

GALAXY ZOO: OBSERVING SECULAR EVOLUTION THROUGH BARS*

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ABSTRACT

In this paper, we use the Galaxy Zoo 2 dataset to study the behavior of bars in disk galaxies as a function of specific star formation rate (SSFR), and inner galactic structure, i.e., the prominence of the bulge as parameterized by Sérsic index and central surface stellar mass density. Our sample consists of 13,295 disk galaxies, with an overall bar fraction of $23.6 \pm 0.4\%$, of which 1,154 barred galaxies also have bar length measurements. These samples are the largest ever used to study the role of bars in disk galaxy evolution. We find that the likelihood of a galaxy hosting a bar is anti-correlated with SSFR, regardless of stellar mass or bulge prominence. We find that the trends of bar likelihood with bulge prominence are bimodal with SSFR, i.e., in star-forming galaxies, bulges are more prominent in galaxies more likely to host bars, while in quiescent disk galaxies, bars are less frequent where there are prominent bulges. Our observations of bar length reveal a complex picture. In star-forming disks, longer bars are found where the bulges are more prominent, while in quiescent disks there is a maximum in the average bar length as a function of bulge prominence. We interpret these observations using state-of-the-art simulations of bar evolution which include live halos and the effects of gas and star formation. We suggest our observed trends of bar likelihood with SSFR are driven by the gas fraction of the disks; a factor demonstrated to significantly retard both bar formation and evolution in models. We interpret the bimodal relationship between bulge prominence and bar properties as due to the complicated effects of classical bulges and central mass concentrations on bar evolution, and also to the growth of disky pseudobulges by bar evolution. These results represent empirical evidence for secular evolution driven by bars in disk galaxies. This work suggests that bars are not stagnant structures within disk galaxies, but are a critical evolutionary driver of their host galaxies in the local universe ($z < 1$).

Subject headings: galaxies: bars — galaxies: evolution — galaxies: central structure — galaxies: secular evolution

1. INTRODUCTION

Stellar bar-shaped structures within galaxies, or more simply ‘bars’, have been known to exist since the days of Edwin Hubble. With only the 100 inch telescope at Mount Wilson, Hubble accurately surmised that bars were abundant in the local universe. So abundant, that he devoted a major part of his classification scheme, the Hubble sequence of galax-

ies (Hubble 1936), to barred galaxies. Decades later, infrared and optical studies have confirmed that many galaxies have bars. Indeed, among local disk galaxies, as many as two thirds are barred (e.g., Mulchaey & Regan 1997; Knapen et al. 2000; Eskridge et al. 2000; Kormendy & Kennicutt 2004; Menéndez-Delmestre et al. 2007; Sheth et al. 2008).

Bars have an important influence on galaxy evolution. The presence of bars has been linked to the existence of spiral arms, rings (Sanders & Huntley 1976; Simkin et al. 1980; Schwarz 1981), and/or disky pseudobulges¹² (Kormendy & Kennicutt 2004; Athanassoula 2005). Bars have also been associated with an increase in central star formation (Hawarden et al. 1986; Dressel 1988; Giuricin et al. 1994; Huang et al. 1996; Martinet & Friedli 1997; Martin & Friedli 1997; Ho et al. 1997; Ellison et al. 2011; Oh et al. 2012; Wang et al. 2012), the flattening of galactic chemical abundance gradients (Vila-Costas & Edmunds 1992; Zaritsky et al. 1994; Martin & Roy 1994; Williams et al. 2012), and, perhaps, active galactic nuclei (AGN) activity (Noguchi 1988; Shlosman et al. 1989; Laine et al. 2002; Martini et al. 2003; Jogee 2006; Hao et al. 2009; Oh et al. 2012).

Given that bars have an important influence on galaxy evolution, two natural questions are “how do bars form and evolve?” and “how do they affect their host galaxies?” A re-

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¹² Bulges created through secular evolution have been called both “pseudobulges” and/or “disky bulges”. For completeness, we will use the term “disky pseudobulges” throughout to represent such bulges in galaxies.

view of the theoretical work on bars is given by Athanassoula (2012), so we will only summarize here the parts that are most relevant to this work. Many past theoretical works have shown that bars can redistribute the angular momentum of the baryons and dark matter of a galaxy (e.g., Sellwood 1980; Debattista & Sellwood 2000). The angular momentum is emitted mainly by stars at (near-)resonance in the bar region and absorbed mainly by (near-)resonant material in the spheroid (i.e., the halo and, whenever relevant, the bulge) and in the outer disk (Lynden-Bell & Kalnajs 1972; Tremaine & Weinberg 1984; Athanassoula 2003, hereafter A03).

A03 showed that the redistribution of angular momentum is not merely a side-effect of bars, but is, instead, a process that is closely coupled to the evolution of bars. Specifically, the exchange of angular momentum from the inner disk to the outer disk and/or spheroid (bulge/halo) is the main driver of bar evolution. The efficiency of the angular momentum exchange is primarily dependent upon the mass distribution and velocity dispersion of the disk and spheroid. More angular momentum can be redistributed if the spheroid mass density at the location of the resonances is high, leading to stronger bars (A03). The second factor governing the efficiency of angular momentum exchange is the velocity dispersion. In lower velocity dispersion (lower temperature) disks and spheroids, resonances can emit or absorb more angular momentum than in cases with high velocity dispersion, thereby making the transfer of angular momentum more efficient (A03; Sheth et al. 2012).

This redistribution of angular momentum allows bars to drive gas, and to a lesser extent, stars, to the centers of galaxies (Matsuda & Nelson 1977; Simkin et al. 1980; Athanassoula 1992; Wada & Habe 1992, 1995; Friedli & Benz 1993; Heller & Shlosman 1994; Knapen et al. 1995; Sakamoto et al. 1999; Sheth et al. 2005). This process is responsible for the increase of bar length and strength and of the disk scale length (e.g., Hohl 1971, Debattista & Sellwood 2000, A03, O’Neill & Dubinski 2003, Valenzuela & Klypin 2003, Debattista et al. 2006, Martinez-Valpuesta et al. 2006, Minchev et al. 2011), the formation of a disky pseudobulge (Kormendy & Kennicutt 2004; Athanassoula 2005), the increase of central star formation (Friedli & Benz 1993; Martinet & Friedli 1997; Martin & Friedli 1997), and the dilution of abundance gradients (Friedli et al. 1994; Friedli & Benz 1995; Martel et al. 2013). This process is known as secular evolution (Kormendy & Kennicutt 2004; Kormendy 2012).

It has been shown that bar formation and evolution is also dependent on the gas content in the galaxy (e.g., Shlosman & Noguchi 1993; Berentzen et al. 1998, 2007; Villa-Vargas et al. 2010). More recent simulations – with a multi-phase description of the gas, including star formation, feedback and cooling, and a sufficiently large number of particles to describe adequately the gas flow – have shown that bars form later in simulations with a larger gas fraction (Athanassoula et al. 2013, hereafter AMR13).

Recent observational works have begun to test many of these predictions. For example, Masters et al. (2011) used classifications from Galaxy Zoo 2 (see §2.2), to show that the fraction of disk galaxies that possess a bar (bar fraction) increases in redder disk galaxies (see also Skibba et al. 2012). This result was confirmed by Lee et al. (2012), who also used a large sample of galaxies from the Sloan Digital Sky Survey (SDSS), but with their own classifications (combining

a mix of visual and automated methods). Assuming that galaxy color is closely related to galactic gas content (e.g., Catinella et al. 2010; Saintonge et al. 2011), then this is consistent with the expected effects of gas on bar formation and evolution. Indeed, using a sample of Galaxy Zoo 2 bars with HI measurements from the ALFALFA survey, Masters et al. (2012) found that bar fraction correlates strongly with HI content. In that sample, more bars were found in the gas poor disk galaxies, even at fixed color or stellar mass.

Alternatively, Barazza et al. (2008) and Aguerri et al. (2009) found different results using samples of SDSS galaxies with bars identified from ellipse fitting methods. Both of these works found that bar fractions were larger for the bluer (and presumably more gas rich) galaxies in their samples. However, Nair & Abraham (2010a,b) suggest a way to reconcile these results which came from samples of disk galaxies with very different selections; notably Barazza et al. 2008 and Aguerri et al. 2009 selected only blue galaxies as disks, and included lower redshift and less massive galaxies than were present in Masters et al. 2011, Masters et al. 2012, or Lee et al. 2012. The sample of Nair & Abraham (2010a), which probed a wide range of stellar mass, suggested that bar fraction is bimodal with disk galaxy color – having peaks both towards the bluer and redder disk galaxies¹³. Nair & Abraham (2010a) suggest this trend may reveal two distinct types of bars, namely weak bars are predominantly found in lower mass and more gas rich (and bluer) spirals, while stronger bars are more common in massive, redder and gas poor disks.

In addition to the dependence on galaxy color, bar fraction has also been found to depend on inner galactic structure. Masters et al. (2011) found that bar fraction was correlated with fracDeV , which is a parameter measured by the SDSS representing the fraction of the best-fit light profile that originates from the de Vaucouleurs fit to the profile, as opposed to an exponential fit. Lee et al. (2012) also found that the bar fraction was highest at moderate central velocity dispersion. However, Barazza et al. (2008) found that barred galaxies are most likely to exist in galaxies with low Sérsic indices while Aguerri et al. (2009) found that bars are most likely to exist in galaxies with low concentration indices. Although these results appear conflicting, they all show that the presence of a galactic bar is influencing the inner structure of these galaxies.

While the trends of bar fraction can reveal aspects of bar formation and evolution, bar fraction is crude as it hides information on the bar itself. According to A03, the characteristics of a bar (e.g., long or short) can be used as tracers of bar evolution. Therefore, a common bar property that has been studied in the literature is bar length. Athanassoula & Misiriotis (2002) and A03 predicted that the presence of a bulge will result in a longer and more evolved bar. Comparing this prediction to previous observational works shows a good consensus; early-type disk galaxies do indeed have longer bars (Kormendy 1979; Athanassoula & Martinet 1980; Martin 1995; Elmegreen & Elmegreen 1985; Regan & Elmegreen 1997). Larger samples and/or infra-red imaging continues this agreement (Laurikainen et al. 2002; Erwin 2005; Laurikainen et al. 2007; Menéndez-Delmestre et al. 2007; Elmegreen et al. 2007; Aguerri et al. 2009; Gadotti 2011; Hoyle et al. 2011).

In this paper, we use the Galaxy Zoo 2 dataset

¹³ Masters et al. 2011 also commented on a possible upturn in bar fraction for the bluest galaxies in their sample

Table 1
Sample Selection

Criterion	GZ2D #	BL #
Galaxy Zoo 2*	295,305	3,150
$0.01 < z < 0.06^{**}$	76,336	2,674
$M_r < -20.15$	43,266	2,177
$b/a > 0.5$	28,540	1,753
$\frac{1}{4}$ answers bar question	14,353	1,753
$p_{mg} < 0.4$	14,038	1,734
GIM2D models $< 1''$ offset	13,328	1,655
Quality GIM2D disks	13,328	1,159
MPA cross-match	13,295	1,154

Note. — *See footnote 17. **We only consider galaxies with spectroscopic redshifts.

(Masters et al. 2011; Hoyle et al. 2011; Willett et al. 2013) to investigate how the likelihood of a galaxy hosting a galactic bar depends on two important factors, namely the gas content of the galaxy and its inner galactic structure. We perform the same investigation with bar length and compare both of these sets of relationships to theoretical predictions, which will not only give us a better understanding of bar formation and evolution, but also a better understanding of how bars affect their host galaxy.

