



Lecture 19 : Weighing the Universe, and the need for dark matter

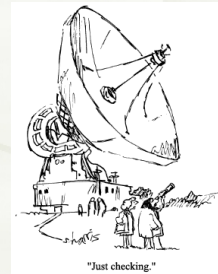
★ Baryonic matter and nucleosynthesis

- ★ Stellar nucleosynthesis
- ★ The importance of measuring the total density parameter Ω

★ Measuring the mass of the Universe

- ★ Mass to light ratio
- ★ Mass of luminous stars
- ★ Masses of galaxies and galaxy clusters

★ Non-baryonic dark matter



© Sidney Harris

This week: start reading Chapter 13

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How are other elements formed?

★ Big Bang Nucleosynthesis produces most of the hydrogen & helium observed today.

★ But what about other elements?

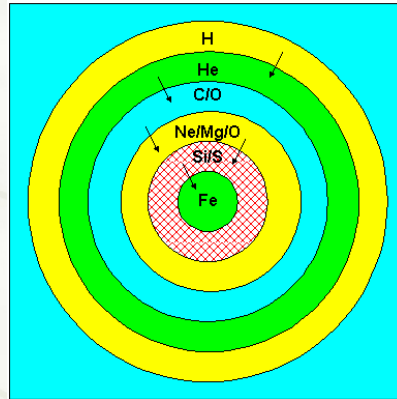
- ★ There are naturally occurring elements as heavy as Uranium
- ★ Some elements (e.g., Carbon, Nitrogen, Oxygen) are rather plentiful (1 atom in every 10^5 atoms)
- ★ Astronomers believe these elements were formed in the cores of stars long after the big bang
 - ★ Theory of stellar nucleosynthesis was first worked out by Burbidge, Burbidge, Folwer, & Hoyle in 1957

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Stellar “burning”

- ✦ In the normal life of a star (main sequence)...
 - ✦ nuclear fusion turns Hydrogen into Helium
- ✦ In the late stages of the life of a massive star...
 - ✦ Helium converted into heavier elements (carbon, oxygen, ..., iron)
 - ✦ “Triple-alpha” process bridges stability gap from Be to C
 - ✦ At end of star’s life, get an onion-like structure (see picture to right)



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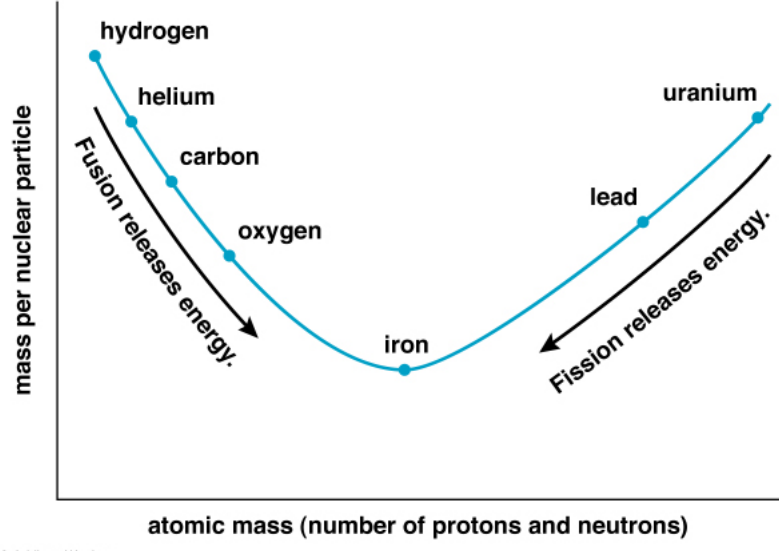
Iron, the most stable nucleus

- ✦ What’s special about iron?
 - ✦ Iron has the most stable nucleus
 - ✦ Fusing hydrogen to (eventually) iron releases energy (thus powers the star)
 - ✦ Further fusion of iron to give heavier elements would require energy to be put in...
 - ✦ Can only happen in the energetic environment of a supernova explosion

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Fission, fusion, and nuclear

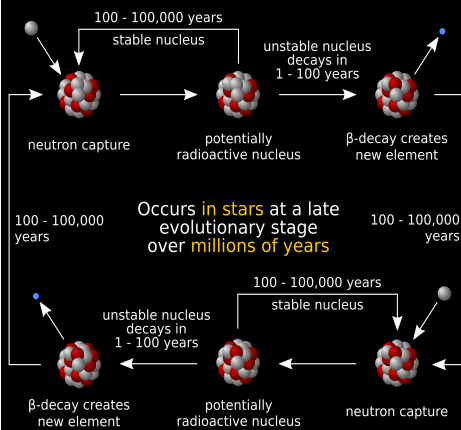


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Creating heavy elements by neutron capture

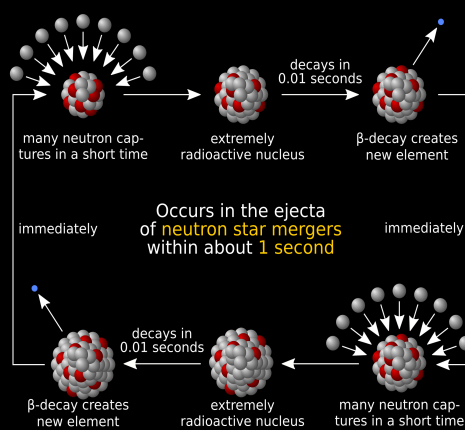
Slow neutron capture process (s-process)

There is a **small** number of free neutrons available, so the time to capture a neutron is **much longer** than the β -decay time.



