The Basic Structure of Present-Day Galaxies

1) Basic description of galaxy ‘components’
   - Stellar distribution: bulge, disk, bars,
   - Distribution of gas (and dust)
   - Dark matter halo

2) Parameter Relations in Galaxies
   - Tully-Fisher, the ‘Fundamental Plane’ and the Kormendy relations
   - Morphology, mass vs. kinematics
   - Stellar mass vs. halo mass

3) Morphology and structure vs. formation history
   - the sizes of disk galaxies
   - the shapes of massive galaxies

4) Extreme ends of the galaxy property spectrum
   - the smallest galaxies
   - the most massive galaxies and galaxy clusters
Multiwavelength Milky Way
M87 with HST
Interacting/merging galaxies
X-ray (hot gas) in nearby Elliptical galaxies with Chandra satellite

Galaxy cluster Abell 1689 (HST)

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Basic Description of the Stellar Distribution

- For fairly massive galaxies a basic two-component description of the stellar distribution proves useful:
  - **Bulges/spheroids**
  - **Disks**
- Radial profile description

Sersic (1968) profile

\[
\Sigma(r) = \Sigma_0 e^{-\kappa [(r/r_e)^{1/n} - 1]}
\]

\[
\kappa \approx 2n - 0.331
\]

**Disks:** \( n \sim 1 \): ‘exponential profile’

**Spheroids:** \( n \sim 2-5 \) (\( n=4 \): deVaucouleur)

NB: \( n_{\text{spheroid}} = f(L_{\text{spheroid}}) \)

Note: bulge/disk approach (3D shape \( \leftrightarrow \) profile) not sensible for low-mass galaxies
Radial profiles: Comments

- Many (massive) ellipticals fit the de Vaucouleur’s profile beautifully

- Bulge-disk decompositions on the basis of radial profiles alone are terribly prone to fitting degeneracies
Bulge-to-Disk Ratios in the Present-Day Universe
(e.g. Tasca and White 2005 and Benson et al 2007 based on SDSS)

- Bulge-disk decomposition is interesting, because
  a) disk-stars: no violent relaxation
  b) Spheroid stars: post-violent relax
  c) $M_{BH} \sim M_{Spheroid}$

Globally:
- 60% of r-band light from disks
- 40% from spheroids

In stellar mass:
- 40%/60% disk/spheroid mass fraction

Spheroids dominate the massive end
Vertical stellar profile can often be described by \( f(z) = \text{sech}^{2/N}(Nz/z_0) \).

In most galaxy disks a description by two vertical components is suggested (incl. Milky Way)
- Thicker \( \rightarrow \) more (vertical) kinetic energy \( \rightarrow \) Why?

(Some) stellar disks are ‘truncated’ in radius
- Max. angular momentum, or
- Threshold in star-formation efficiency?
Structure of Galaxy Disks II

• Stellar bars are common in disk galaxies
  – Often only recognized in near-IR images (less dust)
  – Consequence of disk instability
  – Effective means of angular momentum transport

• Spiral arms are common and coherent features
  – even after accounting for young stars

• e.g. M51, Rix and Rieke 1995
The 3D Shapes of Spheroidal Galaxies

- What is the relation between intrinsic shape and projected ellipticity

  axially symmetric case (oblate or prolate, see Binney/Merrifield):

  \[ q_{\text{internal}}^2 \sin^2 i + \cos^2 i = \begin{cases} q_{\text{projected}}^2 & \text{(oblate)} \\ 1 / q_{\text{projected}}^2 & \text{(prolate)} \end{cases} \]

- If we view a sample from random angles, then \( \cos(i) \) is uniform

  \[ a : b : c \approx 1 : 0.95 : 0.7 \]

- Massive spheroidal galaxies are nearly oblate and only somewhat flat
Color-gradients in Galaxies

- Almost all galaxies become bluer outward
- Combination of
  - Decreasing dust
  - Decreasing age(?)
  - Decreasing metallicity
- Sheroids are redder/older than disks

Ensemble of spiral galaxies with dust and red bulges at the center →
(de Jong 1996)
Basic Kinematics of Spheroidal Galaxies

Stellar velocity fields for nearby spheroidal galaxies
(Capellari, deZeeuw, Bacon, et al 2005)

- Generically:
  - Rotation rises slowly outwards
  - Dispersion falls gently outward

- $0 < v/\sigma < 1.5$
Interstellar gas occurs in a wide range of physical conditions.