We begin in §2 by describing all the data used in the paper, while the main observational results are presented in §3. We compare our results with several theoretical simulations in §4 and discuss our work, and these comparisons, in §5. We conclude in §6. In Appendix A, we discuss the completeness of our sample. We assume a cosmological model with $H_0 = 70$ km s⁻¹ Mpc⁻¹, $\Omega_m = 0.30$ and $\Omega_\Lambda = 0.70$ throughout this paper.

2. DATA

This section lists all sources of data that this paper uses. In order to have a fully complementary dataset, we cross-matched every dataset, as described in each subsection, resulting in a successive reduction of the initial sample size. As a guide, our initial dataset is described in §2.2, which derives from SDSS DR7 (summarized in §2.1). We list the sample totals at the end of each subsection, starting with §2.2. Table 1 lists every major cut made to our two samples, and the resultant sample sizes.

2.1. SDSS

All the galaxies used in our sample are drawn from the Main Galaxy Sample in the Legacy area of the SDSS Data Release Seven (SDSS DR7; Strauss et al. 2002; Abazajian et al. 2009). Where possible, we use the standard photometric and structural parameters provided by the SDSS pipeline. For example, we use the SDSS information to define a surface stellar mass density within a radius of one kiloparsec of the center of the galaxy, $\Sigma_{1 \text{ kpc}}^*$. We choose one kpc for this density as it matches the typical scale of bulges (Fisher & Drory 2010) and therefore, should be closely related to the bulges of most galaxies.

In detail, $\Sigma_{1 \text{ kpc}}^*$ is created from the SDSS galaxy surface brightness profiles, `profMean`, which is the mean surface brightness in a series of circular annuli, from the `PhotoProfile` table in the `CasJobs` website¹⁴. In accordance with

the SDSS recommendations¹⁵, we take the inverse hyperbolic sine of each cumulative profile and fit them with a natural cubic spline. After transforming the spline fits back with a sine function, we differentiate the fits and obtain an estimate of the azimuthally averaged surface brightness profile. Finally, we compute the magnitude and color within one kpc for each galaxy from these profiles and convert them into a stellar mass through a color-dependent mass-to-light (M_*/L_g) ratio (e.g., Bell & de Jong 2001). Our M_*/L_g relationship is derived from a linear fit to the rest-frame $g-r$ color from GIM2D (see §2.3) and the M_*/L_g , where the stellar masses are taken from the MPA-JHU catalog (see §2.4) and the g -band luminosity is taken from GIM2D models.

One concern is that the one kpc radius aperture is smaller than the typical seeing of SDSS. However, an analysis of angular sizes of galaxies in our sample, which lies within the redshift range $0.01 < z < 0.06$ (see §2.2), shows they are typically larger than the full width at half maximum (FWHM) of the SDSS point-spread function ($\sim 1.3''$ in the r -band; Abazajian et al. 2009).

2.2. Galaxy Zoo

Galaxy Zoo is a citizen science project that enlisted hundreds of thousands of volunteer “citizen scientists” to make morphological classifications of nearly one million galaxies (Lintott et al. 2008, 2011). The initial Galaxy Zoo project asked the public to classify galaxies as elliptical, spiral, or merger. With the Galaxy Zoo 2 project (Willett et al. 2013), the citizen scientists were asked to make more detailed classifications of approximately 304,000 galaxies.

The final product of Galaxy Zoo 2 is a table of morphological likelihoods, including the likelihood that a bar is present in each galaxy, as represented by p_{bar} , e.g., if 5 out of 10 scientists classified a galaxy as having a bar, the galaxy would be assigned a bar probability of $p_{\text{bar}} = 0.5$. These raw probabilities are then adjusted to account for the reliability of each user through an iterative weighting scheme that “down-weights” classifications from unreliable users (typically a few percent of the population). We also apply a correction to the likelihoods to account for the deterioration of the image quality due to increasing distance of galaxies, i.e., we assume galaxies of a similar luminosity and size will share the same average mix of morphologies regardless of redshifts. This also assumes there is no significant evolution within the SDSS at these low redshifts, which is probably reasonable (Bamford et al. 2009; Willett et al. 2013). Therefore, throughout the paper, we will only use these corrected, or “debiased”, bar likelihoods and will calling them p_{bar} for convenience.

In Masters et al. (2011) and Masters et al. (2012), barred galaxies were selected using $p_{\text{bar}} \geq 0.5$. This threshold delivered a high purity of barred galaxies in comparison with other barred galaxies sample, e.g., almost all galaxies with $p_{\text{bar}} \geq 0.5$ were classified as possessing a strong bar by Nair & Abraham (2010a) (see Appendix A of Masters et al. 2012). Weaker bars in Nair & Abraham (2010a) were found to correspond to $0.3 \leq p_{\text{bar}} \leq 0.5$ (Masters et al. 2012; Willett et al. 2013).

In this work, we choose to use p_{bar} as a bar likelihood, rather than as a bar threshold. This method has been used before with Galaxy Zoo classifications (e.g., Bamford et al. 2009; Skibba et al. 2009, 2012). Our results are in qualitative agreement with other GZ results who used bar fractions, e.g.,

¹⁴ <http://casjobs.sdss.org/CasJobs/>

¹⁵ <http://www.sdss.org/dr7/algorithms/photometry.html>

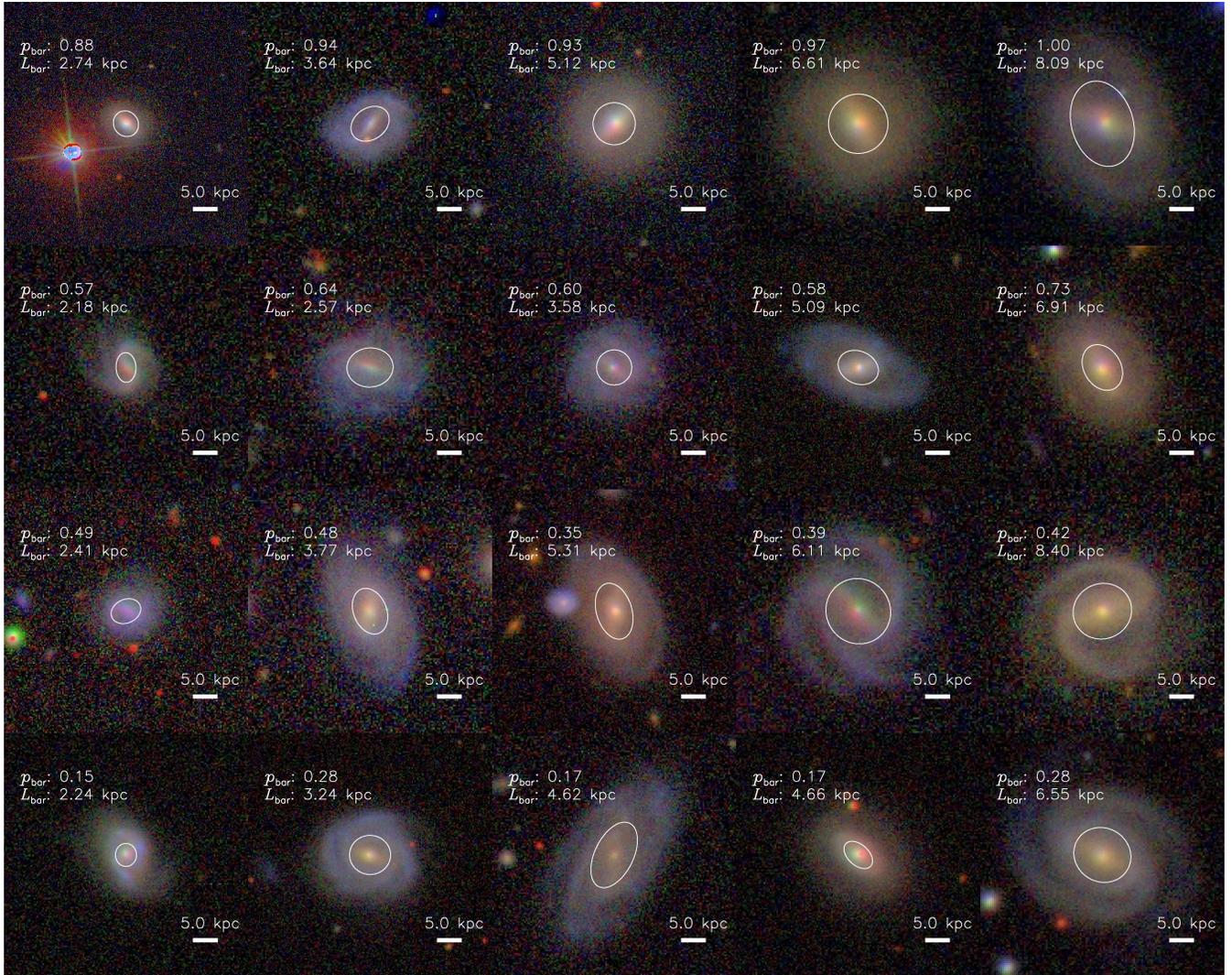


Figure 1. A gallery of galaxies with a range of bar likelihood, p_{bar} , and bar length, L_{bar} . Each row is ordered by increasing bar length. The ellipse drawn over each galaxy represents the GIM2D disk model at r_d . Visually, the bars generally extend out the disk scale length, consistent with Combes & Elmegreen (1993). The physical scales of every image are the same (± 1 pixel).

if we adopt a bar threshold of $p_{\text{bar}} = 0.5$, we find an overall bar fraction of $23.6 \pm 0.4\%$, which is similar to Masters et al. (2011)¹⁶.

Our initial sample is the Galaxy Zoo 2 dataset¹⁷. Following Masters et al. (2011), we only select galaxies with spectroscopic redshifts in the range of $0.01 < z < 0.06$. In order to have a volume-limited sample, we only include galaxies with $M_r < -20.15$, where M_r is the rest-frame absolute Petrosian r -band magnitude. This limit corresponds to the Galaxy Zoo 2 completeness Petrosian magnitude of 17 in the r -band (Willett et al. 2013) at $z = 0.06$. To ensure that our sample contains relatively face-on galaxies, we applied an axis ratio requirement of $b/a > 0.5$ (this corresponds to inclination angles less than ≈ 60 degrees), where b/a is the axis ratio from the GIM2D single Sérsic model fit (see §2.3). This requirement minimizes projection effects and thus results in

¹⁶ The difference between our bar fraction and that of Masters et al. (2011) is due to the use of the weighted and debiased bar fractions from Willett et al. (2013) which were unavailable at the time of Masters et al. (2011).

¹⁷ This Galaxy Zoo 2 sample is comprised of the ‘original’, ‘extra’, and ‘stripe82’ sample in Table 1 of Willett et al. (2013). These data are available at <http://data.galaxyzoo.org>

more reliable bar classifications. This sample also requires that all galaxies have a `Petro90` radius of $> 3''$. We have tested our results with a larger minimum radius requirement and find that our results are unchanged¹⁸.

We also require that for each galaxy, at least a quarter of all its classifications involved answering the bar question, ‘*Is there a sign of a bar feature...*’ (Masters et al. 2011). In order to reach the bar question, however, a user must first classify a galaxy as a non-edge-on galaxy with a disk or some sort of feature (e.g., spiral arms, rings, bars). Assuming that most identified features are associated with a disk, then this last selection effectively ensures we have non-edge-on-disk galaxies.