Rapid neutron capture process (r-process)

There is a **huge** number of free neutrons available, so the time to capture a neutron is **much shorter** than the β -decay time.

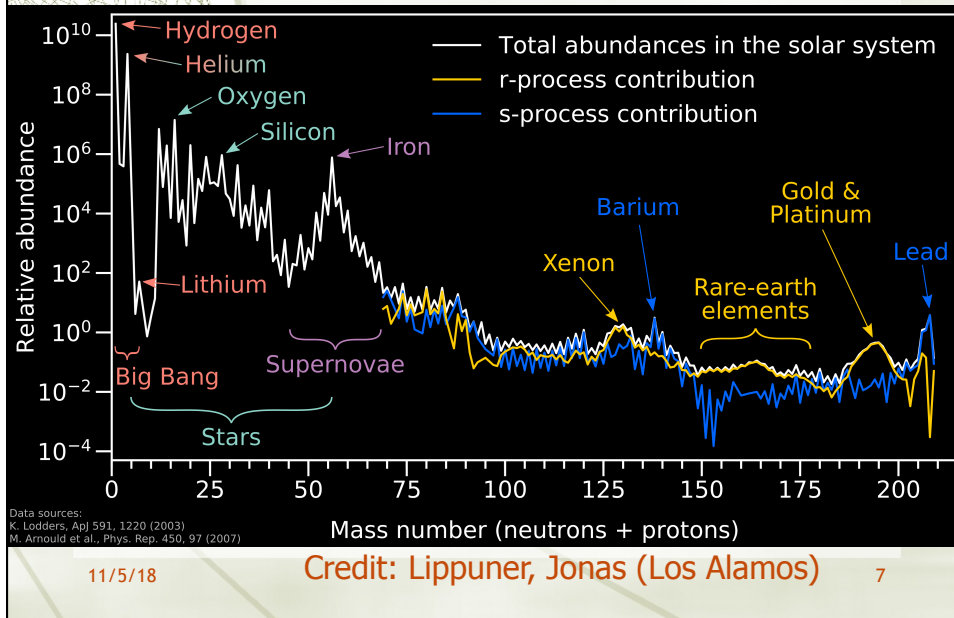


Credit: Lippuner, Jonas
Los Alamos

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Creating heavy elements



So... where are we?

- ★ We have described the first ~10 mins of the Universe's life...
 - ★ Origin of matter (well within first second)
 - ★ Origin of elements (within first few mins)
- ★ Universe continues to expand and cool...
 - ★ $t=70,000\text{yr}$: Radiation ceases to be dominant over matter
 - ★ $t=380,000\text{yr}$: Universe cools to the point where neutral hydrogen can form
 - ★ EPOCH OF RECOMBINATION
 - ★ Universe suddenly becomes transparent... photons free stream, redshift and are observed today as the CMB!!
- ★ Until now, there's essentially no structure in the Universe. To discuss emergence of structure, we need to look harder at contents of Universe

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RECAP

- ★ The density parameter for matter is defined as

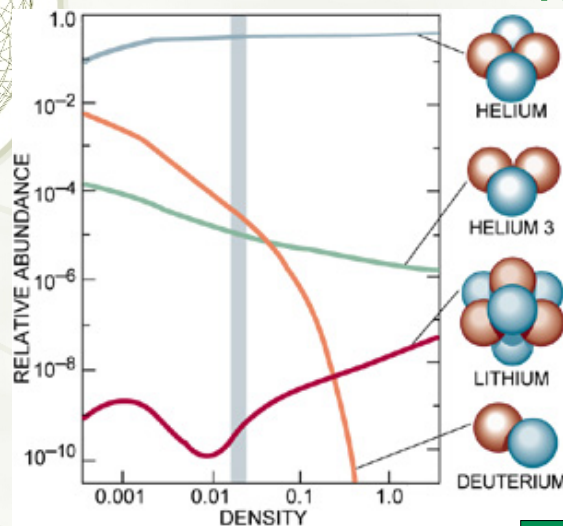
$$\Omega_M = \frac{\rho_{matter}}{\rho_{crit}} = \frac{\rho_{matter}}{3H_0^2 / (8\pi G)}$$

- ★ Value of Ω_M very important for determining the geometry and dynamics (and ultimate fate) of the Universe
- ★ Constraints from nucleosynthesis
 - ★ To get observed mixture of light elements, we need the baryon density parameter to be $\Omega_B \approx 0.049$
 - ★ If there were **only** baryonic matter (“normal” stuff made of protons, neutrons, & electrons) in the Universe, then this would imply that $\Omega_M \approx 0.049$.
 - ★ In that case, and if Λ were =0, the Universe would be open (hyperbolic) and would expand forever

