Lecture 3: Cosmology of the Scientific Revolution

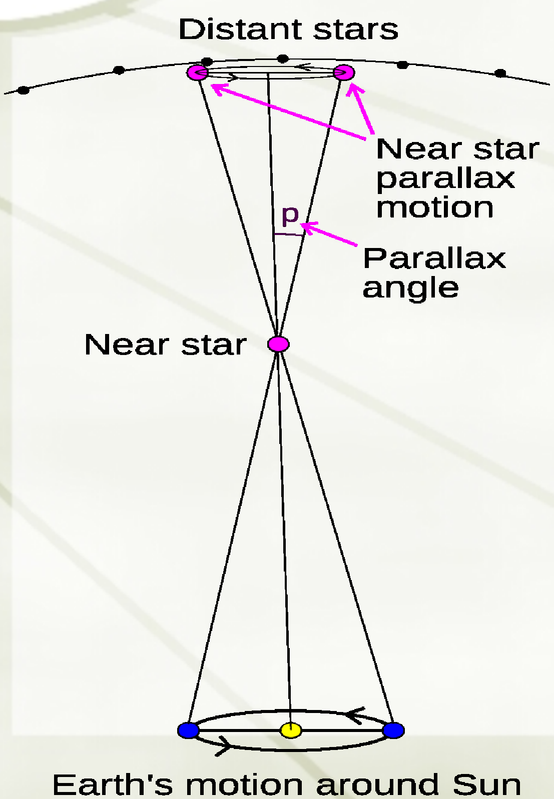
- More Tycho
- Kepler
- Galileo
- Newton
- Finish reading ch 2 and start on ch 3

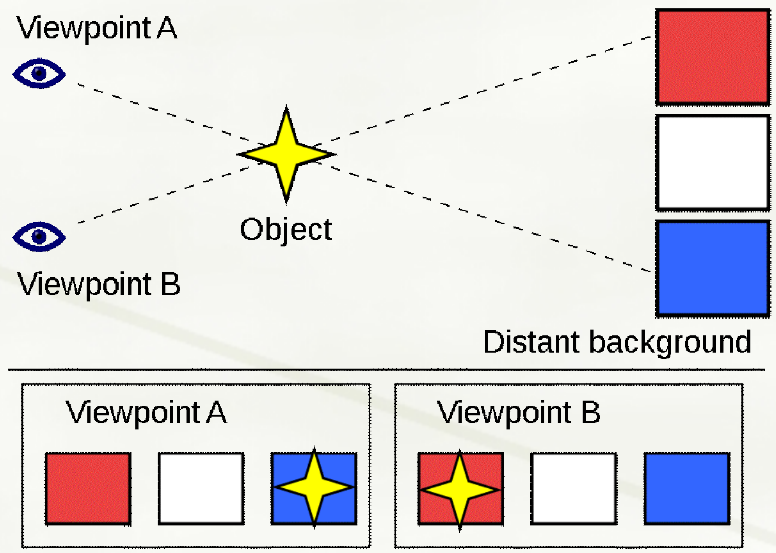
Jupiter and its 4 major (Galilean) moons

Large quadrant at Uraniborg ~2.6m in diameter- example of the advanced instrumentation Tycho used

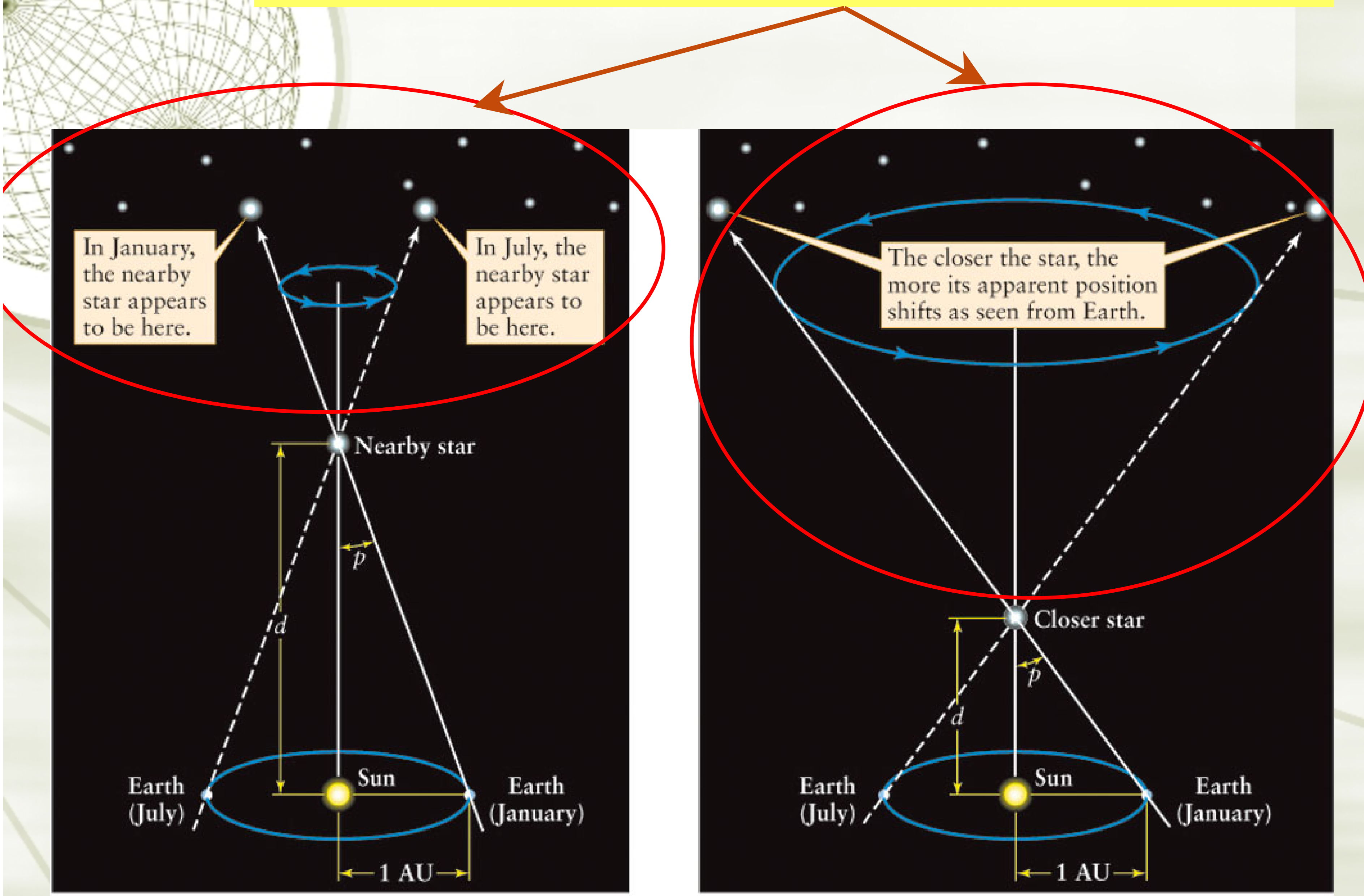
Parallax

- There are two sources of an observers motion with respect to the distant stars
  - rotation of the earth (diurnal motion)
  - rotation of the earth around the sun (annual motion)





These are projections of 3D onto 2D



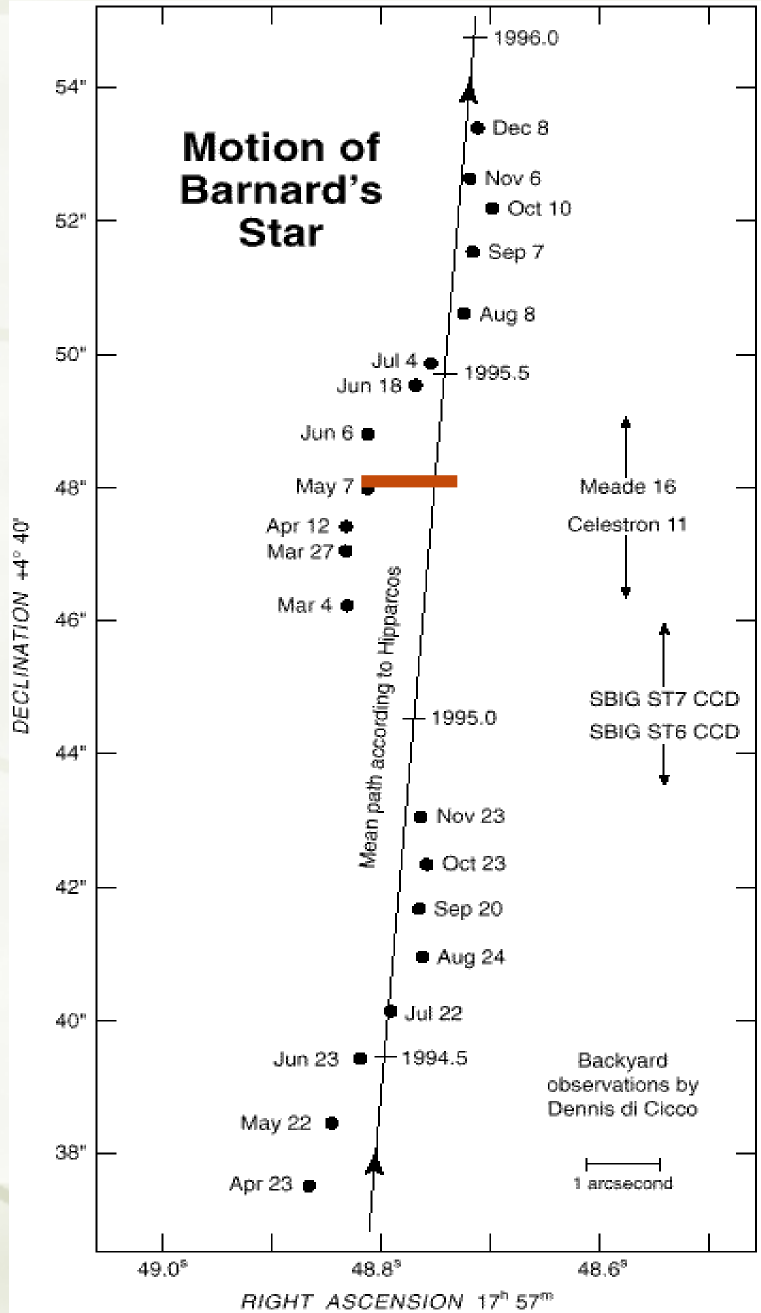
(a) Parallax of a nearby star

(b) Parallax of an even closer star

- If star "wobbles" with amplitude of 1 arc-second over 6 months then it is at distance of **1 parsec** (*definition* of parsec = parallax arcsecond).
- 1pc = 3.26 ly