<table>
<thead>
<tr>
<th>Name</th>
<th>State</th>
<th>Density</th>
<th>Temperature</th>
<th>Main diagnostics</th>
</tr>
</thead>
<tbody>
<tr>
<td>&quot;hot&quot;</td>
<td>fully ionized</td>
<td>$10^{-2} \text{ cm}^{-3}$</td>
<td>$10^6 \text{ K}$</td>
<td>X-rays UV absorption</td>
</tr>
<tr>
<td>warm (H II)</td>
<td>fully ionized</td>
<td>$1 \text{ cm}^{-3}$</td>
<td>$10^4 \text{ K}$</td>
<td>Optical emission lines</td>
</tr>
<tr>
<td>neutral (H I)</td>
<td>neutral atomic</td>
<td>$1 \text{ cm}^{-3}$</td>
<td>$10^2 \text{ K}$</td>
<td>21cm line</td>
</tr>
<tr>
<td>&quot;cold&quot; molecular gas</td>
<td>molecular</td>
<td>100</td>
<td>20 K</td>
<td>CO lines (radio, sub-mm)</td>
</tr>
</tbody>
</table>

What sets the temperature and the physical state of the gas?

Heating processes
- photo-ionization
- mechanical (shock) heating

Cooling processes
- Bremsstrahlung
- line cooling
Galaxies and their Dark Matter Halos

- All evidence for dark matter halos on galaxy scales comes from the comparison/modeling of kinematic tracers with identified mass components.

  - Kinematic tracers: stars, cold gas (HI and Ha), hot gas (X-ray), satellites (GCs and galaxies) and photons (gravitational lensing)

  - Identified (baryonic) mass components: stars, hot gas (in clusters), cold gas (~10% of stars)

- Historically:
  - Need for dark matter from dynamics on scales of galaxies played an enormous role in establishing its (dynamical) existence

- Current Paradigm:
  - Dark matter is a indispensable ingredient in structure formation; galaxies are the places where DM is least dominant → DM studies on galaxy scales can be tricky
Observational Constraints on Dark Matter Halos around Big Galaxies

a) HI rotation curves

"flat" to \( \sim 30 \) kpc (\( \Rightarrow R_{\text{opt}} \))

\[
V_c^2(R) = -R \frac{d \Phi(\vec{r})}{d R} \approx -\frac{g}{R} M(<R)/R
\]
Note: can't constrain 2 functions, $\rho_*(r)$ and $\rho_{DM}(r)$, by only one observable function $V_c(r) \rightarrow$ degeneracies
b) Satellite galaxies

e.g. Zaritsky 1994, Prada et al 2002 by stacking images
→ DM halos around MW-like galaxies extend to >200kpc

NFW profile:

\[ \rho(r) = \frac{\delta_s}{[(r/r_s)(1 + r/r_s)^2]} \]
Present-Day knowledge about Dark Matter Halos

c) Strong and weak gravitational lensing

(Maoz and Rix 1993; Brainerd et al 1988; McKay et al 2001)

Background galaxy lensed into arcs by lens

(Sheldon et al. 2004; SDSS)

Correlation function between

a) Shear (from gravitational lensing seen in background images)

b) Position of foreground galaxies
d) X-ray gas around massive galaxies

- Only in massive galaxies (and galaxy clusters) is the ‘hot’ phase hot enough to be detected by current X-ray satellites
- Assume gas is in (approximate) hydrostatic equilibrium

\[
\ln \left( \frac{\rho_g}{\rho_{g0}} \right) = - \ln \left( \frac{T}{T_0} \right) - G \mu m_p \int_{R_0}^{R} \frac{M_{\text{grav}}(<R)}{kT R^2} dR
\]