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RECAP



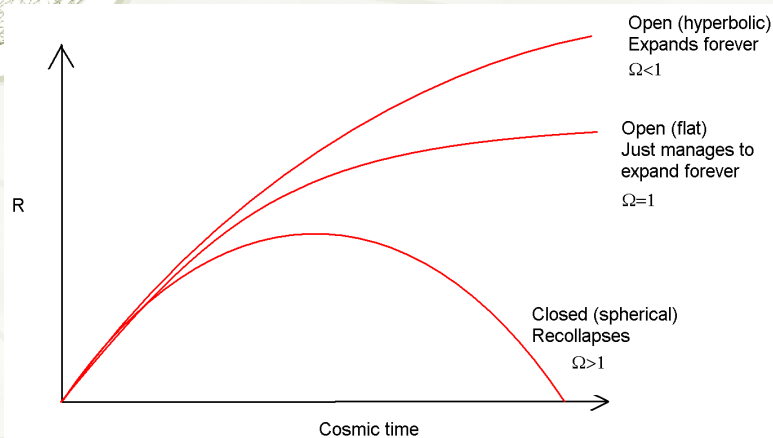
From M.White's webpage, UC Berkeley

$$\Omega_B h^2$$

$$h = \frac{H_0}{100 \text{ km/s/Mpc}}$$

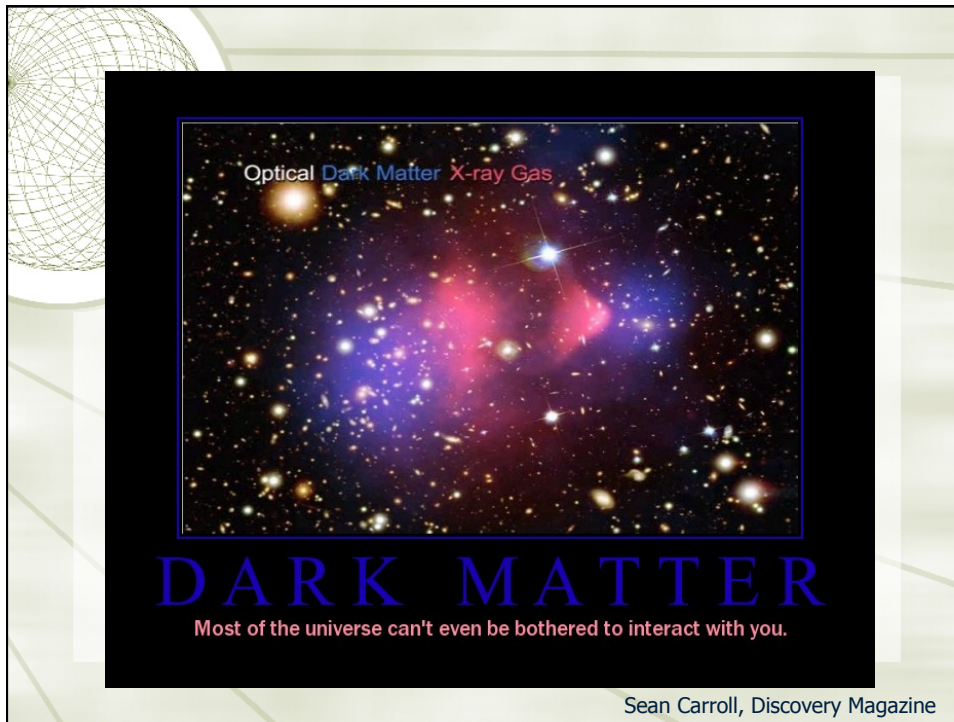
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Standard model evolution diagrams



Preview...

- ★ But life is more complicated than that...
 - ★ Much evidence shows that Ω_M may be 5 or 10 times larger than Ω_B , yet still $\Omega_M < 1$
 - ★ Additional evidence suggests that nevertheless, the Universe is flat, with $k = 0$ so $\Omega_k = 0$ (i.e. neither hyperbolic nor spherical geometrically)
 - ★ This implies the cosmological constant Λ must be nonzero... and in fact, there is observational evidence for accelerating expansion!
- ★ We'll start with the accounting of all forms of mass in the Universe...

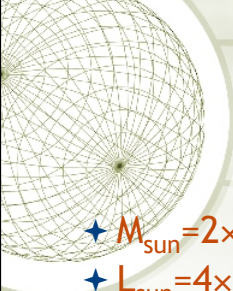


THE MASS OF STARS IN THE UNIVERSE

- ★ Stars are the easiest things to see and study in our Universe...
 - ★ Can study nearby stars in detail
 - ★ Can see the light from stars using “normal” optical telescopes in even distant galaxies.
- ★ But...what we see is the light, and what we’re interested in is the mass...
- ★ Need to convert between the two using the mass-to-light ratio M/L .

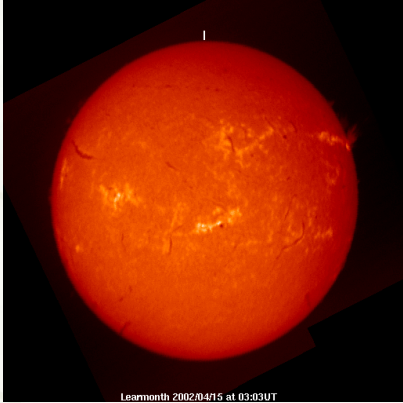
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The Sun



- ★ $M_{\text{sun}} = 2 \times 10^{30} \text{ kg}$
- ★ $L_{\text{sun}} = 4 \times 10^{26} \text{ W}$

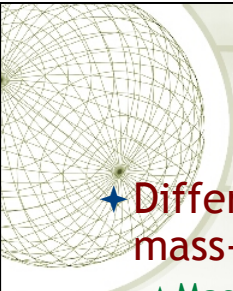
★ Actual numbers not very instructive...
 ★ From now on, we will reference mass-to-light ratios to the Sun ($M_{\text{sun}}/L_{\text{sun}}$).