Finally, we discard all merging galaxies from the sample since we are only concerned with isolated galaxies that have reliable photometric and structural measurements. According to Darg et al. (2010), the Galaxy Zoo merging parameter, p_{mg} , can identify merging galaxies with a cut of $p_{\text{mg}} > 0.4$; we adopt this threshold to eliminate merging galaxies. There is a total of 14,038 galaxies in the resulting sample, which we

¹⁸ We find that our results are unchanged when we restrict our sample to galaxies with global half-light radii (as measured by GIM2D) larger than $5''$.

will call the Galaxy Zoo 2 Disk (GZ2D) sample.

We carefully review here the make-up of our sample to avoid confusion with comparisons with other disk, spiral or late-type selections based on GZ morphologies. The disk galaxy selection presented herein possibly includes a fraction of very early-type disks galaxies (Sa or S0) which would normally be included in a majority of early-type samples selected either by color, or central concentration. This results in our diverse disk galaxy sample showing bimodality in their optical color-mass diagram (Fig. 3a). However, other Galaxy Zoo samples, that are more focused on late-type disks or spirals sample (Sb, Sc or later) can be constructed using the GZ1 “clean” spiral criterion as first discussed in Land et al. (2008), and most recently used in Schawinski et al. (2013, in preparation), but also through stricter limits in GZ2/GZ Hubble data. This more conservative late-type sample will be more dominated by “blue cloud” spirals and thus show less bimodality of their galaxy properties.

In addition to this sample, we use a Galaxy Zoo 2 subsample that possesses additional bar length measurements. The bar lengths were visually measured by citizen scientists using a Google Maps interface described by Hoyle et al. (2011). The bar lengths represent the lengths from one end to the bars to the other. In order to be consistent with previous works, who define it as the semi-major axis of maximum ellipticity in the bar region (e.g., Erwin 2005), we will take half of the Galaxy Zoo 2 bar lengths and denote it L_{bar} . This catalog requires at least 3 independent bar length measurements per galaxy; the mean of these independent bar length measurements gives L_{bar} of each galaxy. The vast majority of galaxies that were selected for this sample have $p_{\text{bar}} \geq 0.6$, i.e., this sample contains mainly strong bars (Masters et al. 2012; Willett et al. 2013). Of the GZ2D sample, there are 1,734 galaxies that have bar length measurements, which will now be referred to as the Bar Length (BL) sample.

We present a gallery of barred galaxies with a range of p_{bar} and L_{bar} in Fig. 1. Each row is ordered by absolute bar length.

2.3. GIM2D

Two-dimensional bulge+disk decompositions in the g and r bandpasses of over a million SDSS galaxies were performed with GIM2D by Simard et al. (2011). Improvements to the sky background determinations and object deblending over the standard SDSS procedures led to more robust galactic structural parameters than those offered by the standard SDSS pipeline.

Three different models were used in these decompositions: a pure Sérsic model, an $n = 4$ bulge + exponential disk model, and a Sérsic (free-floating n) bulge + exponential disk model. The most important GIM2D parameter for the GZ2D sample is the galaxy Sérsic index, n , from the pure Sérsic model, i.e., the best-fitting single Sérsic index for a given galaxy. The Sérsic index has often been used to separate early-type and late-type galaxies and is widely regarded as a good proxy for bulge dominance (Blanton et al. 2003; Shen et al. 2003; Bell et al. 2004; Schiminovich et al. 2007; Drory & Fisher 2007; Bell 2008; Wuyts et al. 2011; Bell et al. 2012; Wake et al. 2012; Cheung et al. 2012).

Although a similar parameter, fracDeV from the SDSS database, has been explored by previous works (e.g., Masters et al. 2011; Skibba et al. 2012), n is a more common parameter in the literature and has been thoroughly studied (e.g., Graham & Driver 2005). It is also the basis of most galaxy fitting programs (e.g., GALFIT, BUDDA, and

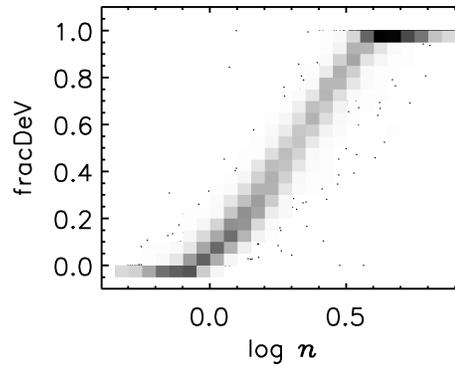


Figure 2. Comparison of n from the GIM2D single Sérsic model fit and fracDeV (r band) from the SDSS database. The cluster of galaxies at fracDeV=1 and fracDeV=0 accounts for $\sim 27\%$ of the total GZ2D sample, indicating that there is a loss of galaxy structural information in the fracDeV parameter.

GIM2D; Peng et al. 2002; de Souza et al. 2004; Simard et al. 2002), which allows for easier and more consistent comparisons to other works. For reference, we compare n and fracDeV in Fig. 2 for our GZ2D sample. Clearly, the two parameters are correlated. However, the overdensity of galaxies at fracDeV=1, which accounts for $\sim 15\%$ of the GZ2D sample, indicates that there is a saturation of galaxy structural information in the fracDeV parameter. Indeed, for fracDeV=1, $\log n$ ranges from 0.5 to 0.9, corresponding to $n \sim 3 - 8$. A similar effect occurs at fracDeV=0, which accounts for another $\sim 12\%$ of the GZ2D sample. Our use of Sérsic index in this paper should be more sensitive than fracDeV to the complicated structures of galaxies.

Another similar parameter is the Petrosian concentration index from SDSS. This parameter has been shown by Gadotti (2009) to be a better proxy for bulge fraction than the global Sérsic index. We would like to note, however, that the global Sérsic indices that Gadotti (2009) used were from the New York University Value-Added Galaxy Catalog (Blanton et al. 2005a,b), which fitted one-dimensional profiles extracted from two-dimensional images using *circular* annuli. The GIM2D fits were done using *elliptical* annuli, and are two-dimensional fits. As noted by Simard et al. (2011), this difference in methodology, i.e., using circular and elliptical apertures, results in a systematic offset between the NYU and GIM2D galaxy half-light radius and galaxy Sérsic index. At the request of the referee, we tested our results using R90/R50 in Appendix C – we find no major impacts to our conclusions.

The most important GIM2D parameter for the BL sample is the semi-major axis exponential disk scale length, r_d ; this is needed to properly scale the bar length. The disk scale length is available in both the $n = 4$ bulge + exponential disk model and the Sérsic bulge + exponential disk model; we use the latter model¹⁹. As is noted in Simard et al. (2011), the quality of the GIM2D bulge+disk decompositions is highly dependent on the spatial resolution and signal-to-noise of the SDSS images. Therefore, it is important to ensure that we only allow model fits that are reliable. However, since we are only concerned with r_d , picking out reliable decompositions is not difficult. From Simard (priv. comm.), galaxy models with $B/T \leq 0.5$ (the B/T from the Sérsic bulge + exponential disk model) accurately model the disk component, and hence we consider all these galaxies. This is understandable since these

¹⁹ We find no change in our main conclusions if we use the $n = 4$ bulge + exponential disk model.

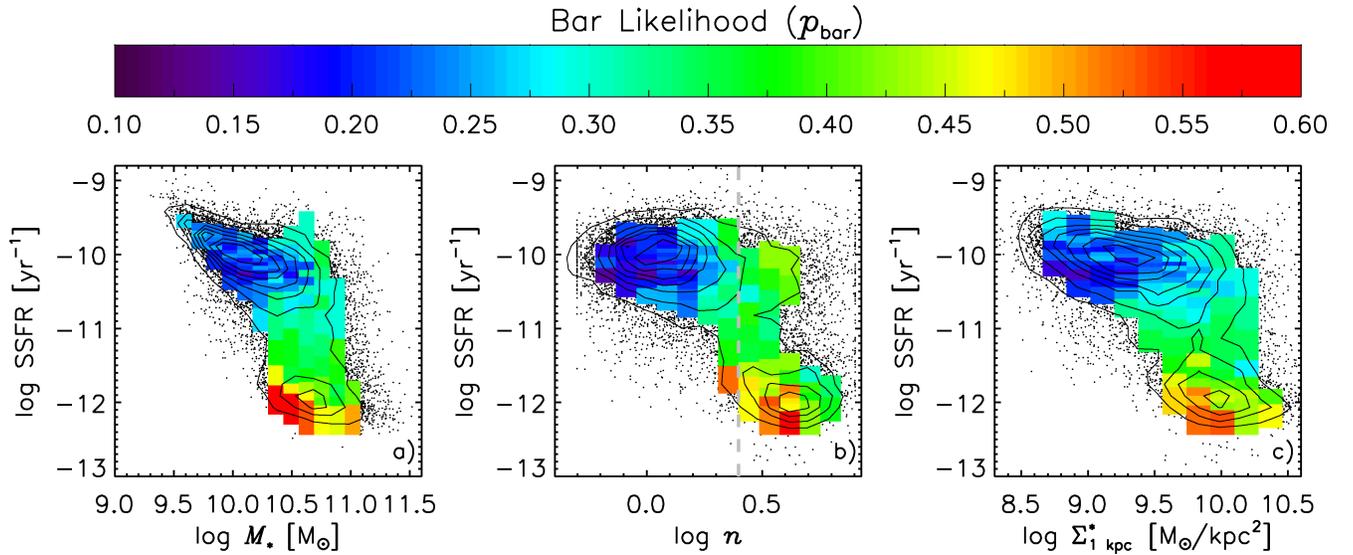


Figure 3. Average bar likelihood, p_{bar} , in bins of: a) SSFR vs. stellar mass M_* , b) SSFR vs. Sérsic index n , c) SSFR vs. central surface stellar mass density $\Sigma_{1 \text{ kpc}}^*$. Each bin is adjusted so that it contains ~ 100 galaxies (individual points are shown for poorly populated bins). Bin colors indicate the average value of p_{bar} in the bin (see color bar at top), while the contours show the density of points. The gray dashed vertical line in panel b represents the division between galaxies containing disk pseudobulges ($n < 2.5$) and classical bulges ($n > 2.5$; see Drory & Fisher 2007). This plot shows that the trends of bar likelihood with galaxy properties depend on the SSFR of the galaxies. The relationship of p_{bar} with n and $\Sigma_{1 \text{ kpc}}^*$ is bimodal with SSFR.

galaxies are disk-dominated and their corresponding GIM2D models will likely yield reliable disk measurements. For models with $B/T > 0.5$, Simard (priv. comm.) recommends considering only galaxies with $P_{pS} < 0.32$, where P_{pS} represents the probability that a bulge+disk model is *not* required compared to a pure Sérsic model (Simard et al. 2011). Thus $B/T > 0.5$ galaxies that have a high probability of requiring a bulge+disk model are also considered.

To avoid the effects of the SDSS point-spread function on the GIM2D disk model, we only allow disk models with $r_d > 2''$. Furthermore, we impose a strict face-on requirement such that all GIM2D model disks have inclination angles of less than 55 degrees. This corresponds to axis ratios greater than 0.6, a parameter space that has been shown by MacArthur et al. (2003) to produce no systematic variations on r_d when using 2D galaxy decompositions. Finally, we require that the fractional errors on r_d ($r_{d,\text{error}}/r_d$, where $r_{d,\text{error}}$ is the formal error of r_d from GIM2D) be less than 2%. This number is approximately two standard deviations above the average $r_{d,\text{error}}/r_d$ of the BL sample. We choose this conservative cut in order to include only quality disk models.