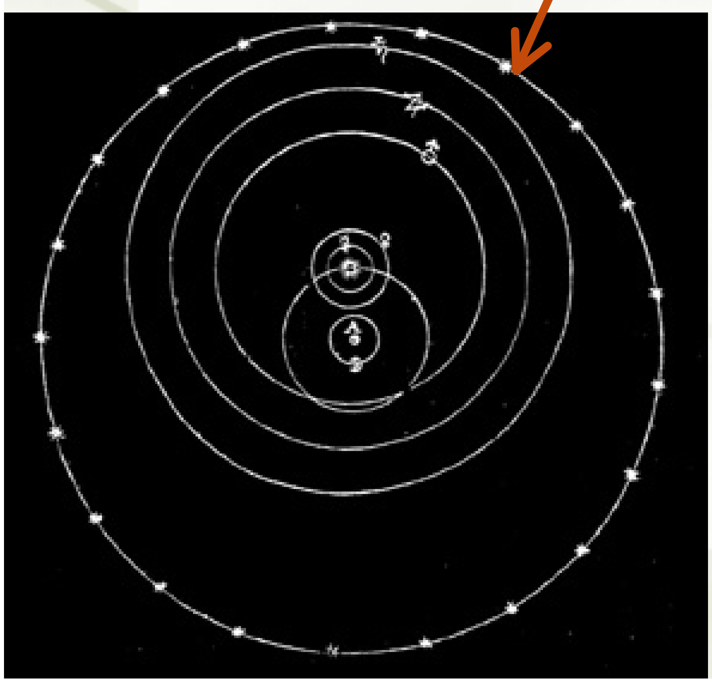
$$D(\text{pc}) = \frac{1}{\theta_{wobble}(\text{arcsec})}$$

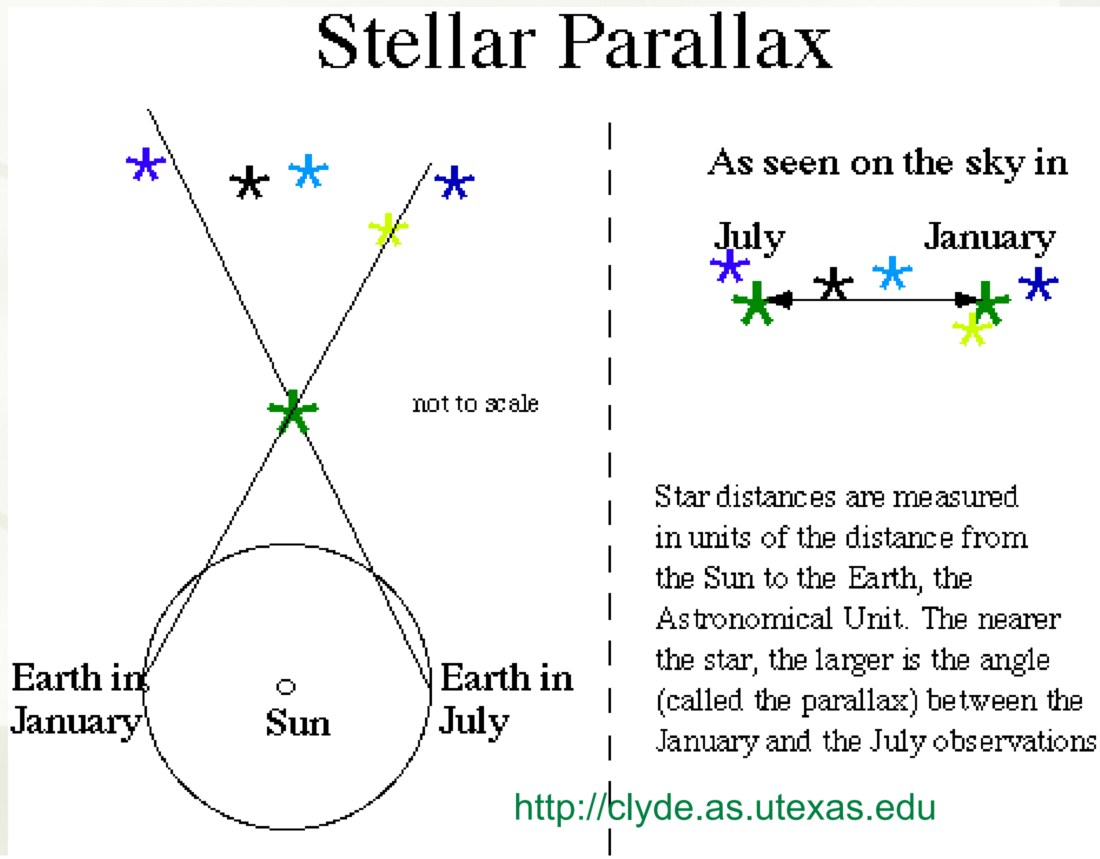
- Stars have also 'proper motion'
- **(transverse velocity)**
- Largest is for Barnard's Star
- ~10"/yr



Tycho's cosmological model

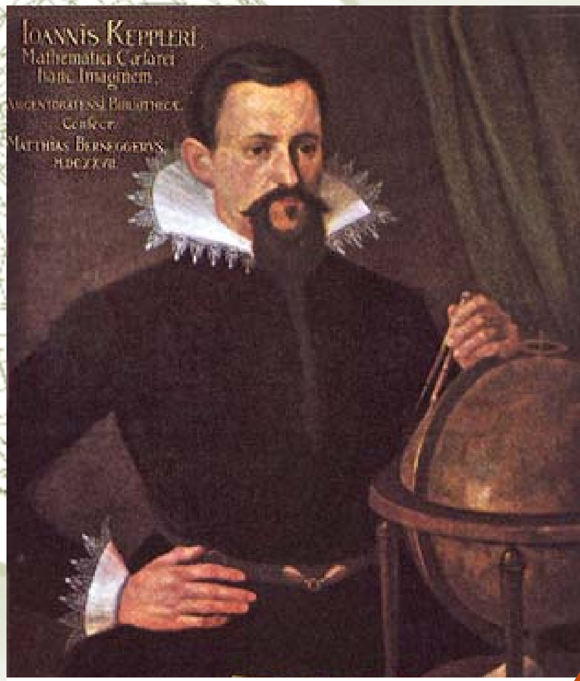
- Tycho used parallax observations to explore heliocentric model:
  - If Earth moves, then parallax of stars ***should*** be observable
  - Tycho could not detect any significant parallax; he concluded Earth is stationary
  - In fact, stellar parallax is 100× too small for naked-eye observation to measure; largest values are about 1 arcsecond=(1/3600)°
- Tycho settled on combined geo/helio-centric model
  - Sun orbits Earth; all other planets orbit Sun

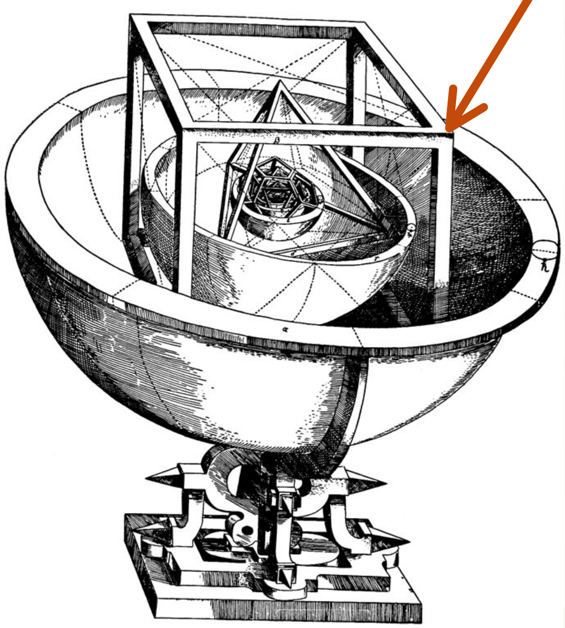




The perils of conversion factors and algebra

- ***p(arcseconds)* = 1 / *D***
- if size is in AU and distance is in parsecs. Rearranged:
- ***D(parsecs)* = 1 *AU / p(arcseconds)***
- from this we can figure out the relationship between AU and parsecs…





The Polyhedra inscribed into the planetary orbits. Kepler's drawing is a pure geometrical fancy, but it is meant to correspond to the actual relation between the radii of the planetary orbits. Most important here is the cube, fitted into the outermost sphere of Saturn.

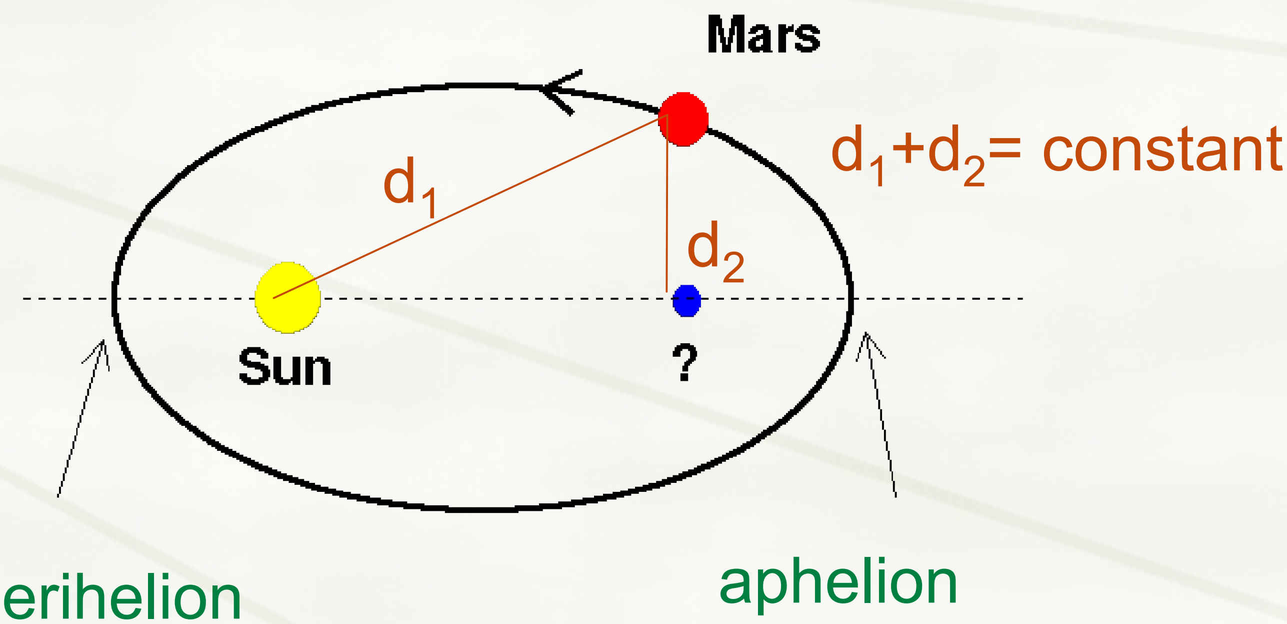
Johannes Kepler (1571-1630)