- In all massive galaxies with good measurements:
  DM halo with properties expected from $\Lambda$CDM (NFW halo)
2) ‘Parameter Relations’ in (Present-Day) Galaxies

Many parameters with which to describe the stellar component of galaxies are tightly correlated (though such correlations are/were not ‘expected’)

Most of them can be cast as

(stellar) luminosity/mass vs

- size
- characteristic velocity (Tully-Fisher; Faber-Jackson)
- 3D - shape
- (radial) concentration, black hole mass

These correlations are important constraints on galaxy formation mechanisms
John Kormendy has been a pioneer in pointing out that the photometric descriptions are correlated.
The ‘Tully-Fisher’ Relation for Disk Galaxies

- Tully&Fisher 1977
  - HI linewidth correlates well with absolute magnitude of spiral galaxy.

- In general:
  - Correlation between circular velocity and stellar luminosity
  - $L_{\text{opt}}$ can predict $v_{\text{circ}}$ to $\sim$5-8%
    - $M_*, L_{\text{opt}} \sim v_c^{3-4}$
  - Historically: extremely important distance indicator
  - Now: also constraint on galaxy formation
Explanations for a Tully-Fisher-like relation

Let’s consider the self-gravitating case

\[ v_{\text{max}}^2 \sim G \Sigma_0 R_d \quad \text{with} \quad \Sigma_0 \text{ central mass density and } R_d \text{ scale length} \]

\[ \Rightarrow L \sim v_{\text{max}}^4 I_0^{-1} \Gamma_{\text{disk}}^{-2} \quad \text{with} \quad I_0 = \Sigma_0/\Gamma_{\text{disk}} \]

Right slope, but central surface brightness/mass density should be a 3rd parameter

Let’s presume the disk is a small fraction assembled from a DM halo

For the halo (also Mo, Mao and White 1993)

\[ r_{\text{vir}} = \sqrt{\frac{2}{\Delta_{\text{vir}}(z)}} \frac{V_{\text{vir}}}{H(z)} \quad \text{and} \quad M_{\text{vir}} = \sqrt{\frac{2}{\Delta_{\text{vir}}(z)}} \frac{V_{\text{vir}}^3}{G H(z)} \]

\[ \rho_{\text{crit}} = 3H^2(z)/(8\pi G) \]

\[ M_d \approx 1.3 \times 10^{11} h^{-1} M_\odot \left( \frac{m_d}{0.05} \right) \left( \frac{V_{\text{vir}}}{200 \text{ km s}^{-1}} \right)^3 \]

with NO surface brightness/mass dependence!

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Parameter relations for (massive) spheroids: Faber-Jackson and the ‘fundamental plane’

- For spheroids: \( \rightarrow \) 3-parameter relation!!
- \( M/L = f(M) \)

One version of the ‘fundamental plane’, involving \( L, R_e, \sigma_* \)
Rotation support and isophote shape = \( f(L) \)
Stellar mass vs. Halo Mass
How efficient is galaxy formation?

Identify (observed) galaxy populations with (simulated) halos that have the same clustering properties.

Dark matter halos cluster … more massive → more clustered

M/L strong function of M!

Van den Bosch et al 2006
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3) Galaxy Structure vs Formation Mechanisms

a) (Disk) Galaxy Sizes and Angular Momentum

- In disk galaxies the stellar body is centrifugally supported (stars move on near-circular orbits), with a "spin parameter",

\[ \lambda = \frac{J}{G \sqrt{E/M^5}} \]

where \( J \) is the angular momentum and \( E \) is the binding energy of the system.