We note that, although we only model a bulge and disk for these disk galaxies, $\sim 24\%$ of which are strongly barred, previous works have shown that, while bulge parameters may be affected by the presence of a bar, the disk scale length is not significantly affected (Erwin 2005; Laurikainen et al. 2005). This reliability is evident in the fact that our results are not sensitive to the choice of GIM2D bulge+disk model, i.e., both r_d from the $n = 4$ bulge+disk model and the Sérsic bulge+disk model produce the same results. Furthermore, the GIM2D formal errors on r_d are not significantly different from strongly barred systems ($p_{\text{bar}} > 0.8$) and non-bared systems ($p_{\text{bar}} < 0.05$).

We impose a final cut that eliminates all GIM2D models where the centers are offset from the input science images by more than one arcsecond. Large offsets like these usually represent a bad fit, and, indeed, upon visual inspection, we find that almost all these cases contained bright point sources within the galaxy and/or diffraction spikes from nearby stars.

Matching the GZ2D and BL samples to the GIM2D catalogs leave us with 13,328 and 1,159 disk galaxies, respectively.

2.4. MPA-JHU

Stellar masses and star formation rates are taken from the MPA-JHU DR7 release²⁰. Stellar mass (M_*) estimates are calculated using the Bayesian methodology and model grids described in Kauffmann et al. (2003). The models are fit to the broadband *ugriz* SDSS photometry, instead of the spectral indices from the $3''$ fiber aperture. These estimates are corrected for nebular emission and a Kroupa (2001) initial mass function is assumed.

Star formation rates (SFR) are based on the technique presented in Brinchmann et al. (2004). For their ‘Star-Forming’ class, which consists of 39,141 galaxies, they estimate the SFR from model fits that cover a wide range of star formation histories of several emission lines from the SDSS fiber. For ‘Low S/N Star-Forming’ class, which contains 29,115 galaxies, they convert the observed $H\alpha$ luminosity into a SFR. And for the ‘AGN’, ‘Composite’ and ‘Unclassifiable’ classes, which contain a total of 66,986 galaxies, they use the D4000 value to estimate SFR/M_* and SFR. Aperture corrections follow the method of Salim et al. (2007), resulting in the SFR of the entire galaxy. The specific star formation rate (SSFR), a parameter that will be used throughout the paper, is defined to be the SFR divided by stellar mass; it was calculated by combining the SFR and M_* likelihood distributions as outlined in Appendix A of Brinchmann et al. (2004).

Matching the GZ2D and BL samples to the MPA-JHU catalog brings our final sample to 13,295 and 1,154, respectively. A detailed discussion of the completeness of the GZ2D and BL samples is presented in Appendix A. We find that while we are missing some low-mass quiescent disk galaxies, the effect is small and does not affect our results.

3. RESULTS

²⁰ <http://www.mpa-garching.mpg.de/SDSS/DR7/>

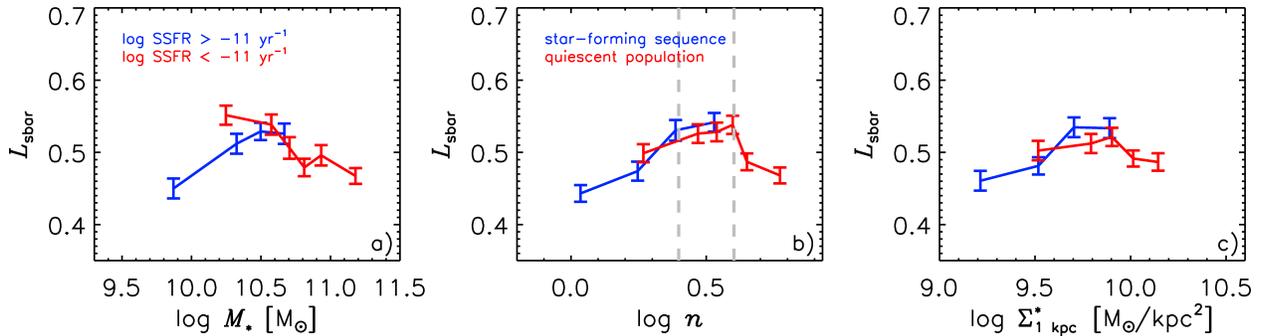


Figure 4. Average L_{sbar} plotted against: a) M_* , b) n , and c) $\Sigma_{1 \text{ kpc}}^*$. Galaxies were split by their star formation state, namely, $\log \text{SSFR} > -11 \text{ yr}^{-1}$ (star-forming; blue) and $\log \text{SSFR} < -11 \text{ yr}^{-1}$ (quiescent; red). Each bin contains ~ 100 galaxies. The error bars are given by σ/\sqrt{N} , where σ is the standard deviation of L_{sbar} per bin, and N is the total number of galaxies per bin. The vertical dashed lines in panel b are located at $\log n = 0.4$ ($n = 2.5$) and $\log n = 0.6$ ($n = 4$).

3.1. Bar Likelihood Trends

In this section, we present the trends of bar likelihood with SSFR, stellar mass, and measures of bulge prominence.

The three panels of Fig. 3 plot both galaxy density and average p_{bar} in a 2D plane of: SSFR versus stellar mass (M_* ; panel a), SSFR versus global Sérsic index (n ; panel b), and SSFR versus central surface stellar mass density ($\Sigma_{1 \text{ kpc}}^*$; panel c). The locations of the galaxies are shown by the contours. Bin sizes are adjusted so that they contain ~ 100 galaxies each, and individual data points are shown for poorly populated bins. Each bin is colored by the average p_{bar} of the galaxies in it as indicated by the color bar.

The well-known bimodality between galaxies (even for disk galaxies) in the star-forming sequence and those in the quiescent population is clear in our sample and affects not only the galaxies' SSFR, baryonic mass, and bulge properties, but also their likelihood of being barred (Masters et al. 2011). We find that there is a strong correlation between average p_{bar} and SSFR such that the average values of p_{bar} are larger for low SSFR disk galaxies (i.e., quiescent disk galaxies are more likely to host bars). The observed relationship between p_{bar} and SSFR is present even at fixed M_* , n , or $\Sigma_{1 \text{ kpc}}^*$ (Fig. 3), indicating that this relationship is nearly independent of these galaxy properties.

Taking SSFR as a proxy for gas fraction (e.g., Kauffmann et al. 2012) suggests that the underlying relationship is really between p_{bar} and gas content such that bar likelihood is increasing as gas fraction decreases. Similar trends between bar fraction and gas content were also observed by Masters et al. (2012).

We observe that the trends of the average bar likelihood with M_* , n , and $\Sigma_{1 \text{ kpc}}^*$ depend on whether the disk galaxy is star-forming or quiescent, as is illustrated by Fig. 3. Thus we look in more detail at the observed trends within the star-forming ($\log \text{SSFR} > -11 \text{ yr}^{-1}$) and quiescent ($\log \text{SSFR} < -11 \text{ yr}^{-1}$) disk galaxy populations. We find:

- **Stellar Mass, M_* (Fig. 3a)** – There is a correlation between average p_{bar} and stellar mass within the star-forming disks such that p_{bar} is larger the larger their stellar mass. There is also an anti-correlation of p_{bar} with stellar mass within the quiescent population.
- **Sérsic Index, n (Fig. 3b)** – For the star-forming sequence, p_{bar} is strongly correlated with n (even more so than it is with M_*). Within the quiescent population, we see an inverse correlation between p_{bar} and n . This is an important point to note and might explain the

contradictions between the results of previous studies, which found opposite trends of bar fraction with measures of bulge prominence from light profile shape (e.g., Masters et al. 2011 compared to Barazza et al. 2008). Moreover, this observation is in good agreement with theoretical predictions of bar formation as will be described in §4.

- **Central surface stellar mass density, $\Sigma_{1 \text{ kpc}}^*$ (Fig. 3c)**

– We find similar trends of p_{bar} with this parameter as between p_{bar} and n . Star-forming galaxies show a correlation between p_{bar} and $\Sigma_{1 \text{ kpc}}^*$ (star-forming disks are more likely to host bars where the central density is higher), while quiescent galaxies show an anti-correlation (quiescent disks are more likely to host bars where the central density is lower)

3.2. Bar Length Trends

In this section we examine how bar length depends on galaxy properties. We define a scaled bar length, L_{sbar} , as the bar length divided by a measure of disk size. We choose for this $2.2r_{\text{d}}$ (2.2 semi-major axis exponential disk scale lengths) because this is where the rotation curve of a self-gravitating exponential disk reaches its maximum (Freeman 1970). Hereafter, we will refer to the scaled bar length simply as the bar length unless stated otherwise.

Bars become longer over time as they transfer angular momentum from the bar to the outer disk and/or spheroid (halo and, whenever relevant, bulge). This secular evolution causes the host disk to expand and increase its scale length while the bar also grows. We will compare trends of bar length with those of p_{bar} to test if the trends we observe in the average value of p_{bar} in the galaxy population are due to the evolution of the bars, or the likelihood of bar formation in a galaxy.

Since the BL sample is more than an order of magnitude less numerous than the GZ2D sample, we find that breaking it up into small bins, as we did in Fig. 3 for p_{bar} results in no clear correlations. Since we found that the trends of p_{bar} had different properties depending on the SSFR of the galaxies, we split the BL sample into two subsamples (star-forming, or $\log \text{SSFR} > -11 \text{ yr}^{-1}$, and quiescent, or $\log \text{SSFR} < -11 \text{ yr}^{-1}$) to look at the trends of average L_{sbar} . These trends are shown in Fig. 4.

This figure shows that in the star-forming sequence, the average value of L_{sbar} increases with all three properties (M_* , n , and $\Sigma_{1 \text{ kpc}}^*$). In the quiescent population we find that the average bar length decreases with M_* . Curiously we find that the average bar length increases with n and $\Sigma_{1 \text{ kpc}}^*$ up to a maxi-

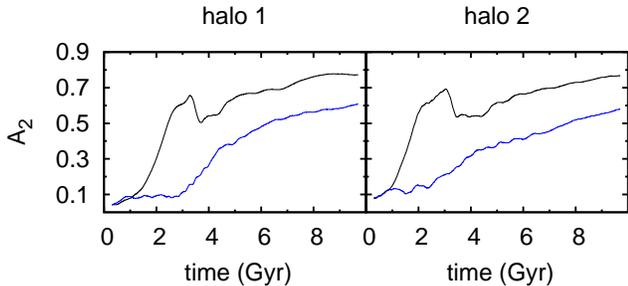


Figure 5. Bar strength, A_2 , which can be considered as a rough proxy for bar length, as a function of time for four simulations. Two simulations have a gas-rich disk (blue lines) while the other two have a gas-poor disk (black lines). The two panels correspond to different types of haloes: initially spherical (left panel) and initially triaxial (right panel). For a full description of these simulations and their results, see AMR13. These simulations show that bars grow slower and are less strong in the gas-rich case.

imum value at around $\log n \approx 0.6$ ($n \approx 4$) and $\Sigma_{1 \text{ kpc}}^* \approx 10^{9.8} M_\odot/\text{kpc}^2$ respectively, where the trend reverses.

4. COMPARISON TO THEORY

In this section, we compare our results in §3 with theoretical expectations of bar formation and evolution. We start with a short summary of theoretical results.

4.1. Theoretical Reminders

One can distinguish (at least) two phases in the lifetime of a bar: the formation phase and the secular evolution phase. AMR13 showed that these two phases are contiguous in gas-rich cases, while, for gas-poor ones, they are not. In the latter case, there are two further stages of relatively short duration in between the formation and secular evolution phases²¹.

