have not yet joind this FOF group.

HST Image of M87 Globular Clusters



Cosmology



Mass Function

- The number of clusters per unit mass (optical luminosity, x-ray luminosity, velocity dispersion, x-ray temperature)
- Is a strong function of cosmology
- One of the main areas of research is to determine this function over a wide range in redshift.
- One of the main problems is relating observables to mass.



Frg. 18.— Same as Fig. 16 but the high-z sample is split into three redshift bins.





The Galaxy Cluster Redshift Distribution



Redshift distribution of clusters for 3 sets of cosmological parameters

Notice for for a 'low' Ω universe with no cosmological constant there are many more clusters in the high z universe

Mass Estimation-Girardi et al 1998

In principle, one can estimate the cluster mass within a radius r, $M_J(< r)$, by using the Jeans equation, coupled with the equation which links the two observable quantities $\Sigma(R)$ and $\sigma_P(R)$, i.e. the projected galaxy number density and the projected velocity dispersion as a function of the projected radius R:

$$\frac{d(\rho\sigma_r(r)^2)}{dr} + \frac{2\rho(r)\beta\sigma_r^2}{r} = -\frac{G\rho(r)M_J(< r)}{r^2}, \quad (1)$$

$$\sigma_P^2(R)\Sigma(R) = 2\int_R^\infty \rho(r)\sigma_r^2(r)(1-\beta\frac{R^2}{r^2})\frac{r}{\sqrt{r^2-R^2}}dr \quad (2)$$

where r is the distance from the cluster center, $\rho(r)$ is the spatial number density of galaxies linked to $\Sigma(R)$ via the Abel integral, $\sigma_r(r)$ is the radial component of velocity dispersion $\sigma(r)$, and $\beta(r) = 1 - \sigma_{\theta}^2/\sigma_r^2$ is the velocity anisotropy parameter (e.g., Binney & Tremaine 1987).

Unfortunately, there are three unknowns $(M(\langle r), \sigma(r), \beta(r))$ and only two equations. In order to solve these equations it is therefore necessary to make some assumptions.

The virial theorem derives from the Jeans equation via an integration step. It relates the global kinetic energy with the potential one (2T + U = 0, e.g. Binney and Tremaine 1987) and is usually used to compute virial masses.

Mass Estimation- Girardi et al 1998

3.2 THE MASS DERIVED FROM THE VIRIAL THEOREM

The total virial mass of the cluster, M_V , depends on the global velocity dispersion, σ and the spatial distribution of the galaxy population (e.g., Merritt 1988):

$$M_V = \frac{\langle v^2 \rangle}{G \langle r^{-1}F \rangle},$$
 (3)

where the brackets indicate spatial averages over the observed sample of N galaxies, r are the galaxy distances from the cluster center, and v are the galaxy velocities referred to the cluster mean velocity. The function F(r) is the mass fraction within r and depends on the (generally) unknown form of mass distribution.

If mass is distributed like the observed galaxies (i.e., $\rho_{mass} \propto \rho$), then the appropriate form of eq. 3 is (Limber & Mathews 1960):

$$M_V = \frac{\langle v^2 \rangle}{G \langle r_{ii}^{-1} \rangle} = \sigma^2 R_V / G \tag{4}$$

where R_V is the virial radius which depends on r_{ij} , i.e. the distance between any pair of galaxies.

From the observational point of view, the large advantage of the virial theorem is that the global projected velocity dispersion σ_P and, consequently, the total mass are independent of possible anisotropy of galaxy velocities, always being $\sigma^2 = 3\sigma_P^2$ for spherical systems (e.g., The & White 1986; Merritt 1988). Therefore, in the case of spherical systems, for the respective projected quantities σ_P and R_{PV} , eq. 4 becomes:

$$M_V = 3\pi/2 \cdot \frac{\langle V^2 \rangle}{G \langle R_{ij}^{-1} \rangle} = 3\pi/2 \cdot \sigma_P^2 R_{PV}/G.$$
(5)

X-ray Mass Estimates

- use the equation of hydrostatic equilibrium
- •

$$\frac{dP_{\text{gas}}}{dr} = \frac{-G\mathfrak{M}_{\bullet}(r)\rho_{\text{gas}}}{r^2}$$
(3)

where P_{gas} is the gas pressure, ρ_{gas} is the density, G is the gravitational constant, and $\mathfrak{M}_{\bullet}(r)$ is the mass of M87 interior to the radius r.

$$P_{\rm gas} = \frac{\rho_{\rm gas} K T_{\rm gas}}{\mu \mathfrak{M}_{\rm H}} \tag{4}$$

where μ is the mean molecular weight (taken to be 0.6), and \mathfrak{M}_{H} is the mass of hydrogen atom.