- Born in Germany; originally planned to be ordained as Lutheran minister
- Convinced God made the Universe according to a mathematical plan; saw his Christian duty as understanding works God had created
- Was hired as Tycho Brahe's assistant in Prague; his job was to make sense of Brahe's extremely accurate observations of Mars
- Let to the publication of three laws of planetary motion (1601, 1609, 1619)

http://imagine.gsfc.nasa.gov/docs/features/movies/kepler.html

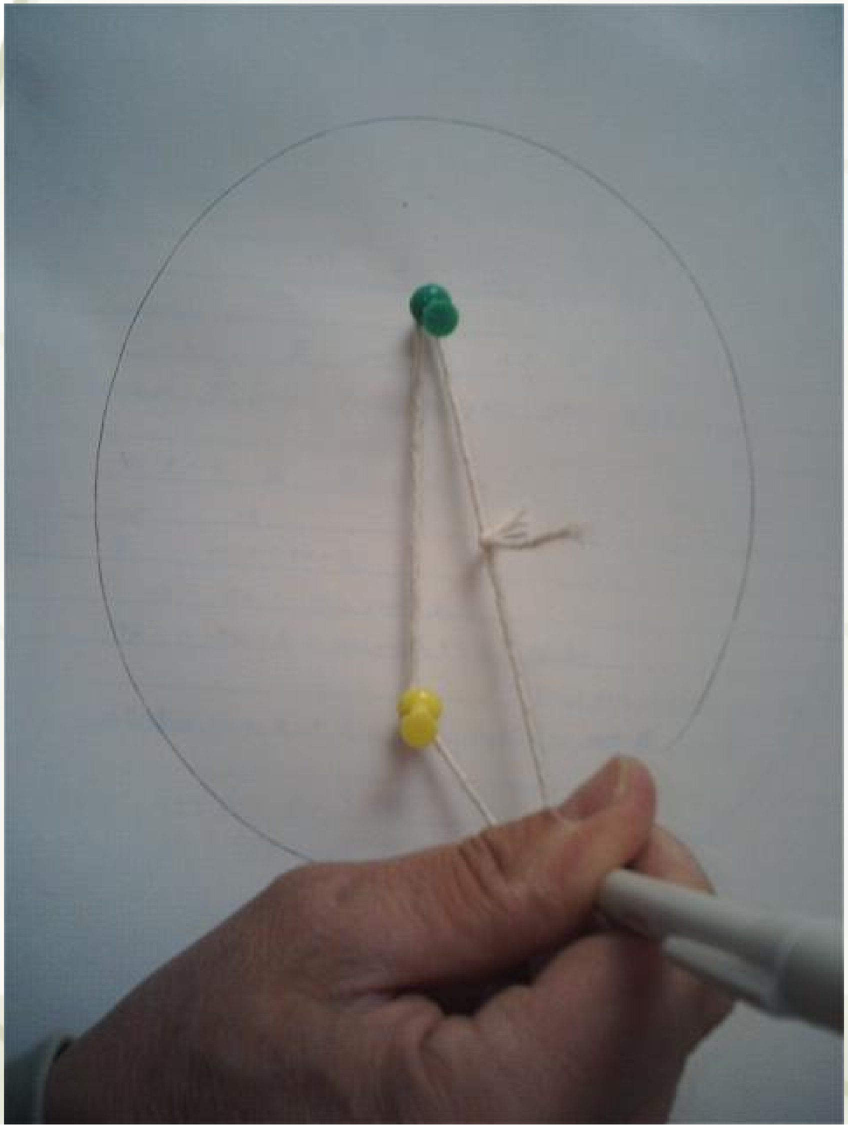
Kepler's first law

- **Planets move around the Sun in ellipses, with the Sun at one focus.**



http://www.youtube.com/watch?v=NG18fObqMV4&feature=related

Kepler's first law

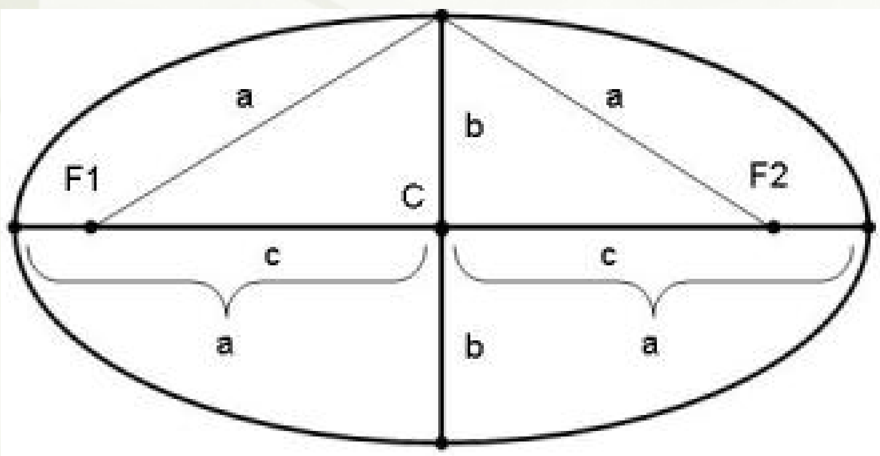


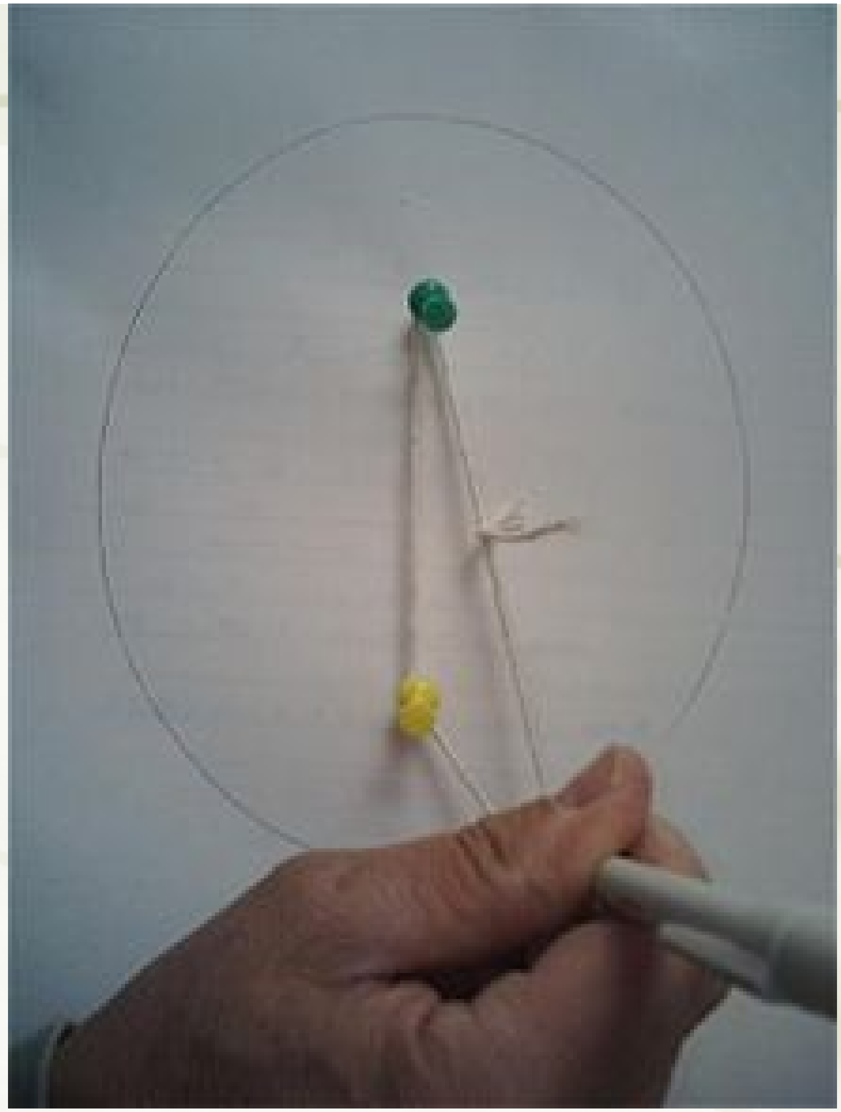
Drawing an ellipse is easy: use two tacks for the foci and a string

Ellipses

- $(x/a)^2+(y/b)^2=1$

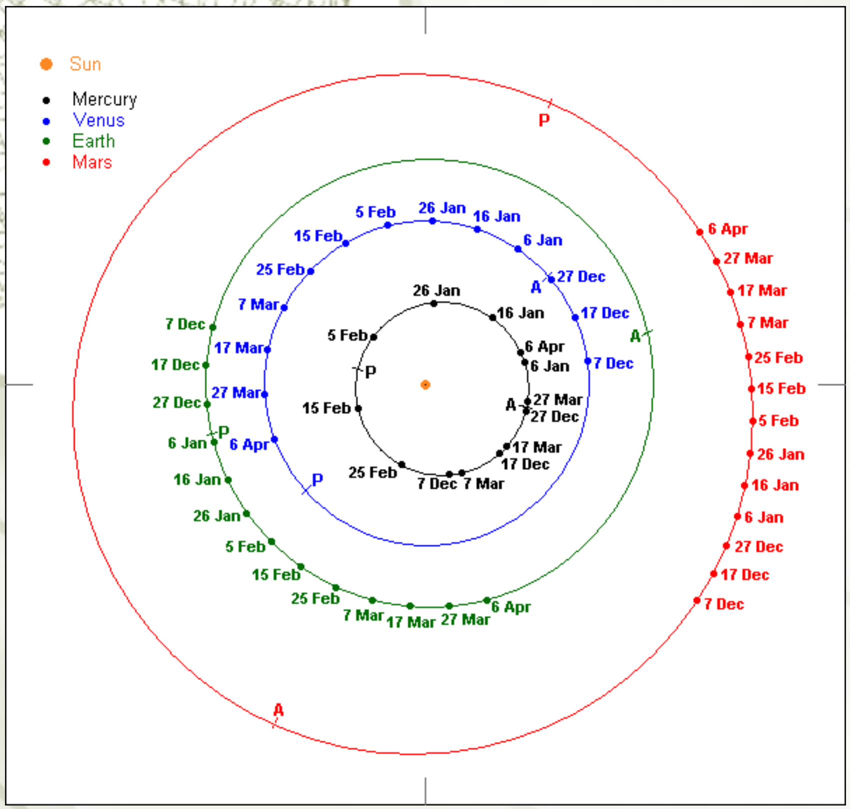
- where a is the semimajor and b the seminor axis



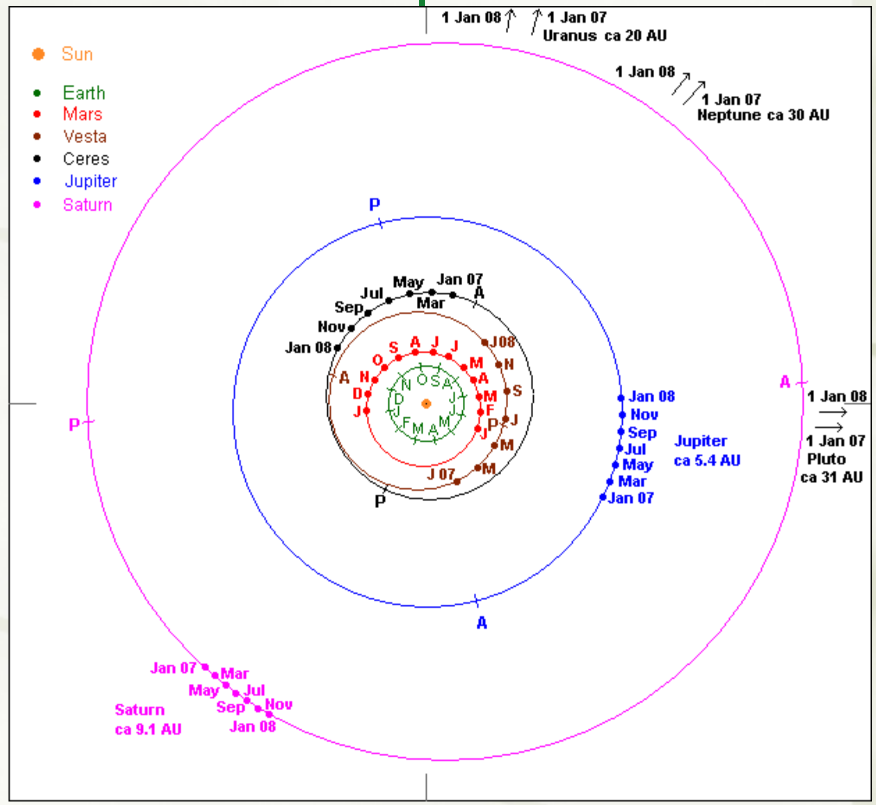


Solar system orbits

Note the low eccentricities!