This is illustrated in Fig. 5, where we plot the bar strength, A_2 , which is closely related to bar length, as a function of time for four simulations from AMR13. The two simulations in each panel have the same initial mass and velocity distribution of the baryonic and dark matter components. The only difference is the gas fraction, where the black and blue lines represent gas-poor and gas-rich simulations, respectively. The end of the bar formation phase is represented by the time when the steep increase of A_2 terminates, which is at times 2 – 2.5 Gyrs for the gas-poor simulations, and around 4.5 Gyrs for the gas-rich ones. These simulations illustrate that gas slows down bar formation considerably (AMR13). This is due both to an increase in the duration of the pre-bar phase (i.e., the phase during which the disk can still be considered as axisymmetric) and a decrease in the rate of the bar growth (i.e., an increase of the time it takes for the bar to end its growth phase), both being compared to the times of the equivalent phases in the gas-poor case.

The secular evolution phase, however, starts roughly at 4.5 Gyrs for all cases. In general, the duration of these phases, as well as the increase of bar strength that they imply, depend on the mass and velocity distribution of the baryonic and dark matter components within the galaxy, as well as on the gas fraction. Readers can find more information and a long list of relevant references in a recent review by Athanassoula (2012). It is also interesting to note in Fig. 5 that, for all times and in both phases, the bar in the gas-rich case is less strong than in the gas-poor one (see also Berentzen et al. 2007).

²¹ These two extra stages are related to the bar buckling phase (i.e., the formation of a boxy/peanut bulge), which is much less obvious in gas rich cases.

Bar formation and evolution is influenced also by galactic bulges. Bulges, however, are an inhomogeneous class of objects (Kormendy 1993; Kormendy & Kennicutt 2004; Athanassoula 2005). Classical bulges have high Sérsic indices, typically around 4, but certainly above 2. Disky pseudobulges, on the other hand, have low Sérsic indices, typically around 1, and usually less than 2 (Fisher & Drory 2010). The most popular scenario for the formation of diskly pseudobulges in barred galaxies is that they are due to stars, and particularly, gas pushed inwards by the bar to the central parts of the disk. Here, the high density gas will give rise to star formation, so that the diskly pseudobulges should be primarily composed of gas and young stars with a smaller fraction of old stars. Their extent is typically of the order of 1 kpc (Athanassoula 1992; Heller & Shlosman 1994; Fisher & Drory 2010)²².

These two different types of bulges have different dynamics and, therefore, different effects on the bar formation and evolution phases. Classical bulges predate the bar, so they will influence both phases. Their influence has many similarities to that of the dark matter halo. Namely, they slow down bar formation in the first phase, but, during the secular evolution phase, they help the bar grow by absorbing angular momentum, leading to stronger bars (Athanassoula & Misiriotis 2002, A03). Thus, simulations predict that bars in galaxies with classical bulges should be stronger than bars in galaxies without classical bulges, assuming all other properties are the same.

On the other hand, diskly pseudobulges in barred galaxies are formed by material pushed inwards by the bar, i.e., they do not predate the bar and thus cannot influence its formation phase. Moreover, diskly pseudobulges should not help the bar grow during the secular evolution phase either, since they cannot absorb angular momentum. This is because the radii of diskly pseudobulges are considerably smaller than the corotation radius, and also because diskly pseudobulges are flat (spherical-like density distributions, like the classical bulge or the halo, can absorb angular momentum). However, although diskly pseudobulges do not affect bar formation or evolution, bars do affect diskly pseudobulges. In fact, bar-driven secular evolution is the primary process of diskly pseudobulge creation and growth (Kormendy & Kennicutt 2004; Athanassoula 2005). Thus, the theoretical prediction is that stronger bars push more gas inwards, resulting in more massive diskly pseudobulges.

A visual approximation of bar formation and evolution is presented in Fig. 6.

4.2. The Effect of Gas Content on Bar Formation

We explain the trends we observe between the likelihood of disk galaxies being barred and their SSFR (present even at fixed M_* , n , or $\Sigma_{1 \text{ kpc}}^*$; see Fig. 3) as being due to the effect of gas on bar formation. In the models, bars form later in disk galaxies with significant gas content, and after they form, they grow slower than disk galaxies with comparably less gas (AMR13 and Fig. 5). This predicts that the bar likelihood should be higher in gas-poor galaxies (i.e., the quies-

²² For completeness, we mention the boxy/peanut bulges, which, in fact, are part of the bar. Their Sérsic indices are smaller, or of the order of that of the diskly pseudobulges. Given that all our decompositions here include only one or two components (§2.3), and bars are not included, and our sample excludes highly inclined systems, such bulges do not enter in our discussion. However, we do note that they may still be present in the sample and may not be well fit by our decompositions.

Schematic of Bar Formation and Evolution

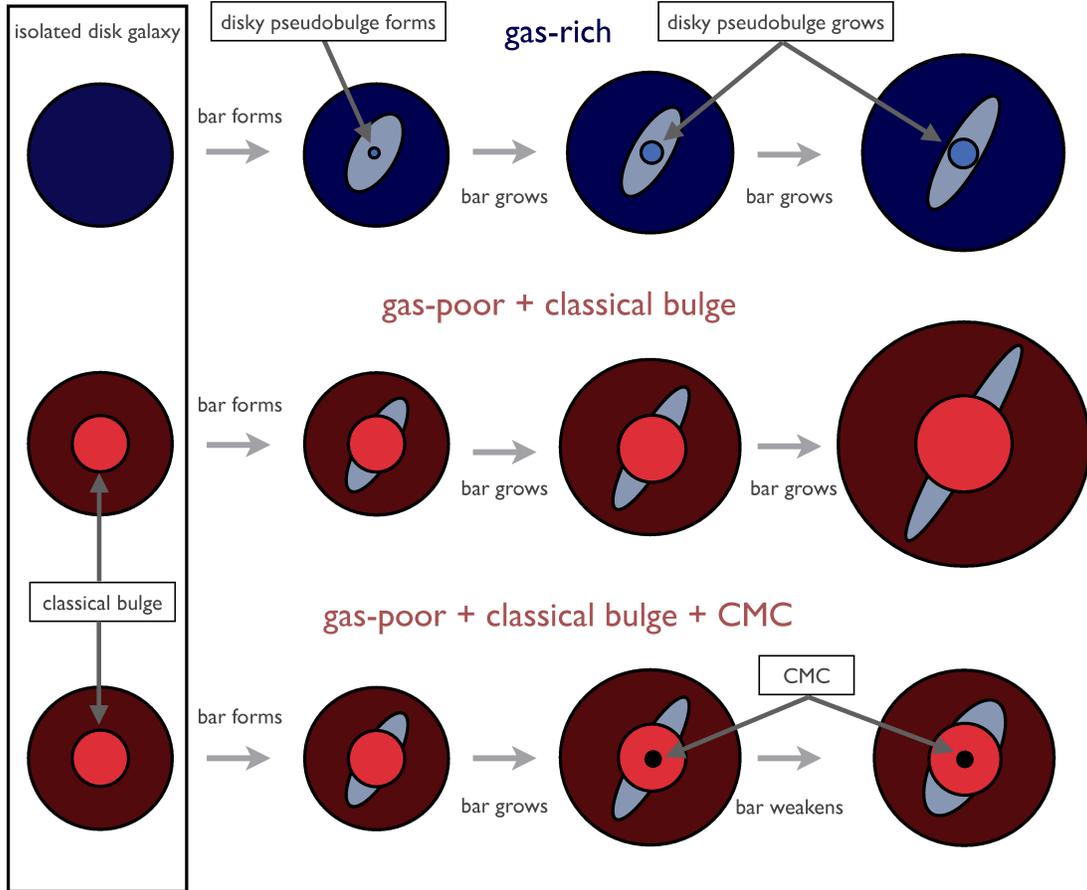


Figure 6. A schematic diagram of bar formation and evolution. *Top row* illustrates the gas-rich scenario, in which a bar forms and grows over time. As the bar enters the secular evolution phase, a diskly pseudobulge is created. The growth of the diskly pseudobulge follows that of the bar. *Middle row* illustrates the gas-poor scenario with a classical bulge. The evolution of the bar in the gas-poor case is faster than that of the gas-rich case. *Bottom row* illustrates the gas-poor scenario with a classical bulge and a central mass concentration (CMC). The development of a CMC weakens the bar.

cent population), simply because some of the gas-rich galaxies (i.e., the star-forming sequence) have not yet formed their bars. Thus, taking SSFR as a tracer of gas content, then there is good agreement between simulation results and the trends we find (see also Masters et al. 2012).

Within the star-forming sequence (defined here as $\log \text{SSFR} > -11 \text{ yr}^{-1}$) disk galaxies do not all have the same p_{bar} , but neither do they all have the same gas content. There are well known trends between SSFR, stellar mass, and gas content of disk galaxies (e.g., Catinella et al. 2010; Saintonge et al. 2011). The trend we observe here for p_{bar} to increase as SSFR declines (and M_* increases) can be explained as being due to decreasing amounts of gas in the disks of these galaxies. Indeed, Masters et al. (2012) showed that if you correct for the typical HI content of a disk galaxy, those galaxies with more HI than is expected for their stellar mass are less likely to host bars.

4.3. The Effects of Classical Bulges and Diskly Pseudobulges on Bar Formation

We observe trends of bar likelihood with the Sérsic index (n , Fig. 3b) and central surface stellar mass density ($\Sigma_{1 \text{ kpc}}^*$,

Fig. 3c), where these latter two parameters are considered to be measures of bulge prominence. In the star-forming sequence bar likelihood increases with both increasing n and $\Sigma_{1 \text{ kpc}}^*$, while the opposite trend is observed in the quiescent population. In order to interpret these trends, we need to remember that there are two main types of bulges – the classical bulge and the diskly pseudobulge, a distinction which will help explain this dichotomy.

The best way to distinguish these types of bulges involves the use of high resolution imaging of the bulges (e.g., Fisher & Drory 2008), something that is not available for our large sample. However one can approximately separate the types with a threshold in the global galaxy Sérsic index (Drory & Fisher 2007)²³. Diskly pseudobulges generally lie in galaxies with global $n < 2.5$ while classical bulges are found in galaxies with global $n > 2.5$. Although this method is less accurate than those using high resolution imaging, this is a simple option that is adequate for our purposes. Hence, we adopt this Sérsic threshold for the rest of the paper to distin-

²³ Gadotti (2009) advocates using the Kormendy relationship to separate classical bulges from diskly pseudobulges. For this work, however, we choose to use the more simple global galaxy Sérsic threshold.