Learnmonth 2002.034915 at 03:03UT

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Other stars



- ★ Different types of stars have different mass-to-light ratios
 - ★ Massive stars have small M/L (they shine brightly compared with their mass).
 - ★ Low-mass stars have large M/L (they are very dim compared with their mass).
 - ★ We're interested in an average M/L
- ★ Averaging regular stars near the Sun, we get $M/L \approx 3 M_{\text{sun}}/L_{\text{sun}}$

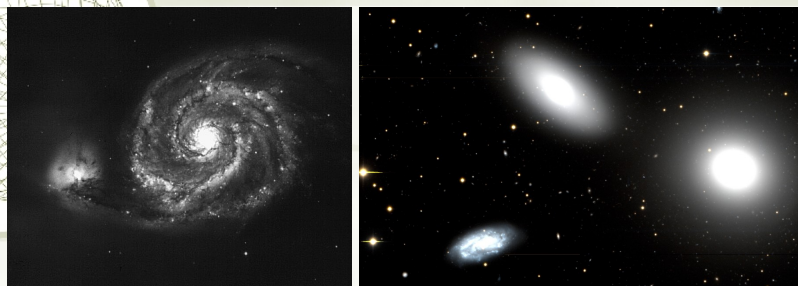
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- ★ But, we also need to include effect of “dead” stellar remnants...
 - ★ white dwarfs, neutron stars, black holes.
- ★ ...and also sub-stellar mass objects
 - ★ Called “brown dwarfs”
 - ★ Interior gravity is too low to compress gas and initiate fusion \Rightarrow very low luminosity
- ★ All of these have mass M , but very little light L .
 - ★ They add to the numerator of the average M/L , but not to the denominator
 - ★ Including the remnants and (smaller) brown dwarf contribution, this would increase the mass-to-light ratio for spiral galaxies to about

$$M/L \approx 10 M_{sun}/L_{sun}$$

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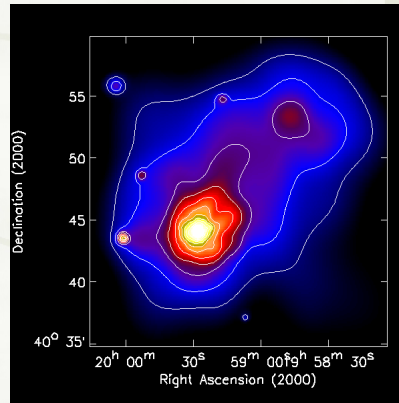
- ★ So, we can add up the visible star light that we see in the Universe, and convert to a mass in stars (luminous and non-luminous).
 - ★ We get $\Omega_L \approx 0.005-0.01$
 - ★ Comparing with $\Omega_B = 0.049$ from nucleosynthesis, we see that most baryons cannot be in stars...

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Where's the rest of the baryonic matter if it's not in stars?

- ★ Galaxy clusters contain a lot of hot gas outside of individual galaxies
 - ★ Gas temperature of 10-100 million K.
 - ★ Can see it using X-ray telescopes.
 - ★ Such gas contains a lot of the baryons
- ★ The rest is believed to be in "warm/hot" (1 million K) gas in intergalactic space.



X-ray emission from the hot gas trapped in the Cygnus-A cluster

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THE MASS OF GALAXIES

- ★ We can also measure total mass of a galaxy using Kepler's/Newton's laws
- ★ Remember that for planets orbiting Sun, square of period is proportional to cube of distance. Measuring in MKS,

$$P^2 = \frac{R^3}{(GM_{sun} / 4\pi^2)} = \frac{(2\pi R)^2 R}{GM_{sun}}$$

- ★ Can rewrite this as

$$M_{sun} = \frac{(2\pi R / P)^2 R}{G} = \frac{V^2 R}{G} \quad \text{or} \quad V = \sqrt{\frac{GM_{sun}}{R}}$$

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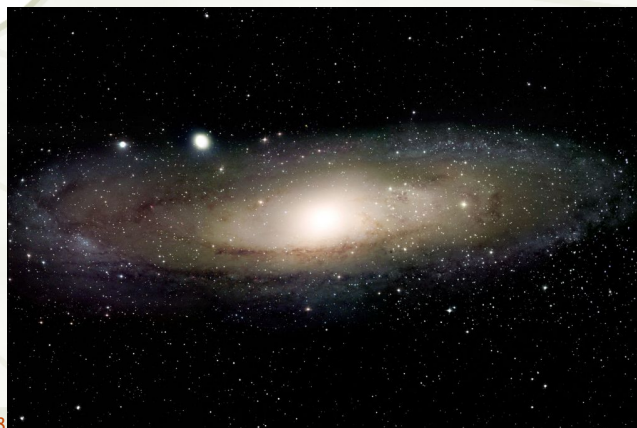
*Velocity dependence on radius
for a planet orbiting the Sun...*



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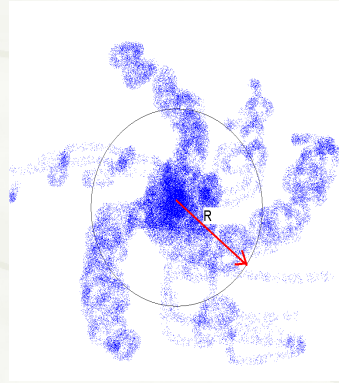
★ Apply same arguments to a galaxy...