Inner planets



http://www.rasnz.org.nz/SolarSys/Orbits07.htm

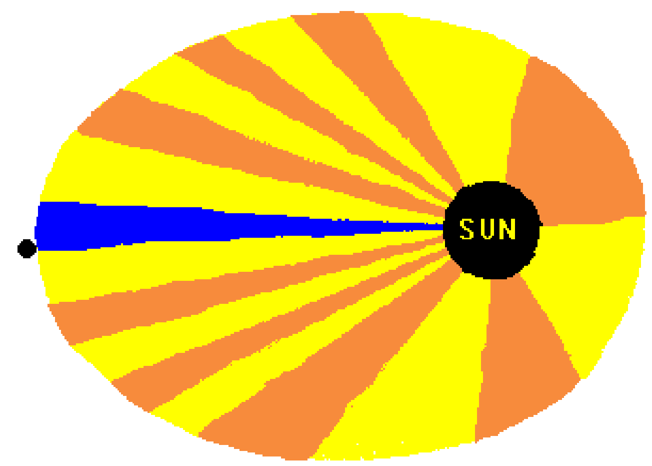
Eccentricities

Mercury	0.21	Jupiter	0.05	Pluto	0.25
Venus	0.01	Saturn	0.06	Haumea	0.19
Earth	0.02	Uranus	0.05	Makemake	0.16
Mars	0.09	Neptune	0.01	Eris	0.44

'minor planets'

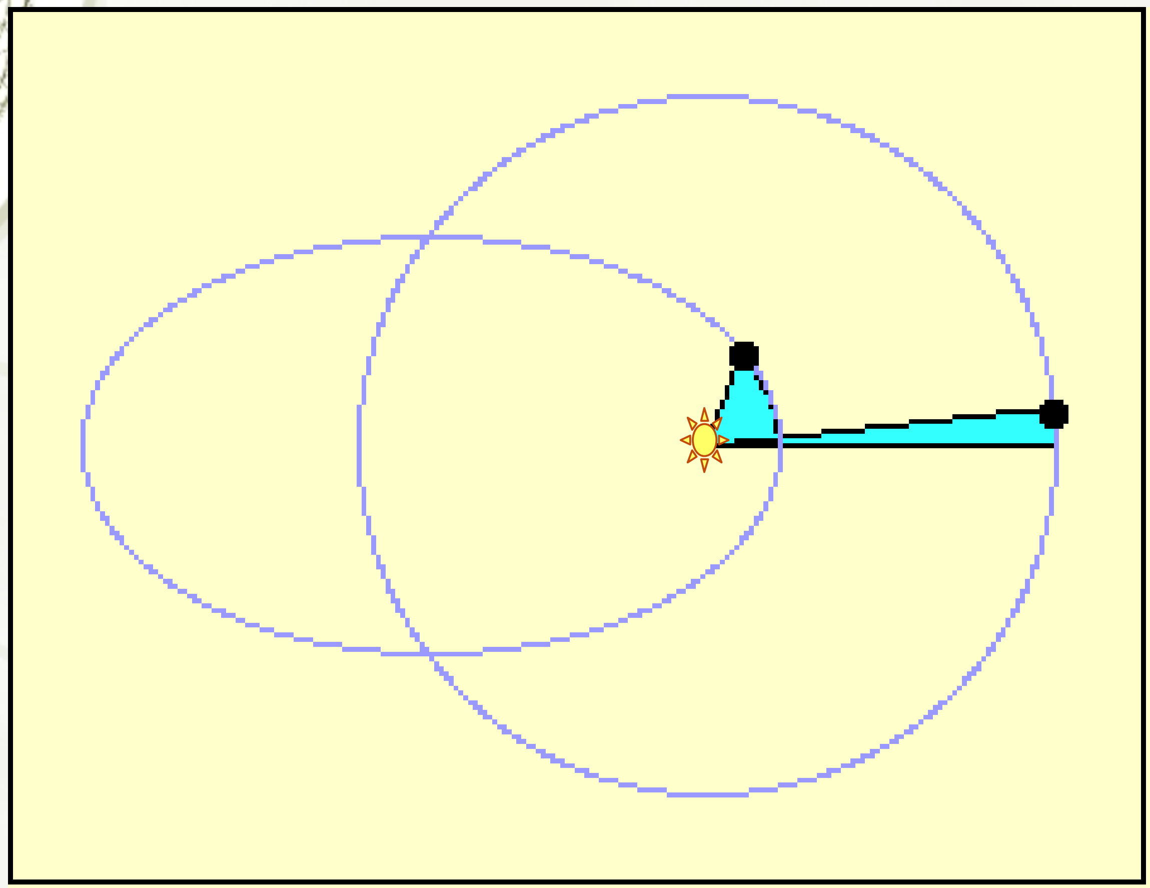
Kepler's second law

- **The line connecting the Sun and a given planet sweeps out equal areas in equal times.**
  - Therefore, planets move faster when they are nearer the Sun
  - Consequence of angular momentum conservation.



http://home.cvc.org/science/kepler.gif

Kepler's second law with high- and low- eccentricity orbits



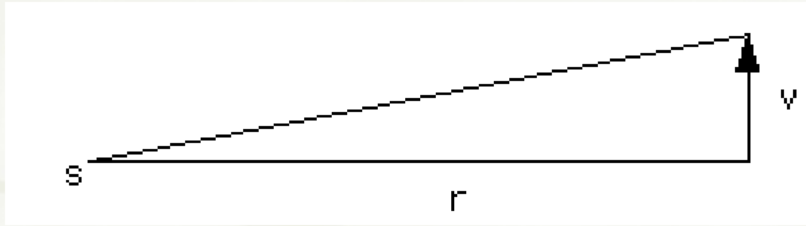
The line connecting the Sun and a given planet sweeps out equal areas (blue color) in equal times

Derivation of Kepler's 2nd Law-not on test

- Newton showed that for **any** central force, the area swept out per time will be a constant. (A central force is a force that is always pointed to a center, as the force of gravity on the earth is always pointed to the sun.)

- Why?
  - For a central force there is no sideways term (torque) and thus the angular momentum will be constant
  - **Angular momentum is defined as $\mathcal{L}$=rxmv (symbols in bold are vectors and x is the cross product).**
  - or L=rmv :r is the radius of the orbit, m is the mass of the body, and v is the velocity (for a circular orbit the velocity is always perpendicular to the radius

This will make more sense after we discuss Newton's Laws

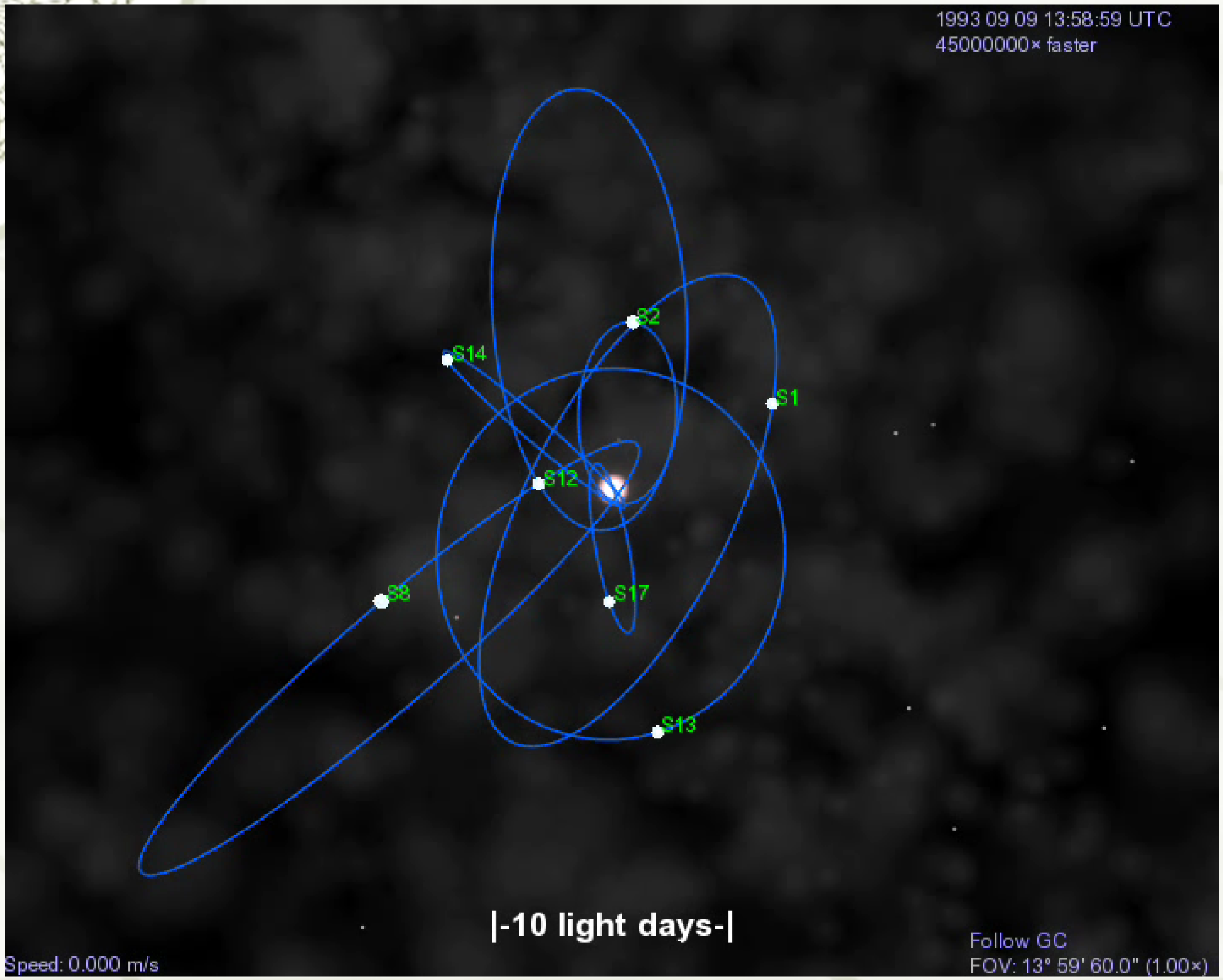


Area swept out in time t is 1/2r(vt); v is velocity, t time (area of triangles)

Put the two equations together
A=1/2L(L/m)t or
in Kepler's language
area per unit time A/t=L/2m
and
since (L/2m) is constant so is (A/t)

Time-lapse movies of orbits

Stars around the Galactic center's black hole



www.mpe.mpg.de/ir/GC/index.php

Kepler's third law- Law of Periods

- **The square of the period P of the orbit is proportional to the cube of the semi-major axis R**
- Period (P) = time it takes for planet to complete one orbit
- Semi-major axis (R) = half of the length of the "long" (i.e. major) axis of the ellipse.