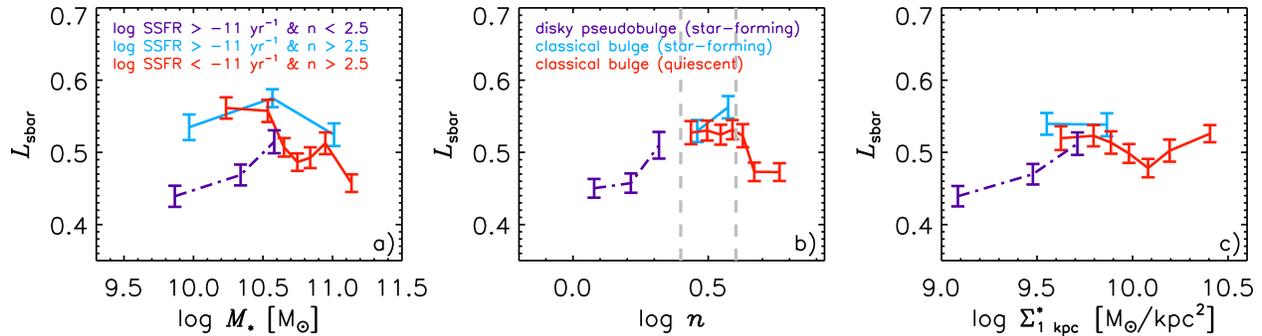


Figure 7. Average L_{sbar} plotted against: a) M_* , b) n , and c) $\Sigma_{1\text{kpc}}^*$. The details of this figure are identical to that of Fig. 4, with the exception that each bin contains ~ 75 galaxies and also, galaxies are further separated by bulge type, as identified by n . Purple points represent the star-forming disk pseudobulge galaxies, light blue points represent the star-forming classical bulge galaxies, and red points represent the quiescent classical bulge galaxies. The correlations of L_{sbar} with n and $\Sigma_{1\text{kpc}}^*$ for the disk pseudobulge galaxies match the predictions of bar-driven secular evolution.

guish the two types of bulges²⁴. This threshold is illustrated with a vertical dashed line at $\log n = 0.4$ ($n = 2.5$) in Fig. 3b.

Our sample confirms the well known observation (e.g., Drory & Fisher 2007) that quiescent (red) disk galaxies primarily have classical bulges while star-forming (blue) disk galaxies mainly have disk pseudobulges (see Fig. 3b). This suggests that the decreasing p_{bar} with n and $\Sigma_{1\text{kpc}}^*$ observed in the quiescent disk galaxies is due to p_{bar} decreasing in galaxies with larger classical bulges, while the increasing p_{bar} with n and $\Sigma_{1\text{kpc}}^*$ observed in star-forming disks shows that p_{bar} is larger in galaxies with more massive disk pseudobulges.

The classical bulge, like the halo, slows down bar formation due to it ‘diluting’ the non-axisymmetric forcing of the bar (Athanasoula 2012). This predicts that bar likelihood should decrease with increasing prominence of the classical bulge, as we indeed observe.

Disk pseudobulges result from the material that a bar pushes inwards to the central part of the disk. Since these bulges formed after the bar, and are in fact, a product of the bar, they cannot influence the bar formation phase. However there is a clear link predicted between the existence of the bar and the amount of mass in the disk pseudobulge, (or central 1 kpc; Athanasoula 1992; Heller & Shlosman 1994; Fisher & Drory 2010). For galaxies of a given gas mass (or SSFR), a higher bar likelihood should result in more massive disk pseudobulges, as we observe (Figs. 3b and 3c).

4.4. Evidence for Secular Evolution

Bar length trends (§3.2) can help us understand the secular evolution phase of the bar. We can safely assume that during the secular evolution phase of any non-interacting galaxy its bar length may be considered a proxy of bar age. However, this may not be true for any two galaxies, because the galaxy with the youngest bar can have the longest bar, provided its halo can absorb larger parts of the angular momentum emitted by the bar region (A03). Our comparisons, however, do not concern two galaxies but ensembles of a relatively large number of galaxies. For example in Fig. 4b we compare ensembles of galaxies with different n values. But the number of galaxies in each ensemble is sufficiently large for us to assume that galaxies with a variety of halo properties are included in a roughly similar manner in all ensembles. This subtle, but im-

²⁴ Of course, there are $n < 2.5$ galaxies that have no bulge (e.g., Simmons et al. 2013). However, for simplicity, we consider all galaxies with $n < 2.5$ to contain a disk pseudobulge even if it might be a pure disk galaxy. This will not affect our discussion since pure disks and disk pseudobulges are closely related (see Kormendy & Kennicutt 2004).

portant point is intrinsic to our analysis and will be discussed further in §6.

The strongest L_{sbar} trends we observe are found within star-forming disk galaxies (the average L_{sbar} increases monotonically with M_* , n , and $\Sigma_{1\text{kpc}}^*$; see Fig. 4). To better understand the underlying physical processes responsible for these trends, we separate the data in Fig. 4 by bulge type; this is shown in Fig. 7. Recall that galaxies with $n < 2.5$ are considered to contain disk pseudobulges while galaxies with $n > 2.5$ are considered to contain classical bulges. Note that quiescent galaxies with $n < 2.5$ are very rare, hence they are not shown.

During the secular evolution phase, bars become stronger, longer, and more efficient at funneling gas into the central regions of galaxies, leading to more massive disk pseudobulges (AMR13). This prediction matches our observations in Figs. 7b and 7c, where it is clear that L_{sbar} is correlated with n and $\Sigma_{1\text{kpc}}^*$ for the disk pseudobulge galaxies (purple). These correlations give evidence for the secular evolution phase of bars.

The L_{sbar} trends with classical bulges are much more complex and also much less straightforward to interpret. Simulations show that classical bulges should foster secular evolution by absorbing some of the angular momentum emitted by the bar region (A03). Hence the expectation is that galaxies with more massive classical bulges should have longer bars, but also longer disk scale lengths.

Figs. 7b and 7c show that the classical bulge galaxies (light blue and red) generally have longer scaled bar lengths than galaxies without a classical bulge, i.e., the disk pseudobulge galaxies. However, there is little evidence of increasing scaled bar length with increasing n and $\Sigma_{1\text{kpc}}^*$. In fact, there actually appears to be a decrease in scaled bar length for $\log n$ larger than 0.6 (i.e., n larger than about 4, equivalent to a more concentrated light profile than the standard $r^{1/4}$ de Vaucouleurs profile). Similarly the scaled bar length stops increasing in the rightmost panel for $\Sigma_{1\text{kpc}}^*$ larger than roughly $10^{9.8} M_{\odot}/\text{kpc}^2$ (although there seems to be a final increase in scaled bar length at the highest $\Sigma_{1\text{kpc}}^*$).

This decrease in scaled bar length with large n and $\Sigma_{1\text{kpc}}^*$ does not disagree with simulation results, and can be attributed to the presence of a very high central mass concentration (CMC)²⁵. Indeed, our last averaged point is roughly

²⁵ We note that this is just one of the possible reasons for this observed decrease. This could also correspond to the regime where the bulge is so massive that it has significantly delayed the onset of bar formation, resulting in a lack of bar evolution.

at a $\log n$ value of 0.8, which corresponds to a Sérsic index of roughly 6.5. This could well be due to a luminosity spike in the center of the galaxy which would hamper the bar growth and evolution if it pre-existed the bar, or if grown later, that would bring a decrease of the bar length and strength (e.g., Shen & Sellwood 2004; Athanassoula et al. 2005). This strong CMC will thus bring a decrease of bar length at the highest values of n , as seen in Fig. 7b (and Fig. 4b).

Nevertheless, at least part of this decrease could be spurious and due to the fact that the bar component is not specifically included in our 2-component decompositions, which is more worrisome for galaxies with stronger and longer bars. To test it we scaled the *absolute* bar length with the r -band isophotal radius at 25 mag arcsec⁻² from the SDSS pipeline and re-created Figs. 4 and 7. The results can be found in Appendix B. We find then that the decrease seen with the disk scale length at high n and $\Sigma_{1 \text{ kpc}}^*$ is considerably lessened. We do not fully understand the bar length trends with the classical bulge galaxies at the highest n and $\Sigma_{1 \text{ kpc}}^*$, more work needs to be done. Let us note, however, that the correlations of the scaled bar length with the disk pseudobulge galaxies are still present even when scaling with the isophotal radius, thus enhancing our confidence in the corresponding decompositions and trends.

5. DISCUSSION

5.1. Are We Observing Secular Evolution?

In §3 and §4, we showed evidence which suggests that disk pseudobulges are more massive in populations of galaxies which are more likely to host bars and which host longer bars (specifically that average values of p_{bar} and L_{sbar} increased with n and $\Sigma_{1 \text{ kpc}}^*$ for disk pseudobulge galaxies). We interpreted this as observational evidence of bar-driven secular evolution growing disk pseudobulges (Kormendy & Kennicutt 2004; Athanassoula 2005). Our interpretation hinges on the assumption that bar length traces the evolution of bars. This assumption is based on both simulations of bar growth as well as observational data. Elmegreen et al. (2007) showed that bar length mirrors bar strength (see also Block et al. 2004). The simulations of bar growth shown in Fig. 5 – and a large number of others, as reviewed by Athanassoula (2012) – demonstrate that isolated bars typically grow stronger with time.

Furthermore, the simulations of AMR13 argue that bars in isolated galaxies are long-lived structures – in the ~ 10 Gyrs that their simulations covered, not one of their bars dissolved (see also Debattista et al. 2006 and Berentzen et al. 2007 for a similar conclusion). Recent zoom-in cosmological simulations by Kraljic et al. (2012) also support the idea that bars are long-lived structures. Their simulations show that most of the bars that formed at $z \leq 1$, when mergers have become less frequent, persist down to $z = 0$. Observational studies have now observed bars with modest frequencies out to $z \sim 1$ (Abraham et al. 1999; Jogee et al. 2004; Elmegreen et al. 2004; Sheth et al. 2008; Melvin et al. 2013), and one upcoming study detects bars as far out as $z \sim 1.5$ (J. Herrington et al. 2013, submitted.), with the implication that many of the bars we observe in the local Universe could have formed at $z \sim 1$ or earlier. This gives a substantial time window for secular evolution to grow longer bars and stronger disk pseudobulges.

Previous works have shown a trend between bar length and Hubble type – that bars are longer in earlier

type disks – and used this to argue that secular evolution had been observed (e.g., Athanassoula & Martinet 1980; Elmegreen & Elmegreen 1985; Martin 1995; Regan & Elmegreen 1997; Erwin 2005; Laurikainen et al. 2007; Elmegreen et al. 2007; Menéndez-Delmestre et al. 2007; Gadotti 2011). Our result is novel in that it looked for trends of bar length with the central mass density in the very centers of galaxies, a quantity that is directly linked to secular evolution in models. Our sample is also nearly an order of magnitude larger than any previous study. Thus, we argue that our result is the best evidence yet for bar-driven secular evolution in disk galaxies.

Recent results from several high resolution simulations present mechanisms for the formation of disk pseudobulges that do not rely on secular evolution (Inoue & Saitoh 2012; Okamoto 2013), but rather involve dynamical instability in clumpy galaxies or high-redshift starbursts. While the bulges of these simulations do have characteristics of local disk pseudobulges²⁶, our results here suggest that secular evolution does have a major effect, both in creating disk pseudobulges and in building up the stellar mass in the bulge region of barred galaxies.

Nevertheless, there are substantial numbers of disk galaxies that are non-barred and are hosting disk pseudobulges (Kormendy & Kennicutt 2004). Up to a third or more of the local disk galaxy population is unbarred in even the most conservative reckoning. This observations argues that disk pseudobulges have more than one formation mechanism. Perhaps disk pseudobulges in non-barred galaxies were created through high redshift channels, while the disk pseudobulges in barred galaxies may have been created, and are still in the process of growing through bar-driven secular evolution, at much later times.

5.2. Can Bars Quench Star Formation?

The highest values of p_{bar} are found among quiescent galaxies with $n \sim 2.5$ (see Fig. 3b). Here we consider the question of whether these bars were formed in situ or if they could be implicated in the processes which turned these disk galaxies quiescent. We ask ‘were these bars formed in $n \sim 2.5$ quiescent galaxies, or did they form in star-forming galaxies (with $n \lesssim 2.5$) that evolved into the $n \sim 2.5$ quiescent disk galaxies?’ We refer to this latter process as ‘bar quenching’ and explore this idea further.