\( \lambda^*, \text{observed} \approx 0.5 - 1 \) for disks (\( \lambda^* \approx 0.005 \) for spheroids)

\( \rightarrow \) Disk size is given by the angular momentum of the material

Angular momentum comes from torques of (adjacent) mass distribution (Hoyle 1949, Ryden and Gunn 1987)

Linear theory: \( \lambda_{\text{total}} = \lambda_{\text{DM}} = \lambda_{\text{gas (init)}} \approx 1/20 \)
Why galaxies are disks of a characteristic size

• Torques before the collapse induce spin $\lambda \sim 0.07$

• Gas dissipates (by radiation) all the energy it can without violating angular momentum conservation $\Rightarrow$ circular orbit

• Fall and Efstathion (1980) showed that observed galaxy disks ($\lambda \sim 0.5$) can form only in DM halos through dissipation $\Rightarrow$ central concentration ($J$ conserved) $\Rightarrow$ spin-up.

a) Presume there is no DM:

\[ \lambda_{\text{obs}} = \frac{J \cdot E^{1/2}}{GM^{5/2}} = \lambda_{\text{init}} \sqrt{\frac{R_{\text{init}}}{R}} \Rightarrow \frac{R_{\text{init}}}{R} \approx 50 \]

We observe $M_{\text{disk}} \approx 5 \times 10^{10} \, M_{\text{sun}}, \ R_{\text{disk}} \approx 8 \, \text{kpc} \Rightarrow R_{\text{init}} \approx 400 \, \text{kpc}$

$\Rightarrow R_{\text{turn-around}} \approx 2 \ R_{\text{init}} \approx 800 \, \text{kpc}$

$\Rightarrow t_{\text{collapse}} \sim 50 \cdot 10^9 \, \text{years}$ for $M \sim 5 \times 10^{10} \, M_{\text{sun}}$
b) If the gas is only a small fraction of the total mass:
⇒ $v_c(r)$ remains unchanged

⇒ $R_{\text{init}}/R \sim \frac{\lambda_{\text{obs}}}{\lambda_{\text{init}}}$ ⇒ $R_{\text{init}} \sim 80 \text{ kpc}$

⇒ $t_{\text{dyn}} \sim 10^9 \text{ years}$

and there is enough time to form disks.

It turns out that the assumption of angular momentum conservation during the gas dissipation yield disk sizes as observed (assuming $\lambda \sim 0.07$)

However: in (numerical) simulations much of the angular momentum is lost → modelled disks too small (unsolved)
Luminosity/Mass vs. Size
[state of the art incarnation: Shen et al 2004 based on SDSS]

- Well defined size relations with \( \sim 2.5 \) scatter
  \[ R \sim M^{0.5} \]
  at \( M>3\times10^{10} \) \( M_{\odot} \)

- Galaxy (stellar) sizes are related to the characteristic angular momentum of the stars (see below)
Why are massive galaxies spheroids?

1. Stars form from dense, cold gas
   - either in disks
   - or from gas that is (violently) shock compressed
2. In the established cosmological paradigm larger (halos) form from the coalescence of smaller units

→ Stars in an (near) equilibrium system form from a disk and stay disk-like
→ ‘Violent relaxation’ shaking up stars (or stars formed during such an event) end up in spheroids

Is it plausible that in nearly all massive galaxies a (major) merger occurred after star-formation was largely complete?
Some physics of mergers

Mergers $\rightarrow$ devaucouleur’s profile
(Barnes 1989)

+ Some gas dissipation is needed to get the (central) densities of ellipticals ‘right’

Merging moves objects ‘within’ the fundamental plane!
The Smallest and the Largest Galaxies

Questions:

- Is there an empirical (upper/lower) limit to ‘galaxies’?

1) ‘Dwarf’ Galaxies

- Definition (not universally established):
  - galaxy that has < $1/10^{th}$ of $L_\odot$ (or $M_\odot$) Milky_Way
  - or $v_{\text{circ}} < 100$ km/s

- Most abundant type of galaxies; contributes negligibly to the total stellar mass budget.