$$\frac{KT_{gas}}{\mu\mathfrak{M}_{H}}\left(\frac{d\rho_{gas}}{\rho_{gas}} + \frac{dT_{gas}}{T_{gas}}\right) = \frac{-G\mathfrak{M}_{\star}(r)}{r^{2}}dr,\qquad(5)$$

which may be rewritten as:

$$-\frac{KT_{gas}}{G\mu\mathfrak{M}_{\rm H}}\left(\frac{d\log\rho_{gas}}{d\log r}+\frac{d\log T_{gas}}{d\log r}\right)r=\mathfrak{M}_{*}(r) \quad (6)$$

Putting numbers in gives

$$M(r) = -3.71 \times 10^{13} \, M_{\odot} \, T(r) \, r \left(\frac{d \, \log \rho_{g}}{d \, \log r} + \frac{d \, \log T}{d \, \log r} \right)$$

ere T is in units of keV and r is in units of Mnc. (



Intracluster Gas

- Majority (75%) of observable cluster mass (majority of baryons) is hot gas
- Temperature $T\sim 10^{7_8}~K\sim 1\text{--}10~keV$
- Electron number density $n_e \sim 10^{-3} \text{ cm}^{-3}$
- Mainly H, He, but with heavy elements (O, Fe, ..)
- Mainly emits X-rays
- $L_X \sim 10^{45}$ erg/s, most luminous extended X-ray sources in Universe
- Age \sim 2-10 Gyr

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The Intracluster Medium as a Fluid

$$\lambda_{p} \approx \lambda_{e} = \frac{3^{3/2} (kT)^{2}}{8\sqrt{\pi} n_{e} e^{4} \ln \Lambda} \qquad \text{mean free path of a particle}$$
$$\approx 23 \left(\frac{T}{10^{8} \text{ K}}\right)^{2} \left(\frac{n_{e}}{10^{-3} \text{ cm}^{-3}}\right)^{-1} \text{ kpc}$$

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X-ray Emission Processes

- Continuum emission
 - Thermal bremsstrahlung, ~exp(-hv/kT)
 - Bound-free (recombination)
 - Two Photon
- Line Emission

(line emission)





Chemical Abundances

Hitomi has the possibility to produce extremely precise chemical abundances



Hitomi SXS Data for Perseus Cluster 10 Fe XXIV DR Fe XXVI Ly**ß** Fe XXV K**y** Fe XXIV DR Ni XXVII Fe XXV K**B** Fe XXVI Lya Fe XXV K**δ** Fe XXV K**ε** ž Fe I fluor. Mn XXIV S, counts s⁻¹ keV⁻¹ IIIXX e L ა || || L T I ||| | |0.1 5.5 6 6.5 7.5 8.5 7 8 E (observed), keV 3 ×× S, counts s⁻¹ keV⁻¹ Fe I fluorescent e Fe XXIV DR Ni XXVII Fe XXV K**B** - Fe XXIV DR - Fe XXVI Lyβ - Fe XXV Kγ Fe XXVI Lya Fe XXV Kδ
 Fe XXV Kε 2 Cr XXIII - Mn XXIV || 11 1 | | |I 0 5.5 8.5 8 6 6.5 7.5 7 E (observed), keV

Full array

Heating and Cooling of ICM

- What determines temperature T?
- Why is ICM so hot?
- What are heating processes?
 - gravitational heating
 - nongravitational heating (SNe, AGNs)
- What are cooling processes?

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Why is gas so hot?

- Clusters have huge masses, very deep gravitational potential wells
- Any natural way of introducing gas causes it to move rapidly and undergo fast shocks

infall

galaxy ejection









Sunyaev-Zel'dovich Effect

Single Clusters

- Measure of integrated pressure (total thermal energy)
- Distances, H_o, H(z)
- Cluster gas mass fractions, cluster structure, evolution studies
- Peculiar velocities at high z

SZ Cluster Surveys

- Exploit SZ redshift independence
- Measure growth of structure and large scale velocity fields to constrain Dark Energy

 $\frac{\Delta T_{SZE}}{T_{CMB}} \propto \int n_e T_e dl$

$$S \propto \int \Delta T_{SZE} d\Omega$$

 $\propto \frac{1}{D_A(z)^2} \int n_e T_e dV$

Carlstrom

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S-Z Simple Physics

- The optical depth for the S-Z effect is small
- the density of electrons is of order $n_e \sim 10^{-3}$ cm⁻³, the path length ` through a cluster medium ~ several Mpc. With a Thomson cross section σ = 6.65 x10 ⁻²⁵ cm²,

optical depth $\tau = n_e \sigma l \sim 0.005; ~ 1\%$

- probability that a CMB photon crossing a rich cluster is scattered by an electron.
- Since the electron energy is much larger that the energy of the photon, to first order $\delta v/v \sim kTe/m_ec^2 = 1\%$. The resulting fractional temperature change of the CMB is of the order of 10^{-4} ,~ $300\mu k$
- For a review see Carnegie Observatories Astrophysics Series, Vol. 3: Clusters of Galaxies: Probes of Cosmological Structure and Galaxy Evolution, 2004 Using the Sunyaev-Zelídovich Effectto Probe the Gas in Clusters MARK BIRKINSHAW