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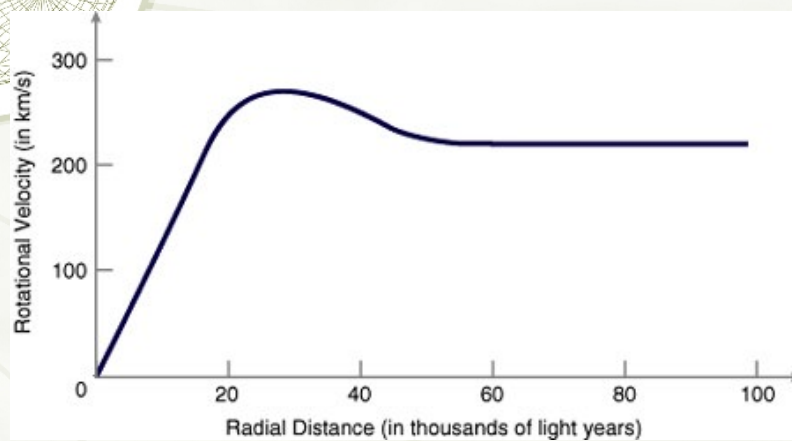
- Consider a star m in the galaxy at distance R from center
- Can measure how fast it's orbiting around the galaxy, V
- Acceleration of star is related to V and R (recall circular orbits have $a = V^2/R$)
- Then use Newton's law, $F = ma$, with F from the gravity of the rest of the galaxy acting on m
- Turns out that force is mainly due to the mass of the galaxy within the star's orbital radius R , $M_{\text{galaxy}}(<R)$
- Thus, can obtain mass of galaxy in terms of V and R :



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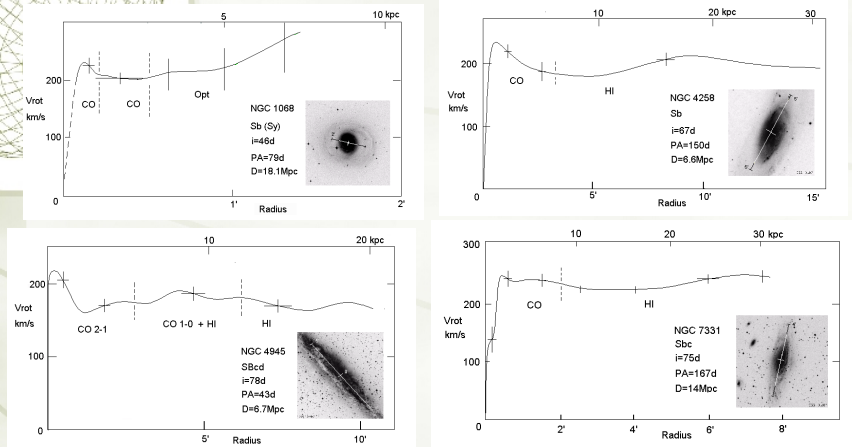
What do we see?



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Real measurements



In the outermost parts of galaxies, V and R are based on measurements of hydrogen gas atoms that orbit the galaxy, rather than stars

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Funny mass distribution?

- ✦ Orbital velocity stays almost constant as far out as we can track it
 - ✦ Means that enclosed mass increases linearly with distance
 - ✦ Mass continues to increase, even beyond the radius where the starlight stops
 - ✦ While there is enough diffuse gas out there to track V , it adds only a tiny amount of mass
 - ✦ So, in these outer regions of galaxies, the mass isn't luminous...
 - ✦ This is **DARK MATTER**.

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Pioneers of dark matter



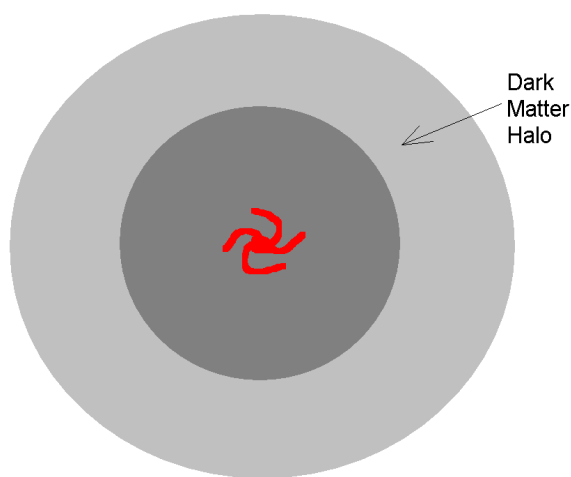
Vera Rubin
(1928-...)