$$P^2 = constant \times R^3$$

Newton determined the constant from his theory of gravity

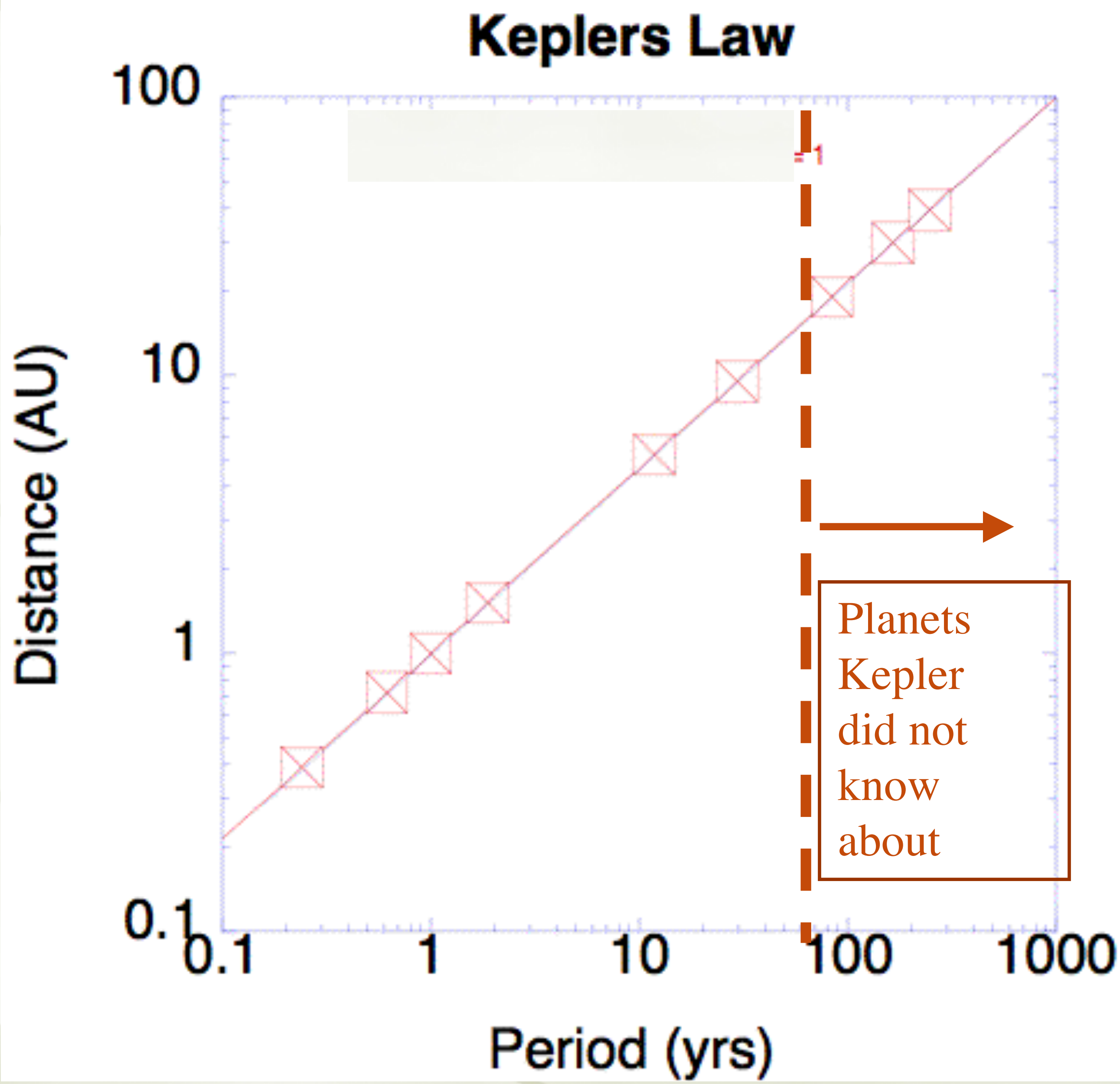
$$constant = 4\pi^2/G(M+m)$$

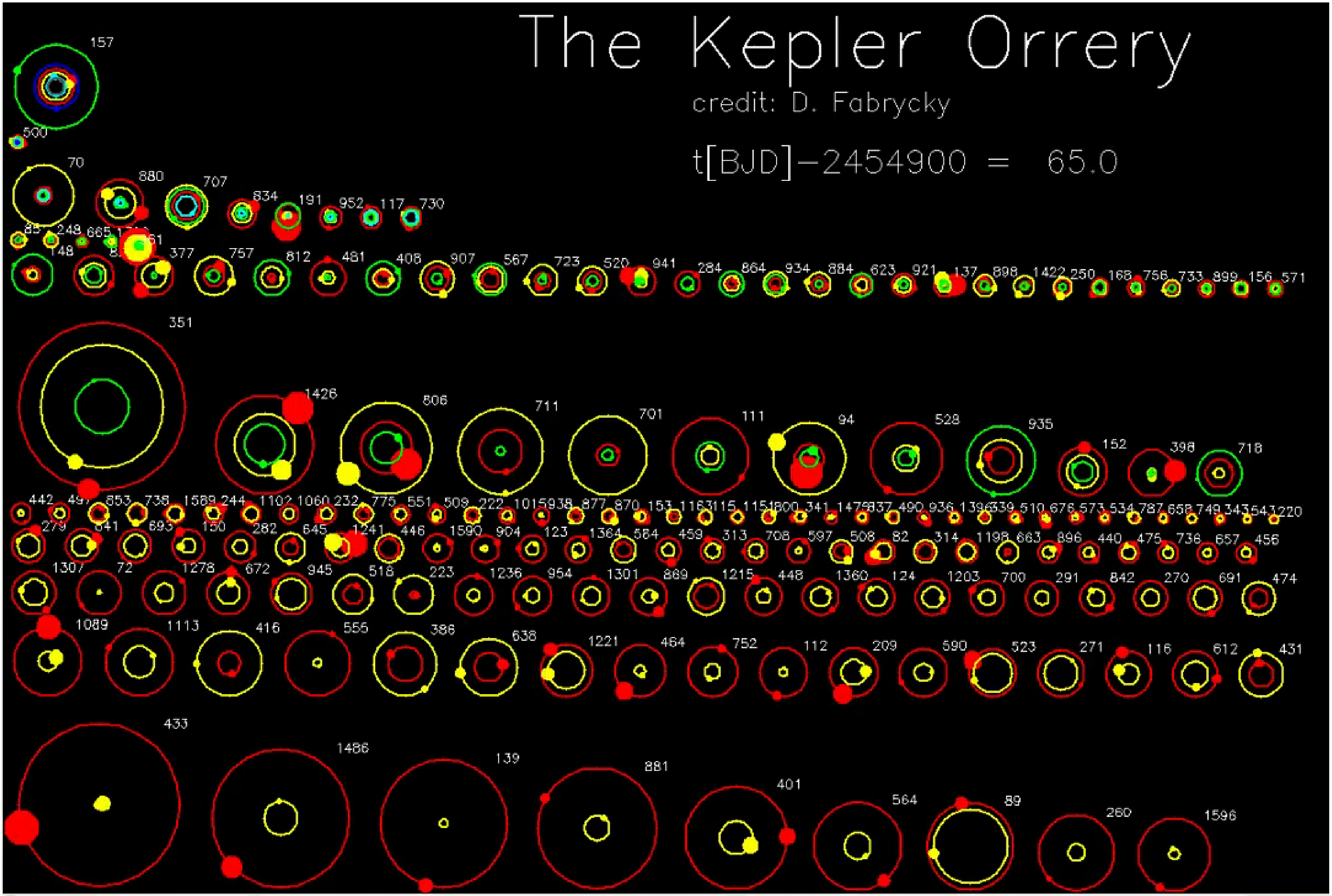
- For the Earth, we know that:
  - P= 1 year = 3.15×10^7 seconds
  - R= 149.6 million km (1 Astronomical Unit, A.U.)
- Kepler's 3rd law says that, for other planets,

$$\left(\frac{P}{yr}\right)^2 = \left(\frac{R}{AU}\right)^3$$

Kepler's 3rd Law

- Lets check that $(P/yr)^2=(R/AU)^3$
- Fitted line is Keplers law
- boxes are real planet distances and periods

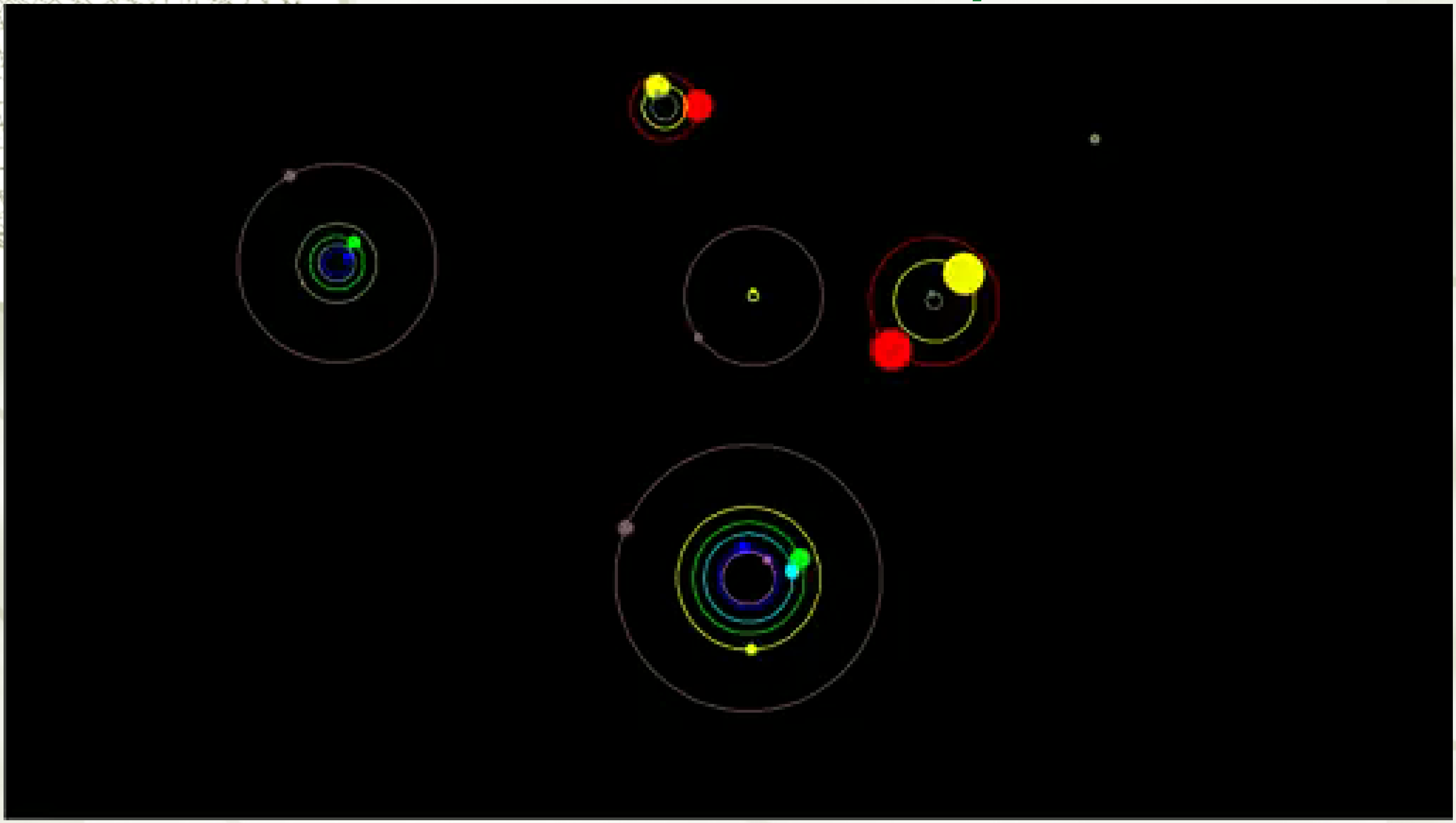




Keplers Law for the new planets discovered by Kepler satellite

http://www.dmns.org/science/museum-scientists/ka-chun-yu/random-quanta/latest-quanta/astro-kepler-orrery-movies