- Structure and morphologies
  - Often ‘irregular’ (highly asymmetric)
  - Often of very low surface brightness

- Stellar populations
  - Inevitably low metallicity (<1/10 solar)
  - Some have very young pops. (most stars after $z < 0.5$)
  - Some have only old (>10Gyrs) stars, many are mixed populations

- Dwarfs are interesting regime to test gravity $\leftrightarrow$ ‘feed-back’

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The Faintest Galaxies Known to Date
Milky Way Satellites

- Most found recently by SDSS (e.g. Belokurov et al 2006)
- Seem to be dark matter dominated
- Same luminosity as globular clusters, but 1000x lower stellar surface mass density
The Extreme Limit of “Galaxy Clustering”

Galaxy Clusters

Galaxy Cluster Abell 2218
NASA, A. Fruchter and the ERO Team (STScI, ST-ECF) • STScI-PRC00-08
cD galaxies: the most massive galaxies

- Galaxies with \( \geq 5 \, L_{\text{MW}} \) are only found at the centers of galaxy clusters

- They are without exception spheroidal

- They have extended light profiles that blend into ‘intra-cluster’ light

‘stacked’ image of 700 cluster centers (Zibetti et al 2005)
Virgo Cluster:
- Nearest large galaxy cluster with more than 2000 galaxies brighter than $M_R \simeq -14$ ($L_R \sim 10^{7.8} L_\odot$)
- Distance $\sim 17 Mpc$ (dependent on $H_0$)
- Extend $\sim 10^\circ \equiv 3 Mpc \times 3 Mpc$
- Irregular cluster, densest regions dominated by ellipticals
- Velocity dispersion of galaxies about 600 km/s

Coma Cluster:
- One of the most luminous clusters known
- Distance $\sim 100 Mpc$ (dependent on $H_0$)
- Regular cluster with probably subcluster merging from SW
- Dominated by ellipticals and S0s, two central cDs and one in subcluster
- Velocity dispersion of galaxies about 1000 km/s
- Strong X-ray source
Galaxy Clusters are filled with Hot Gas

Coma cluster (left: optical image, right: X-ray image)
The X-ray spectra show the characteristics of Bremsstrahlung of a $\sim 10^8 K$ hot gas. The volume emissivity is: 
\[ \frac{dP}{dV} = 2.410^{-27} T^{-1/2} N_e^2 \ \text{[erg cm}^3 \text{s]} \]

The cooling time of the plasma is: 
\[ t_{cool} = \frac{3N_e kT}{dP/dV} \approx \frac{10^{14} T^{1/2}}{N_e} \ \text{[s]} \]

For the center of the Coma cluster we have:

\[ L \approx 10^{44} \text{erg/s} \]
\[ n_e \approx 10^{-3} \text{cm}^{-3} \]
\[ t_{cool} \approx 10^{10} \text{yr/s} \]
\[ M_{gas} \approx 10^{13} M_\odot \]

The following correlations exist between the different components of galaxy clusters:

- The central galaxy density is higher for higher $L_X$.
- The fraction of spirals is lower for higher $L_X$.
- The temperature $T$ is proportional to $L_X$ and typically $10^8 K$.
- The gas metallicity is lower for higher $T$ and typically 1/3 of solar.
- The ratio of gas-mass to galaxy-mass increases with $T$ up to 5 or more.
- The dominant component in all clusters is dark matter. This follows consistently from the dynamics of galaxies, the hydrostatic equilibrium of the X-ray gas and from gravitational lensing. The typical mass ratios are:

\[ \text{galaxies} : \text{X-ray-gas} : \text{dark-matter} \approx 1 : 5 : 25 \]

From R. Bender
Galaxy Properties: Summary

- Description of the stellar body of galaxies
  - Spheroid: post-violent relaxation/merger stars
  - Disks: not shook-up since formation
  - In the present-day universe ~50%/50

- The variety of galaxies in
  - Morphology, shape, structure, ...
  - Stellar content and metallicity....
    is very restricted (many parameter relations).

- The stellar mass range of galaxies
  - Clearly limited at upper end: ‘brightest cluster galaxies’
  - No end in sight (<1000 M*) at the lower end?

- Milky Way
  - Typical galaxies in many ways
  - Central in shaping our thinking about galaxies
    - (historically, but also in future)