Fritz Zwicky
(1898-1974)

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Called a dark matter “halo”



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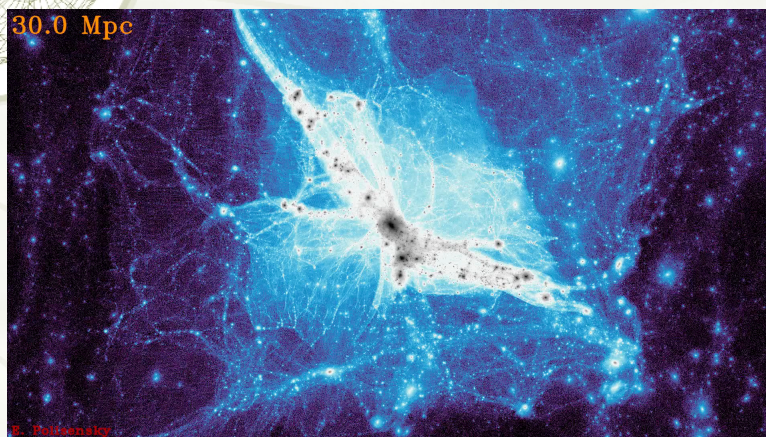
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Halos

- ★ How big are galaxy halos?
 - ★ We don't know!
 - ★ But they might be huge... maybe 10 times bigger than luminous part of the galaxy!
- ★ Add up all the galaxy halos... how much mass would there be?
 - ★ Uncertain - we don't know how far out galaxy halos go.
 - ★ Somewhere in range $\Omega_{\text{halos}}=0.1-0.3$

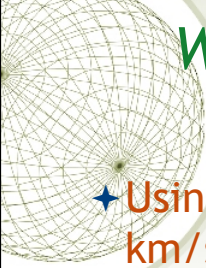
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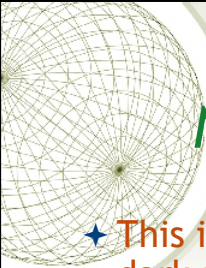
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What is the weight of the Milky Way?

- Using the formula $M=V^2R/G$, with $v=200$ km/s, $R=6 \times 10^{23}$ cm (that is 200 kpc) and $G=6.7 \times 10^{-8}$ (cgs units) what is the mass of the Milky Way?
 - $\sim 4 \times 10^{33}$ grams
 - $\sim 4 \times 10^{40}$ grams
 - $\sim 4 \times 10^{45}$ grams
 - $\sim 4 \times 10^{47}$ grams


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Non-baryonic dark matter

- This is our first evidence for non-baryonic dark matter...
 - $\Omega_B = 0.05$ (nucleosynthesis)
 - $\Omega_{\text{halos}} = 0.1-0.3$ (galaxy rotation curves)
- So, there is substantially more mass in the galaxy halos than could possibly be due to baryons!
- Suggests a non-baryonic form of matter may exist... something not based on protons and neutrons.

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MASS OF GALAXY CLUSTERS

- ★ Galaxy clusters
 - ★ Large groups of galaxies
 - ★ Bound together by mutual gravitational attraction
 - ★ Let's use same arguments for velocities and radii of galaxies in cluster as for V and R of stars in galaxies (i.e., based on Newton's laws) to measure mass...

$$M_{cluster} (< R) \approx V_{gal}^2 R / G$$

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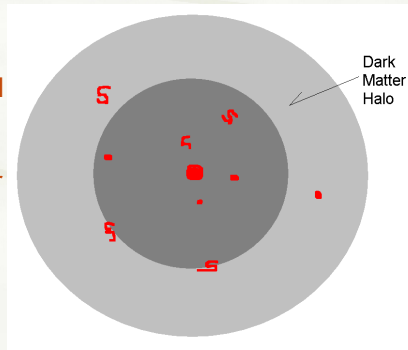
The Virgo cluster



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Dark matter in clusters

- Find that here is a giant halo of dark matter enveloping the galaxy cluster
- Includes the individual halos "attached" to each galaxy in cluster
- Also includes dark matter ripped from individual galaxies' halos, or never attached to them
- Add up the mass in these cluster halos...
- $\Omega_{\text{cluster}} = 0.3$
- Some of this mass is in hot gas in the cluster (contributing to $\Omega_{\text{B}} = 0.05$ from nucleosynthesis), but most is non-baryonic dark matter

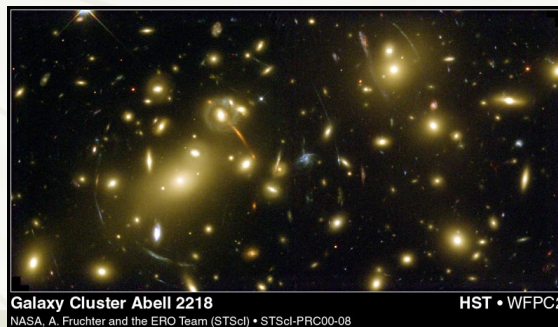


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Gravitational lensing...