'New' Kepler Planets



An imprecise version of Kepler's laws

- Orbits are not circular
- A planet's speed changes during its orbit
- There is a definite relationship between orbital period and the distance from the star
- for a detailed discussion see http://www.physicsclassroom.com/class/circles/u6l4a.cfm

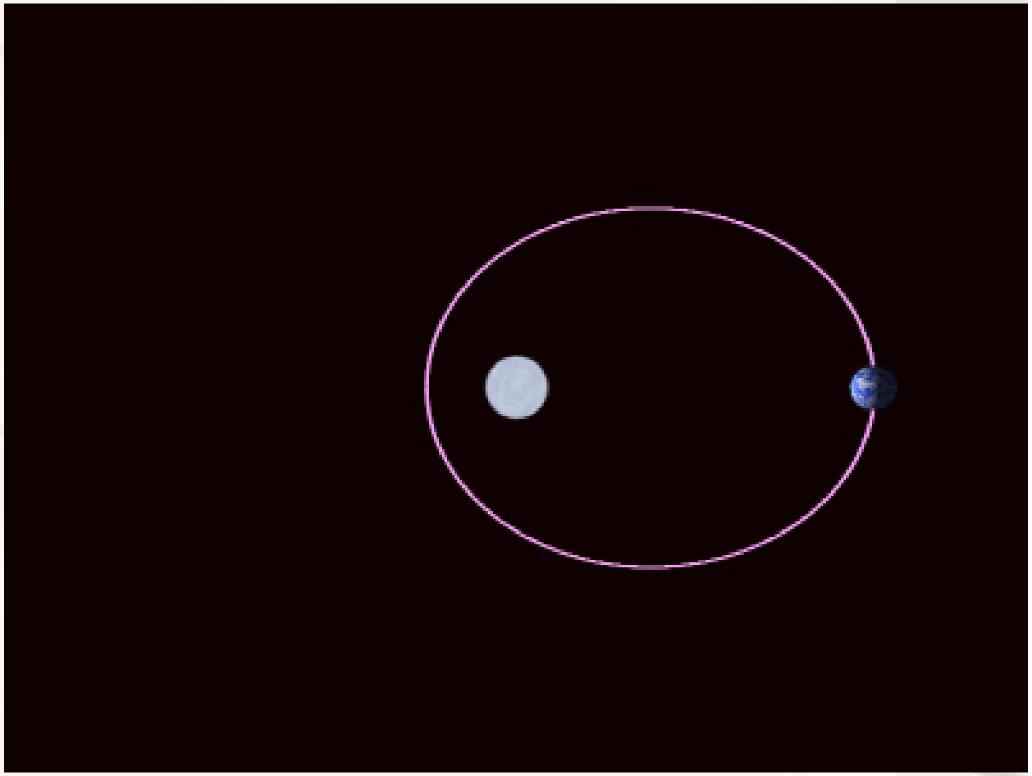
Kepler in perspective

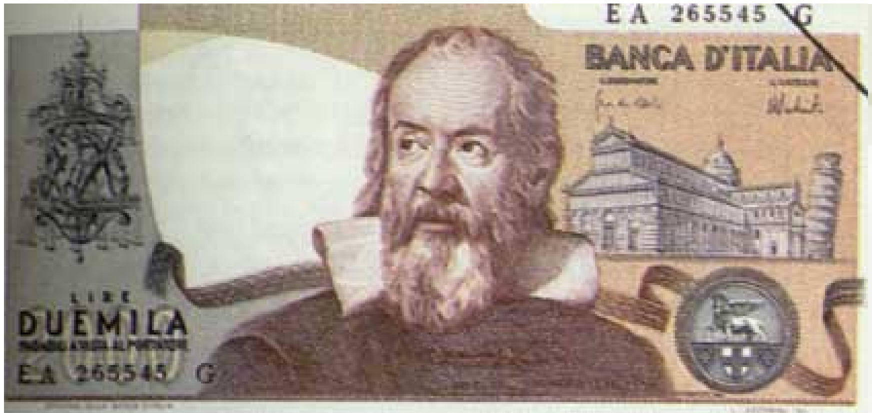
- Based on Tycho Brahe's accurate observations, Kepler calculated and thought his way to a major breakthrough in cosmology
- Kepler's three laws of planetary motion
  - Represented a very simple (and correct!) model of the solar system- and can be generalized to other similar systems
  - Swept away thousands of years of prejudice – and his own previous pet theory!
  - Were driven fundamentally by the **data**, including Tycho's error estimates
- Unlike previous models which quantified only what was observed already, Kepler's Laws had predictive power, consistent with modern idea of a meaningful scientific theory (in fact it was the deviation of Mercury from Kepler's law that was one of the observational tests of General Relativity)

A Discursion

- Keplers laws hold only if the force law is exactly $1/r^2$ - because the sun is not a perfect sphere and the other planets contribute a small amount to the total force the 'apsides' (the two points of closest and furthest distance of the orbit) precess

- However General Relativity does not have an exact $1/r^2$ force law and thus the apsides precess even if one has a perfect sphere and no other planets





Galileo Galilei (1564-1642)

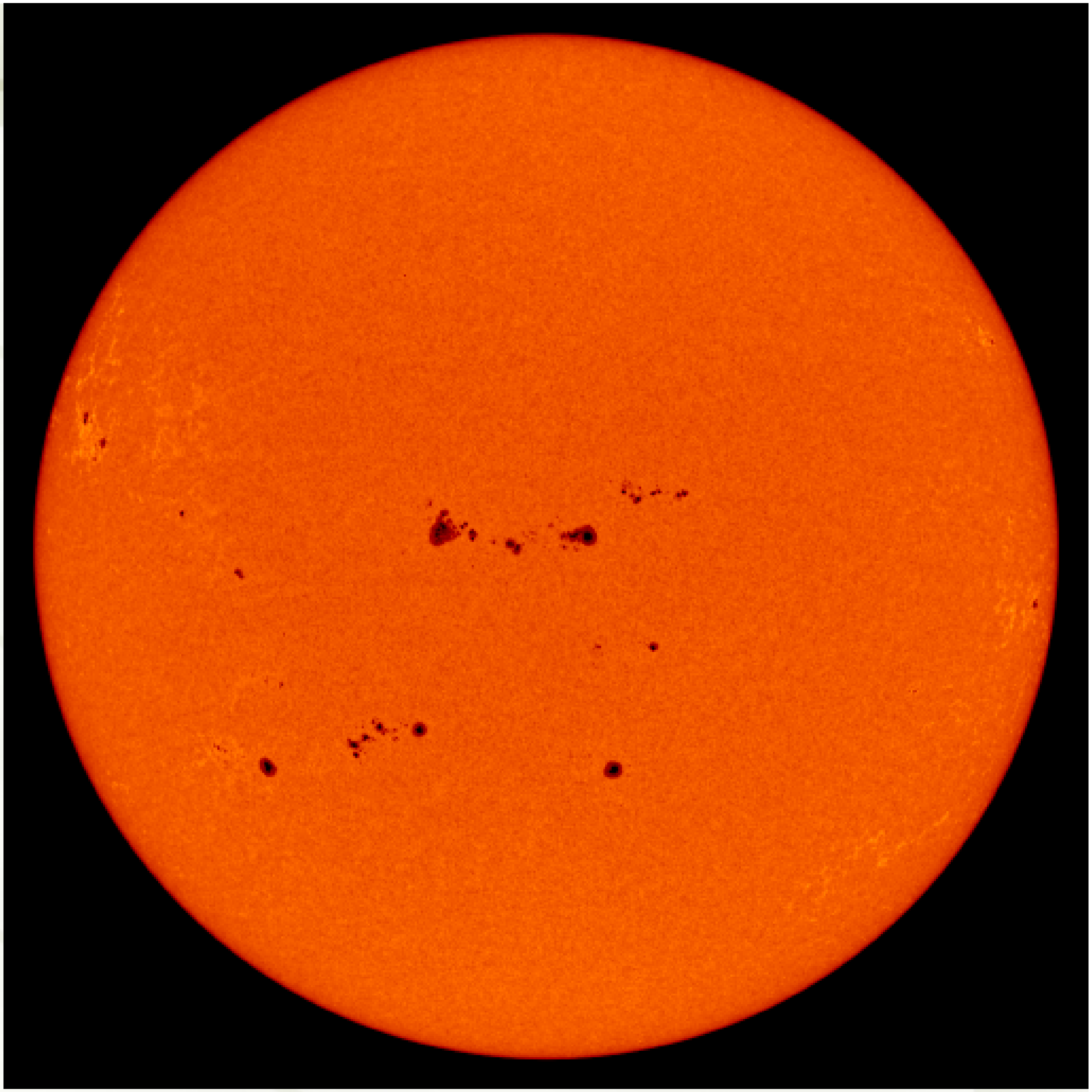
- Born in Pisa; worked as professor of mathematics
- Built one of the first telescopes in 1609
- Published *"The Starry Messenger"* with first telescopic discoveries in 1610
- Telescopic observations: the objects in the sky were not perfect
  - Saw craters and mountains on the Moon
  - Realized sunspots were on surface, not foreground and rotated with Sun
  - Identified four satellites of Jupiter ("Galilean moons")
  - Saw rings of Saturn
  - Resolved the diffuse Milky Way into many faint stars
  - Observed phases of Venus including gibbous (between full and half) and full

Moon is not smooth, but covered by mountains and craters.

http://www.astromax.org

Galileo observed motion of the sunspots indicating that the Sun was rotating on an axis. The spots showed that doctrine of an unchanging perfect substance in the heavens and the rotation of the Sun made it less strange that the Earth might rotate on an axis .