The spectrum of the thermal SZE has a characteristic shape all interacting CMB photons get approximately a 1% boost in energy, the result is a transfer of photons in the CMB spectrum from lower to higher frequencies, resulting in a decrease of brightness at low frequencies

A Strange Fact

- As clusters are observed at higher redshifts the solid angle which scatters the CMB gets smaller- however the CMB gets brighter in the past
- These two terms almost cancel IF the cluster hot gas were the same at higher redshifts.
- Since we expect the cluster hot gas to evolve with z it is not clear what the total effect will be .
- The amplitude of the S-Z effect is t independent of D_A the angular distance

Fig.1. Map of Abell 2163 at 150 GHz, overlaid with XMM-Newton X-ray contours (see Fig. 3) in units of 10^{-13} erg s⁻¹cm⁻²arcmin⁻². Because the correlated-noise re-

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Sunyaev-Zeldovich Distances

- The Sunyaev-Zeldovich effect is the Compton scattering of microwave background photons off the hot electrons in the IGM in the cluster
- At present ~400 clusters have measured S-Z effect "decrements" and x-ray temperatures (Primarily from Planck and the South Pole Telescope and the Atacama Cosmology telescope)

Angular distance $D_A:\Delta T_0$ is the S-Z decrement, S_{X0} the x-ray surface brightness, T_{e0} the x-ray temperature, θ an angular size and Λ the cooling function

All quantities are directly measurable with an x-ray image, temperature map and S-Z image

Sunyaev-Zeldovich effect

- Compton scattering changes both the angular and energy distribution of the microwave background
- At low frequencies the result is a diminution (decrement) in the surface brightness of the MWB whose amplitude and shape depends on the Compton optical depth, the 3-D distribution of the hot electrons and their temperature

Fig. 1.— The spectrum of the microwave background radiation, and the microwave background radiation after passage through an (exaggerated) scattering atmosphere with y = 0.1 and $\tau\beta = 0.05$ (as defined in Sections 3 and 6), compared with the integrated

— The scattering geometry, in the frame of rest of the electron before the interaction. ming photon, at angle θ relative to the x_e axis, is deflected by angle ϕ_{12} , and emerges

Sunyaev-Zeldovich effect

- The main technical limits are the long exposures required in both the x-ray band and the milli-meter (~1 day each for the highest z clusters)
- The S-Z decrement is independent of redshift, while the x-ray surface brightness drops as $(1+z)^4$

Setting a practical limit to z~1.3 for the x-ray measurements

• In a massive cluster the typical optical depth is $\tau \sim 0.1$

X-ray image with S-Z contours for z=0.54 cluster

S-Z contours images for a sample of clusters from $z\sim0.3-0.9$ 7

Feedback- How AGN Influence the Cluster Gas

Direct evidence from cluster x-ray images combined with radio data that central AGN has strongly influenced the gas

Jet power ~ feedback?

Cavities and Low Freq Radio Emission

• The giant cavities seen in many cooling flow clusters are often 'filled' by low frequency radio emitting plasma

A262 Clarke et al 2009

Hydra A Wise et al 2007

Effects of Feedback in Image and Temperature

the hot gas can apparently be strongly affected by AGN activitydirect evidence of the ability of SMBHs to influence environment on large scales

Why are Clusters Interesting or Important

Formation and evolution of cosmic structure

- The Cooling flow problem
- Interaction of radio sources and the hot gas
- Star formation
 - Why are cluster galaxies different than those in the field
- AGN evolution
- Cosmological constraints
 - Evolution of clusters is a strong function of cosmological parameters
 - How to utilize this information
 - Evolution of mass function of clusters
 - Power spectrum of clusters (BAO)

Plasma physics on the largest scaleslots of detailed physics Numerical Simulations

There is a vast literature on numerical simulations of the formation and evolution of structure The properties of clusters of galaxies are one of the strongest tests of these techniques

Particle acceleration

appear in clusters

Cluster shocks source of highest E cosmic rays? Certain types of radio sources only

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Next topic – Black Holes and Active Galaxies Chapter 9 in S&G