- In some cases, can also measure cluster mass using gravitational lensing.
- Get good agreement with dynamical measurements



Galaxy Cluster Abell 2218

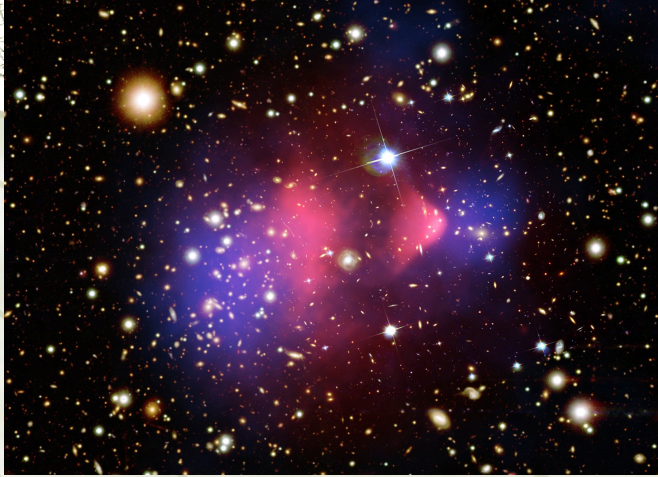
HST • WFPC2

NASA, A. Fruchter and the ERO Team (STScI) • STScI-PRC00-08

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A cosmic collision: the Bullet Cluster



- ◆ Red: X-rays (hot gas)
- ◆ Blue: Matter from lensing

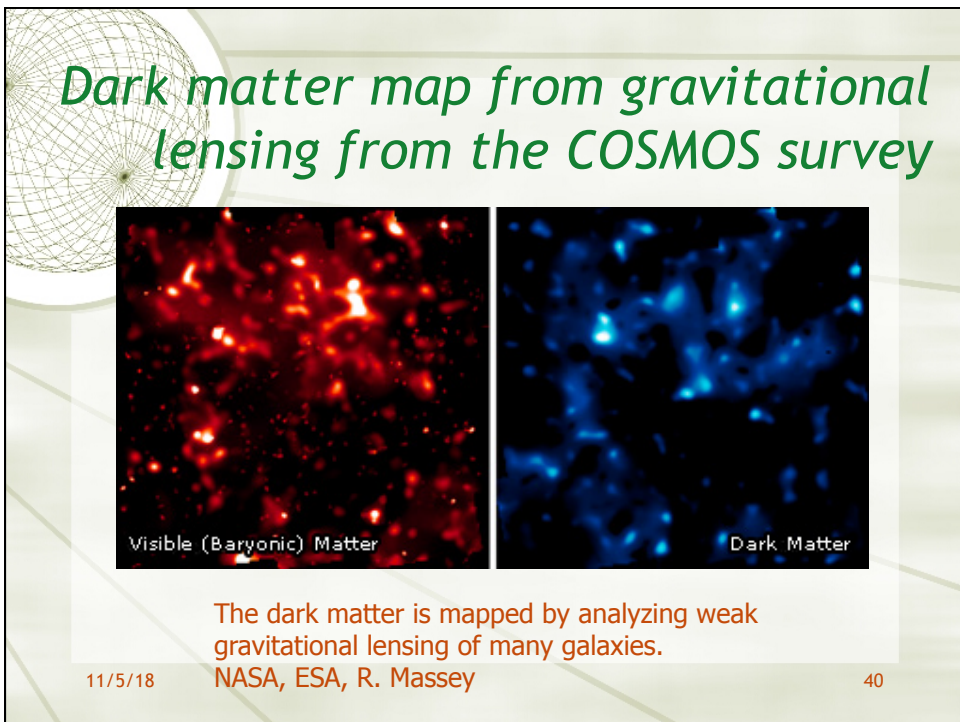
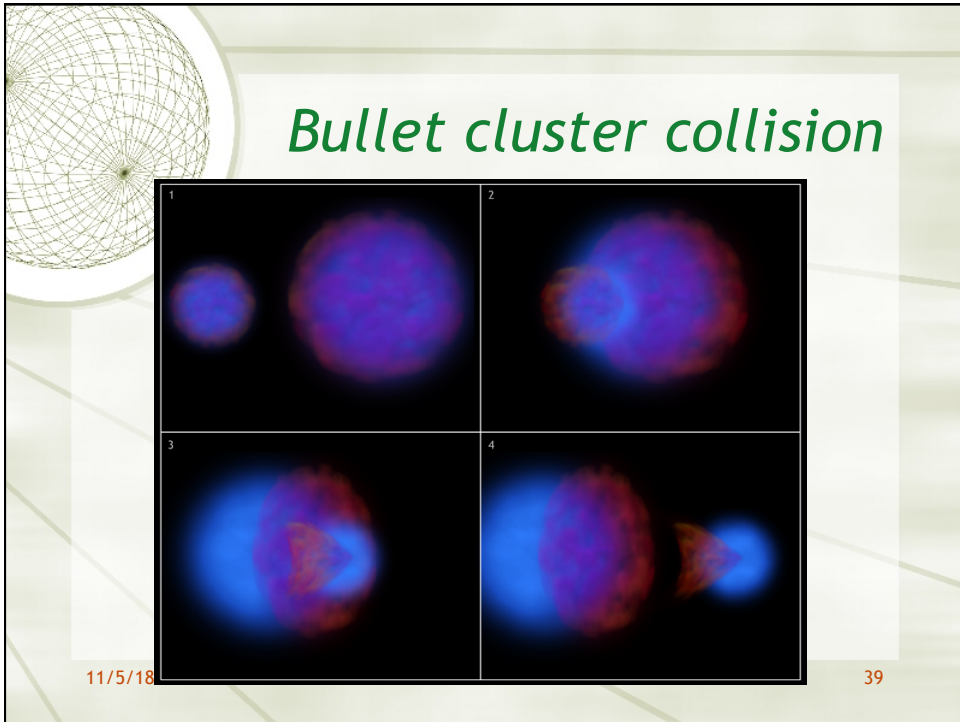
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The mass is not in the baryons