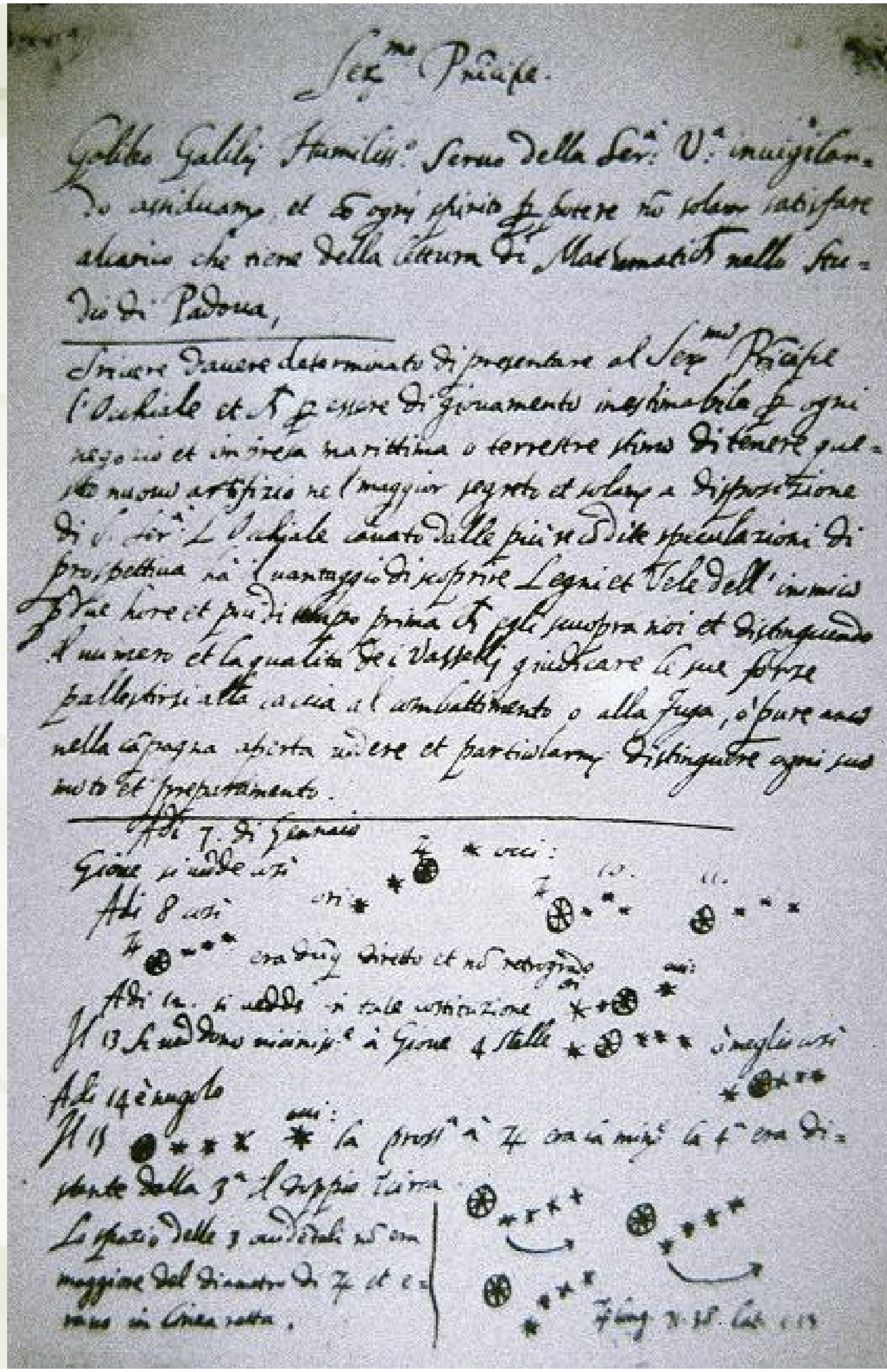
Both were **new** facts made possible by the telescope and thus were unknown to Aristotle and Ptolemy



Galielo's telescope was so famous it was used for the international year of astronomy in 2009 the 400th anniversary of the astronomical telescope

http://www.telescope1609.com/Galileo.htm

Letter from Galileo reporting the discovery of Jupiter's moons… documentation of his discovery



SIDEREUS NUNCIUS 75

On the third, at the seventh hour, the stars were arranged in this sequence. The eastern one was 1 minute, 30 seconds from Jupiter; the closest western one 2 minutes; and the other western one was

East * O * * West

10 minutes removed from this one. They were absolutely on the same straight line and of equal magnitude.

On the fourth, at the second hour, there were four stars around Jupiter, two to the east and two to the west, and arranged precisely

East * * O * * West

on a straight line, as in the adjoining figure. The easternmost was distant 3 minutes from the next one, while this one was 40 seconds from Jupiter; Jupiter was 4 minutes from the nearest western one, and this one 6 minutes from the westernmost one. Their magnitudes were nearly equal; the one closest to Jupiter appeared a little smaller than the rest. But at the seventh hour the eastern stars were only 30 seconds apart. Jupiter was 2 minutes from the nearer eastern

East ** O * * West

one, while he was 4 minutes from the next western one, and this one was 3 minutes from the westernmost one. They were all equal and extended on the same straight line along the ecliptic.

On the fifth, the sky was cloudy.

On the sixth, only two stars appeared flanking Jupiter, as is seen

East * O * West

in the adjoining figure. The eastern one was 2 minutes and the western one 3 minutes from Jupiter. They were on the same straight line with Jupiter and equal in magnitude.

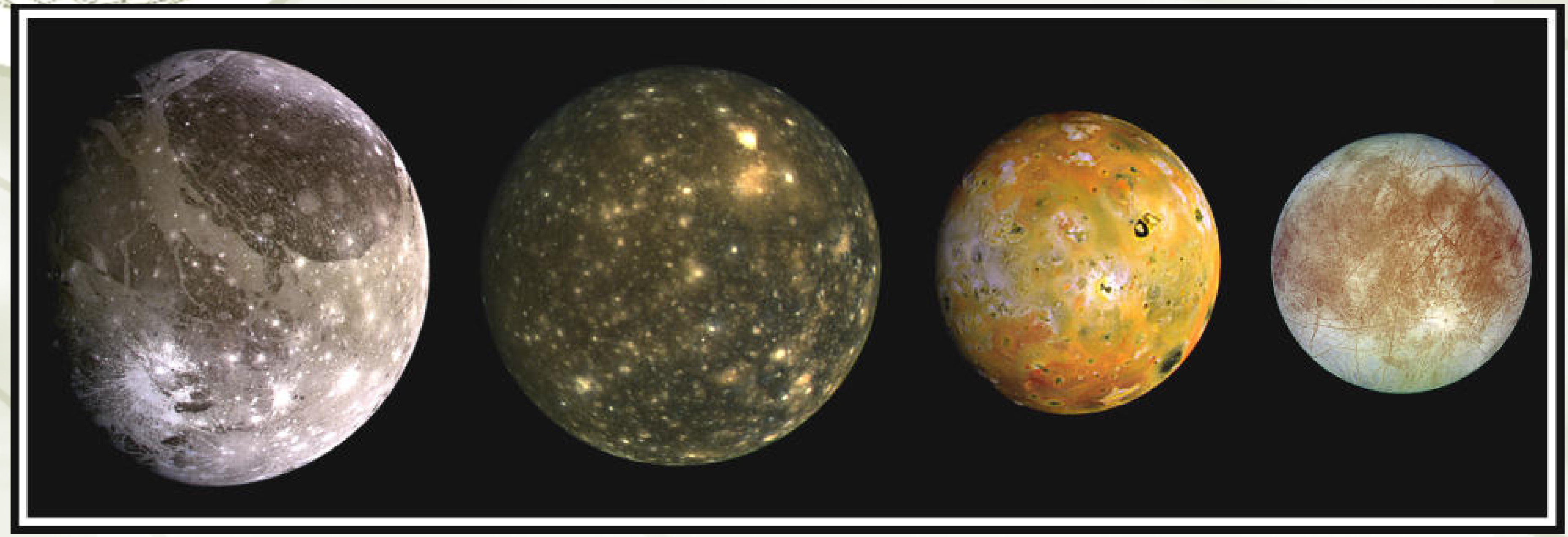
On the seventh, two stars stood near Jupiter, both to the east, arranged in this manner.

Galilean Moons

http://www.ladeltascience.com/astronomy/kisatchie04/

demonstrated that a planet could have moons circling it

Galilean moons (from Galileo spacecraft!)



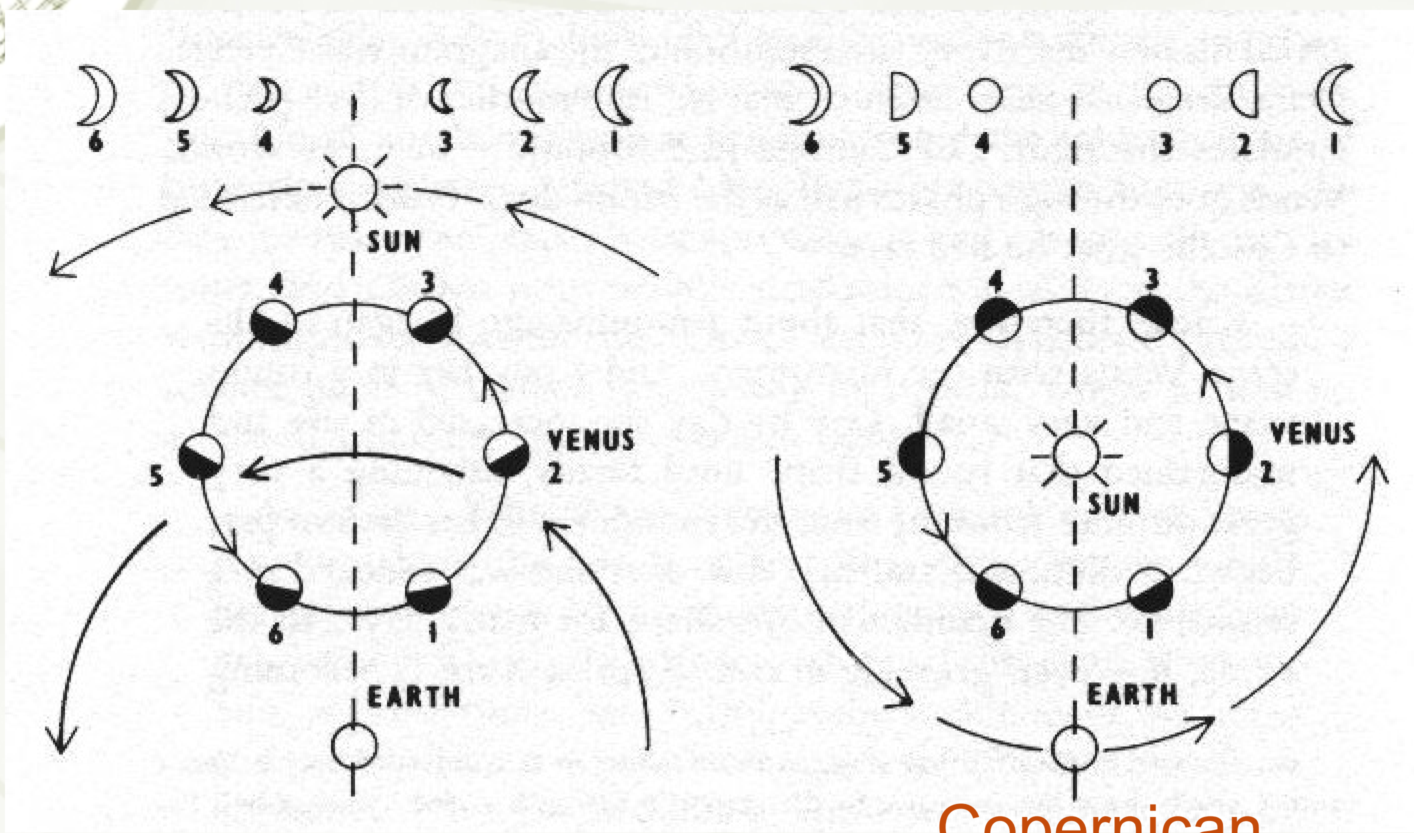
NASA

Impact of Galileo's observations

- Chipping away at Aristotelian point of view:
  - Features on Sun, Moon, Saturn indicated they are not perfect orbs
  - Faint stars resolved in Milky Way indicates stars at many distances -- not just single sphere
  - Moons of Jupiter showed that Earth was not sole center of motion
- Crucial experiment ruling out Ptolemaic model:
  - Possible phases of Venus in Ptolemaic model are only crescent or new -- but Galileo *observed full phase*
  - Observation supported Copernican (or Tycho's) model (Venus on far side of Sun when full)
- As a result of his observations, Galileo became ardent supporter of Copernican viewpoint
- In 1632, published *Dialogue Concerning the Two Chief Systems of the World - Ptolemaic and Copernican;* the Inquisition banned the book; Galileo was found guilty of heresy in supporting Copernican view, and sentenced to house arrest

Phases of Venus: a test of the Heliocentric system

In the heliocentric model Venus can show certain phases impossible if the sun goes around the earth.