Bars have been associated with enhanced central star formation in galaxies for decades (Hawarden et al. 1986; Dressel 1988; Friedli & Benz 1993; Giuricin et al. 1994; Huang et al. 1996; Martinet & Friedli 1997; Martin & Friedli 1997; Ho et al. 1997; Ellison et al. 2011; Oh et al. 2012; Wang et al. 2012). This is a natural consequence of the evolution of gas in a disk galaxy under the influence of a bar. The bar-induced gravitational torques funnel gas into the centers of galaxies (Matsuda & Nelson 1977; Simkin et al. 1980; Athanassoula 1992; Wada & Habe 1992, 1995; Friedli & Benz 1993; Heller & Shlosman 1994; Knapen et al. 1995; Sakamoto et al. 1999; Sheth et al. 2005), where it should quickly form stars, thus enhancing the central star formation. If this secular evolution were efficient, it could accelerate the depletion of the gas supply within a considerable fraction of the disk, namely the region within corotation.

²⁶ Not all bulges made from clump coalescence have characteristics of disk pseudobulges. For example, Elmegreen et al. (2008) show that their bulges made through clump coalescence have properties of classical bulges.

If this process were not balanced by an increased inflow of cosmological gas, this would ultimately, produce a quiescent barred galaxy (Masters et al. 2011; Masters et al. 2012).

Large surveys such as SDSS (Abazajian et al. 2009), COSMOS (Scoville et al. 2007), and AEGIS (Davis et al. 2007) have painted a clear picture of the structural properties of quiescent galaxies – they are massive, centrally concentrated, and have high central velocity dispersions (e.g., Franx et al. 2008; Bell et al. 2012; Wake et al. 2012; Cheung et al. 2012). Cheung et al. (2012) recently found that the most distinguishing structural parameter of quiescent galaxies (compared to star-forming galaxies) is their central surface stellar mass density (within a radius of 1 kpc). Almost all quiescent galaxies in the sample of Cheung et al. (2012) have high values of $\Sigma_{1 \text{ kpc}}^*$, while star-forming galaxies mainly have low values of $\Sigma_{1 \text{ kpc}}^*$. This is clear evidence that the process(es) that quench star formation in these galaxies are related to the buildup of the central stellar mass density. We consider here if secular evolution is *able* to build high enough central densities to act as a quenching mechanism.

Indeed, Fig. 7c shows that the $\Sigma_{1 \text{ kpc}}^*$ values of the diskypseudobulge galaxies overlap partly with the $\Sigma_{1 \text{ kpc}}^*$ values of the classical bulge galaxies. The most massive of the diskypseudobulges we argue are grown by bar-driven secular evolution are comparable in central density to the smallest of the classical bulges. This suggests that secular evolution *can* build the high central densities that are observed in quiescent galaxies. This appears to be circumstantial evidence for an interesting, and potentially important galaxy evolution process – bar quenching. We caution, however, that our identification of diskypseudobulges in quiescent barred disk galaxies is based on global Sérsic fits. If it is indeed the case that there exist quiescent disk galaxies which host only diskypseudobulges, and show no evidence for classical bulges, this will be strong evidence for the process of ‘bar quenching’ having acted in these galaxies. However, more accurate identifications of diskypseudobulges are needed to verify this claim.

6. CONCLUSION

In this paper, we use hundreds of thousands of visual classifications measurements of galactic bars provided by ‘citizen scientists’ through the Galaxy Zoo project (Lintott et al. 2008, 2011; Willett et al. 2013). We first select a sample of disk galaxies in which reliable bar classifications can be made – we call this the Galaxy Zoo 2 Disk (GZ2D) sample, which comprises 13,295 oblique (i.e., face-on or mildly inclined) disk galaxies in a volume limit to $z=0.06$. This sample is similar to the GZ2 samples used previously to study trends of the bar fraction by Masters et al. (2011) and Masters et al. (2012). Strongly barred galaxies identified in GZ2 were part of a small Galaxy Zoo project which used a Google Sky interface to collect measurements of bar lengths (Hoyle et al. 2011). In this paper we also make use of this Bar Length (BL) sample, which comprises 1,154 galaxies. We use these data to analyze the dependence of bar likelihood (p_{bar} , a weighted and debiased fraction of GZ users identifying a bar, and which acts like a probability of a galaxy containing a visually identifiable bar; Willett et al. 2013) and scaled bar length ($L_{\text{sbar}} = L_{\text{bar}}/2.2r_d$; a measure of bar strength, linked to how evolved a bar is) on other galactic properties. Specifically we test how the likelihood and length of bars depend on specific star formation rate (SSFR; estimated through nebular emission lines from the SDSS fiber, and the broadband *ugriz* SDSS photometry,

as measured by MPA-JHU) and inner galactic structure (i.e., bulge prominence) parameterized by global Sérsic index, n , as measured by GIM2D, and central surface stellar mass density, $\Sigma_{1 \text{ kpc}}^*$, as estimated from a 1 kpc radius circular aperture projected onto SDSS images.

Our main observational results (§3) are:

1. There exists an anti-correlation between p_{bar} and SSFR; this relationship is present even at fixed M_* , n , or $\Sigma_{1 \text{ kpc}}^*$.
2. The structural trends of p_{bar} are bimodal with SSFR. In the star-forming sequence, p_{bar} correlates with n and $\Sigma_{1 \text{ kpc}}^*$, while in the quiescent population, p_{bar} anti-correlates with n and $\Sigma_{1 \text{ kpc}}^*$.
3. The structural trends of L_{sbar} are also bimodal with SSFR. Within the star-forming sequence, L_{sbar} correlates with n and $\Sigma_{1 \text{ kpc}}^*$, in a similar way to p_{bar} . However within the quiescent population, L_{sbar} shows a rather different behavior, with a peak at values of $n \sim 4$ and $\Sigma_{1 \text{ kpc}}^* \sim 10^{9.8} \text{ M}_{\odot}/\text{kpc}^2$.

We compare these results to simulations of bar formation and evolution in §4. We find that the underlying physical processes become clearer upon separating these galaxies by those that contain diskypseudobulges ($n < 2.5$) and those that contain classical bulges ($n > 2.5$). This comparison reveals the following:

1. Assuming that SSFR is a good tracer of gas content, the anti-correlation of p_{bar} with SSFR is consistent with the expected effects of gas on *bar formation*. Simulations show that gas delays the formation of bars, thus many gas-rich galaxies simply have not yet formed bars, while most gas-poor disk galaxies have.
2. The observed trends of p_{bar} and L_{sbar} with n and $\Sigma_{1 \text{ kpc}}^*$ for classical bulge galaxies are consistent with the effects of classical bulges and CMCs on bar formation and evolution. The gravitational forcing of classical bulges ‘dilute’ the non-axisymmetric forcing of the bar, which delays the formation of a bar. This diluting effect is more powerful in more massive classical bulges, resulting in a longer delay of *bar formation*. After the bar has formed, however, classical bulges are expected to promote *secular evolution* by absorbing the angular momentum emitted from the bar region; this process also scales with the mass of the bulge and leads to both longer bars and longer disk scale lengths. Our results suggest that for Sérsic index up to roughly $n = 4$ the bar length may increase faster than the disk scale length. For yet higher values of n , a strong ensuing CMC could lead to a decrease of the bar strength by generating instabilities of the main family of bar-supporting orbits.
3. The correlations of p_{bar} and L_{sbar} with n and $\Sigma_{1 \text{ kpc}}^*$ for the diskypseudobulge galaxies are in agreement with the predictions of *bar-driven secular evolution*. Bars drive gas toward the centers of galaxies, where the gas should eventually form stars and give rise to diskypseudobulges. As bars grow stronger and longer, the ability to funnel gas grows stronger as well, resulting in more massive diskypseudobulges.

The comparison of the observational results we present here with simulations of bar formation and growth shows general agreement, indicating that many of the underlying physical processes of bar formation and evolution are understood. An implication of this is that we are confident in our basic understanding of the relationship between bars and their host galaxies. Bars are clearly not stagnant structures, rather they are dynamic, evolving, and furthermore directly influence the evolution of their host galaxies.

While this work only concerns the universe at $z \sim 0$, the ramifications of this idea reach far beyond the local universe. There is increasing evidence that bars have been present since $z \sim 1$ (Abraham et al. 1999; Jogee et al. 2004; Elmegreen et al. 2004; Sheth et al. 2008; Melvin et al. 2013; J. Herrington et al. 2013, submitted.), indicating that the evolution of disk galaxies has been affected by bars for the last ~ 8 billion years. Moreover, if the observed evolution of bar fraction with redshift is extrapolated into the future (there is now an agreement that bar fraction increases towards lower z), then bars will soon be present in nearly all disk galaxies, and hence become an even more dominant driver of disk galaxy evolution.

We can not yet claim to understand all aspects of the symbiotic relationship between bars and their host galaxies. We do not fully understand the complicated behavior we observe between bar length and inner galactic structure in disk galaxies hosting classical bulges. Our tentative explanation is that these trends are due to the presence of CMCs, however this should be tested with much higher resolution imaging to probe the very centers of galaxies. Furthermore, in this work we have not explored many of the parameters that are predicted to affect bar formation and evolution (e.g., the dark matter halo and the velocity dispersion of the stars in the disk, Athanassoula & Sellwood 1986; A03). Even so, we found a good agreement between theory and observations and all observational trends could be well explained by simulations. This may be due to the large size of our sample, which allows for a variety of halo properties and of disk velocity dispersions in a roughly similar manner in all ensembles we compared. Finally, the role bars may play in processes which quench star formation is an interesting, and potentially important issue for galaxy evolution that warrants further study.

The most notable success in our comparison between observation and theory is the evidence we present for secular evolution. Unlike galaxy mergers, secular evolution is a slow and gentle process that is not immediately obvious in images. There has been previous observational evidence of secular evolution in galaxies (e.g., Athanassoula & Martinet 1980; Courteau et al. 1996; MacArthur et al. 2003; Elmegreen et al. 2007; Laurikainen et al. 2009; Coelho & Gadotti 2011; Sánchez-Janssen & Gadotti 2013), however the combination of our large dataset and the observed correlations of bar likelihood *and* bar length with inner galactic structure for star-forming disk galaxies makes our results one of the most com-

prising pieces of evidence of not only the existence of secular evolution, but also of the role of ongoing secular processes on the evolution of disk galaxies.

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APPENDIX

COMPLETENESS

Galaxy Zoo 2 Disk Sample

The Galaxy Zoo 2 Disk (GZ2D) sample was selected on the basis of hundreds of thousands of visual morphological classifications collected via the Galaxy Zoo website. In order for a galaxy to be in this sample, the majority of volunteers classifying it must have identified 'features' in it, and identified it as not being an edge-on disk (see Masters et al. 2011; Willett et al. 2013). In addition we apply an extra cut at $b/a > 0.5$ to ensure disks are face-on enough to identify bars. This results in a sample of disk galaxies with a broad mix in Hubble types. Objects might contain an obvious disk (e.g., SBc, Sc) or a subtle disk (e.g., S0).