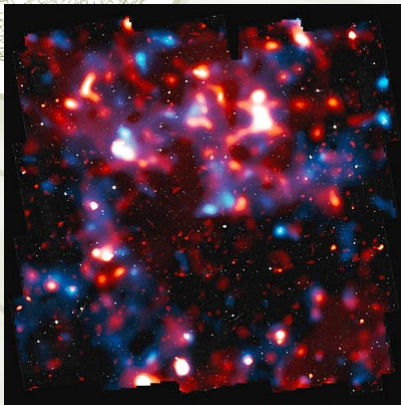


weak lensing mass contours (Clowe in prep.)
HST image

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Dark matter map from gravitational lensing from the COSMOS survey



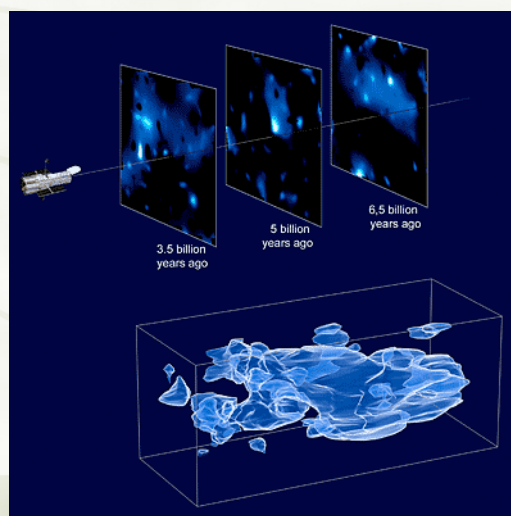
Normal matter (red) from XMM/Newton X-ray observations, dark matter (blue) from gravitational lensing, and stars and galaxies (grey) observed with Hubble.

NASA, ESA, R. Massey

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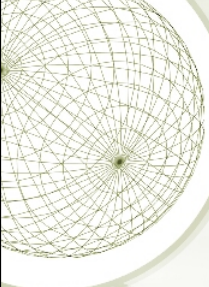
Dark matter map from gravitational lensing from the COSMOS survey



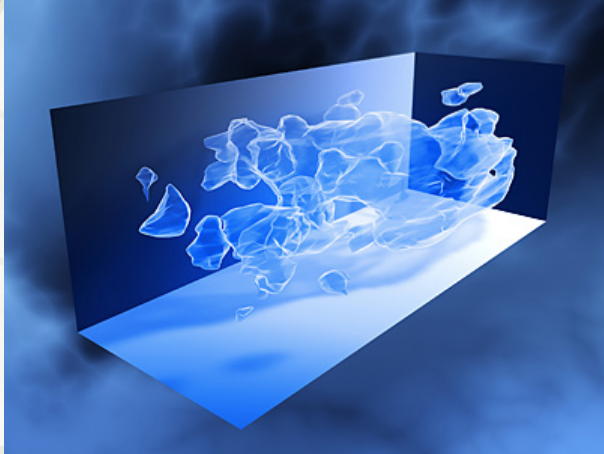
NASA, ESA,
R. Massey

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Dark matter map from the COSMOS survey



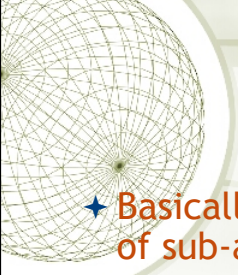
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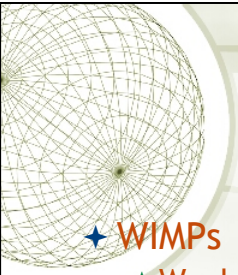
NON-BARYONIC DARK MATTER: SUMMARY

- ✦ Recap again...
 - ✦ Nucleosynthesis arguments constrain the density of baryons ($\Omega_B \approx 0.049$)
 - ✦ But there seems to be much more mass in galaxy and cluster halos (total $\Omega_{\text{Matter}} = 0.3$)
 - ✦ So, most of the matter in the Universe is not baryonic!
- ✦ what is it????
- ✦ We'll discuss candidates for non-baryonic matter later on...

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- ★ Basically, we have to appeal to other kinds of sub-atomic particles.
- ★ Neutrinos (a mundane possibility)
 - ★ Already come across neutrinos when talking about nuclear reactions
 - ★ They are part of the “standard model” of particle physics... they have been detected and studied.
 - ★ Maybe the dark matter is in the form of neutrinos?
 - ★ **No...** each neutrino has very small mass, and there just are not enough of them to make the dark mass (mass measured only very recently)



- ★ **WIMPs**
 - ★ Weakly Interacting Massive Particles
 - ★ Generic name for any particle that has a lot of mass, but interacts weakly with normal matter
 - ★ Must be massive, to give required mass
 - ★ Must be weakly interacting, in order to have avoided detection
 - ★ Various possibilities suggested by Particle Physics Theory...
 - ★ Super-symmetric particles
 - ★ Gauge bosons
 - ★ Many experiments currently on-going



Next time...

- ★ Evidence for flat universe (and Λ)
- ★ “Cosmic concordance” parameter set

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