Ptolemaic

Copernican

http://www.telescope1609.com/Galileo.htm

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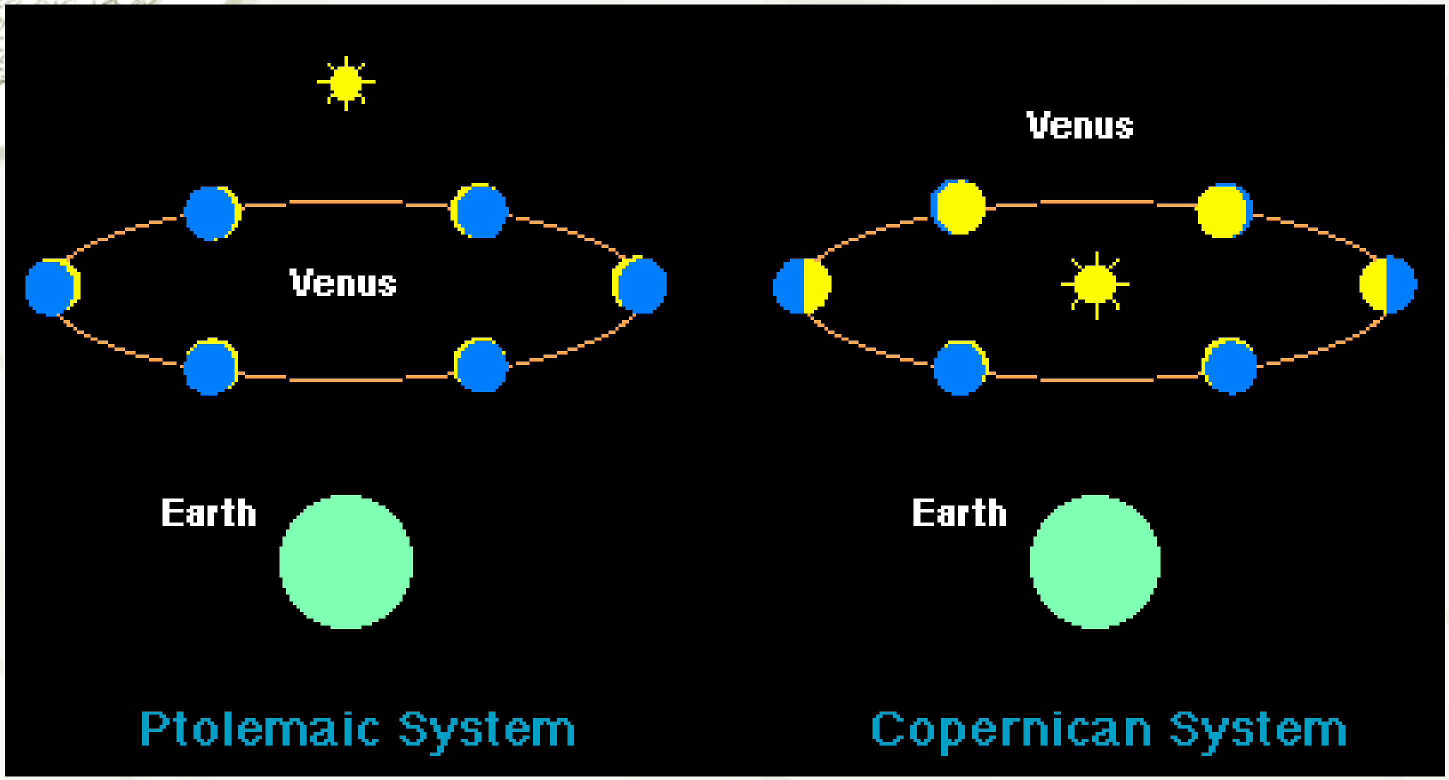


http://csep10.phys.utk.edu/astr161/lect/history/galileo.html

Galilean physics

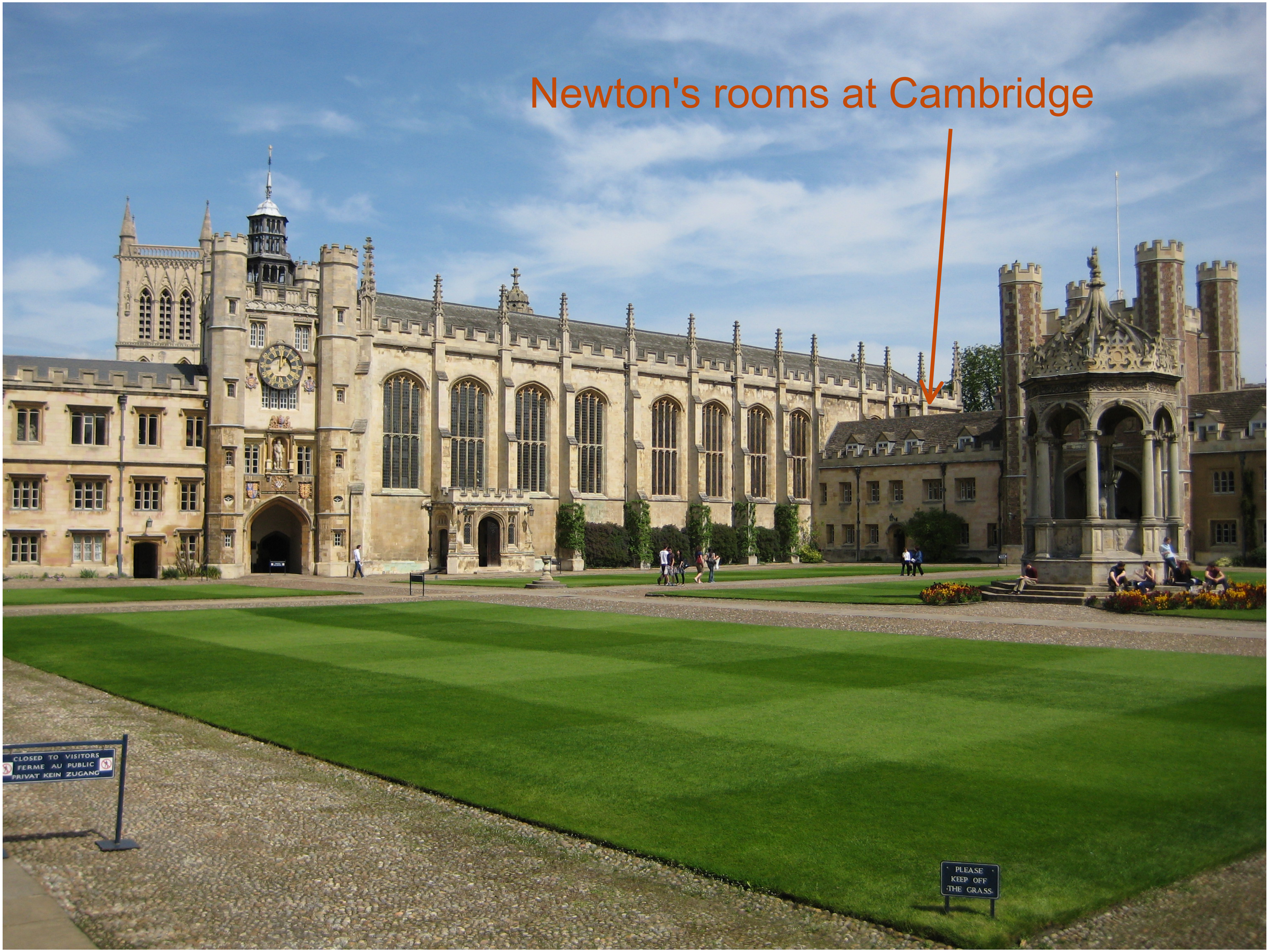
- After 1633 trial, Galileo returned to work on physics of mechanics
- Published *Discourses and mathematical demonstrations concerning the two new sciences (1642)*
- Made experiments with inclined planes; concluded that distance d traveled under uniform acceleration a is $d=at^2$
- Used "thought experiments" to conclude that all bodies, regardless of mass, fall at the same rate in a vacuum --contrary to Aristotle
  - Now known as "equivalence principle"
- Realized full principle of inertia:
  - body at rest remains at rest;
  - body in motion remains in motion (force *not* required)
- Realized principle of relative motion ("Galilean invariance"):
  - If everything is moving together at constant velocity, there can be no apparent difference from case when everything is at rest.
  - Ball dropped from top of moving ship's mast hits near bottom of mast, not behind on deck.

Isaac Newton in 1689, by Sir Godfrey Kneller.

Father of modern physics and cosmology

Isaac Newton (1643-1727)

- Attended Cambridge University, originally intending to study law, but reading Kepler, Galileo, Descartes
- Began to study mathematics in 1663
- While Cambridge was closed due to plague (1665-1667), Newton went home and
  - began to work out foundations of calculus
  - realized (contrary to Aristotle) that white light is not a single entity, but composed of many colors
  - began to formulate laws of motion and law of gravity
- Became professor of mathematics starting in 1669 (age 27!)
- Worked in optics, publishing “Opticks” (1704)
  - invented reflecting telescope
  - showed color spectrum from prism recombines into white light with a second prism
  - analyzed diffraction phenomenon


Newton's rooms at Cambridge
CLOSED TO VISITORS
FERME AU PUBLIC
PRIVAT KEIN ZUGANG
PLEASE
KEEP OFF
THE GRASS

Newton's history, cont.

- In 1687, published *Philosophiae naturalis principia mathematica,* or *"Principia"*
  - publication was prompted (and paid for) by Halley (of comet fame)
  - partly in response to claim by Hooke that he could prove gravity obeyed inverse-square law
  - included proof that inverse square law produces ellipses
  - generalized Sun's gravity law to universe law of gravitation: *all matter attracts all other matter with a force proportional to the product of their masses and inversely proportional to the square of the distance between them*
  - many other applications, including tides, precession, etc.
  - laid out general physics of mechanics -- laws of motion
  - showed that Kepler's laws follow from more fundamental laws
- The *Principia* is recognized as the greatest scientific book ever written!
- Retired from research in 1693, becoming active in politics and government

For next time- Newton and Newtons Laws

- Finish reading ch 2 - we have started on ch 3 of the text.