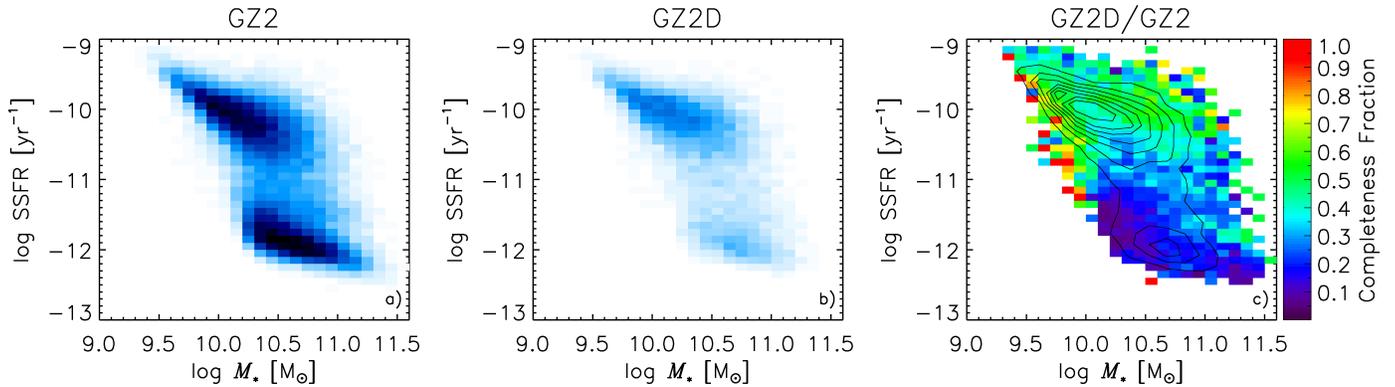


Figure 8. The number density distribution of the: *a)* volume-limited parent Galaxy Zoo 2 (GZ2) sample and *b)* Galaxy Zoo 2 Disk (GZ2D) sample; both are scaled to the same. *c)* The completeness of the GZ2D sample relative to the GZ2 sample. For each bin, we calculate the fraction of GZ2D galaxies in the GZ2 sample and color it according to the color bar to the right. The black contours outline the number density of the GZ2D sample and only bins with at least 2 GZ2 galaxies are shown. The completeness of GZ2D is bimodal such that it recovers $\sim 50\%$ of high SSFR ($> 10^{-11} \text{ yr}^{-1}$) galaxies and $\sim 20\%$ of low SSFR ($< 10^{-11} \text{ yr}^{-1}$) galaxies.

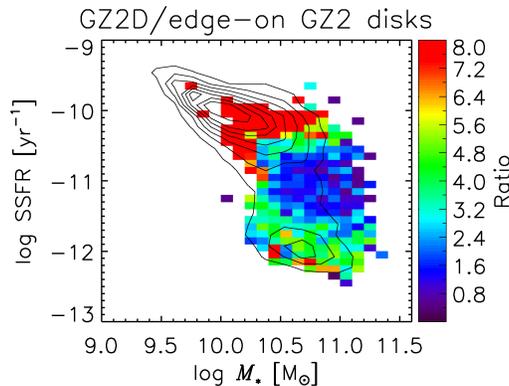


Figure 9. The ratio of the number of galaxies in the GZ2D sample to the edge-on GZ2 disk sample. The black contours outline the number density distribution of the GZ2D sample. Only bins with $n \geq 2$ edge-on GZ2 galaxies are shown. GZ2D does not seem to be strongly biased against low mass quiescent disks.

While we do not expect problems in identifying the former in any orientation, S0 galaxies are notoriously difficult (even for the most expert classifiers) to separate from ellipticals, if viewed face-on. We consider in this section if any face-on disk galaxies are missing from our sample. Presumably, if a galaxy had a bar, it would be readily identify as ‘featured’ and included in this sample, thus we assume any missing disk galaxies will be non-barrred and therefore introduce potential biases into our results.

We use as a comparison sample, the volume-limited parent Galaxy Zoo 2 sample (see §2.2 for details of our initial Galaxy Zoo 2 sample) that the GZ2D sample was originally drawn from, as well as a sample of edge-on disk galaxies in which we expect all types of disks will be equally easy to identify. As a reminder, the parent Galaxy Zoo 2 sample has the following criteria:

1. $0.01 < z < 0.06$, where z is the SDSS spectroscopic redshift.
2. $M_r \leq -20.15$, where M_r is the rest-frame absolute Petrosian r -band magnitude.

Hereafter, this sample will be referred to as the Galaxy Zoo 2 sample, or simply, the GZ2 sample. We match the GZ2 sample to the MPA-JHU catalog for stellar masses and star formation rates, resulting in a total of 43,221 galaxies.

To identify edge-on disks, we use thresholds in the Galaxy Zoo vote fractions for ‘features of disk’ ($p_{\text{features}} > 0.5$) and for ‘edge-on disk’ ($p_{\text{edge-on}} > 0.80$), this is slightly more conservative than the recommended thresholds for selecting a ‘clean edge-on’ sample as given in Willett et al. (2013), but we do not expect the selection to introduce any bias with Hubble type for disk galaxies.

Fig. 8 compares the number density distribution of the GZ2D sample (panel b) to that of the whole volume limited GZ2 sample (panel a). Both panels are scaled so that the blue scale indicates the same range of density and only bins with at least 2 galaxies are shown. Using the GZ2 sample as the fiducial completeness standard, panel c displays the completeness of the GZ2D sample (i.e., the fraction of the GZ2 sample which is in GZ2D) as indicated by the legend. To aid the eye, contours of the GZ2D number density distribution are over-plotted. We point out that completeness levels of greater than 50% are not expected since the selection on axial ratio ($b/a > 0.5$) removes approximately half of all disk galaxies. In this plot we observe the expected bimodality, such that the completeness of high SSFR ($> 10^{-11} \text{ yr}^{-1}$; ‘star-forming’) galaxies is much higher ($\approx 50\%$ complete) than it is for low SSFR ($< 10^{-11} \text{ yr}^{-1}$; ‘quiescent’) galaxies ($\approx 20\%$ complete). This reveals the well know correlation between SSFR and morphology - that most star-forming galaxies have disks, and many quiescent galaxies are elliptical, so do not have obvious ‘features’ to be selected as part of the GZ2D sample.

This test, however, cannot reveal if the GZ2D sample represents a fair selection of all disks. To test that, we isolate a sample of edge-on disk galaxies in which we expect all disks (even S0s) will be identified. If the GZ2D sample is fairly representative

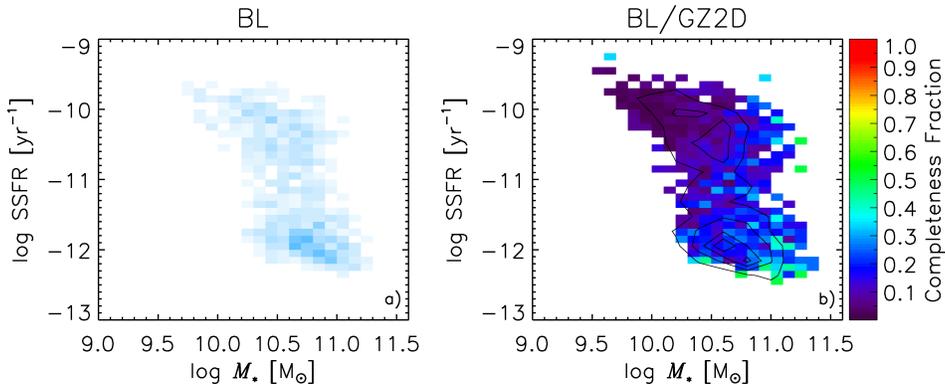


Figure 10. *a*): The number density distribution of the Bar Length (BL) sample scaled to a quarter of panel a of Fig 8. *b*): The completeness of the BL sample relative to the GZ2D sample; the black contours in this panel represents the number density distribution of the BL sample. Only bins with 2 or more GZ2D galaxies are shown.

of all disk galaxies, then the ratio of GZ2D (face-on disk) galaxies to the sample of edge-on disks should be uniform throughout the SSFR-mass diagram (this assumes all disk galaxies are randomly orientated, which we expect they should be, but also see Simard et al. 2011, and that the inclination introduces no systematic biases into estimates of SSFR or stellar mass, which is less clear).

Fig. 9 compares the number density of the edge-on GZ2 disks to our GZ2D sample of mildly inclined or face-on disk galaxies. We show the ratio of the number of galaxies in the GZ2D sample to the edge-on GZ2 disks sample. Only bins with at least 2 galaxies from the edge-on GZ2 disks sample are shown and the black contours represent the number density distribution of the GZ2D sample. For high SSFR galaxies, there are ~ 7 galaxies in the GZ2D sample for every edge-on GZ2 disk galaxy. This is likely due to a combination of the expected number ratios for edge-on and not edge-on disk galaxies (e.g., for random orientations, we expect one galaxy with $i > 85^\circ$ for every five with $i < 65^\circ$), and the possible effects of increased internal extinction in the edge-on sample causing SSFR to be underestimated. However we do not expect to be missing systematically any star-forming disk galaxies.

Because of the extinction of edge-on galaxies, the sample of low SSFR ($\log \text{SSFR} < -11.6 \text{ yr}^{-1}$) edge-on GZ2 disks may contain a combination of truly low SSFR disks and reddened intermediate SSFR disks. However, we assume that the reddened intermediate SSFR contribution to the low SSFR regime of the edge-on GZ2 disks sample is uniform across stellar mass and only changes the absolute scaling of the number ratio between GZ2D and edge-on GZ2 disks. We therefore examine the uniformity of the low SSFR regime in Fig. 9 to gauge whether the GZ2D sample is missing any quiescent disks.

The number ratio between edge-on quiescent disks and face-on quiescent disks is largely uniform (at ~ 5 oblique disks per edge-on disk). There is, however, hints of a small dearth in the GZ2D sample at low masses. Averaging the number ratios at low masses ($\log M_* < 10.6$) reveals that we find $\approx 10\%$ less GZ2D galaxies compared to the average number ratios of the high mass quiescent disks. The total number of low mass quiescent galaxies in our sample is ≈ 900 , so this suggests we may be missing ≈ 90 low mass quiescent disk galaxies. Presumably, if a galaxy had a bar, it would be readily spotted and included in this sample, thus we assume the missing disk galaxies are non-barred. We assume that the missing disks have values of n and $\Sigma_{1 \text{ kpc}}^*$ typical for GZ2D galaxies of the same mass and SSFR. We find that the n and $\Sigma_{1 \text{ kpc}}^*$ values of these low mass quiescent disks are roughly uniformly distributed, meaning that the p_{bar} trends with n and $\Sigma_{1 \text{ kpc}}^*$ for the quiescent population are unaffected by this incompleteness. We can estimate how many unbarred quiescent disk galaxies we are missing for every bin by simply dividing the total number of missing galaxies (≈ 90) by the total number of bins that the quiescent population spans in n and $\Sigma_{1 \text{ kpc}}^*$, which turns out to be ~ 20 bins. Thus we are missing ≈ 5 unbarred quiescent disks in every $N = 100$ bin of n and $\Sigma_{1 \text{ kpc}}^*$ (see Figs. 3b and 3c). Even if all five galaxies have $p_{\text{bar}} = 0$ this would reduce the average p_{bar} in each bin by at most 5% (by simply adding 5 more galaxies in the denominator).

The number of missing low mass disks in the affected part of Fig. 3a works out to be ≈ 10 per low mass quiescent bin (there are ~ 10 bins in the low mass quiescent regime). Fig. 3a shows that the p_{bar} values for the low mass quiescent bins are ~ 0.60 . Adding 10 non-barred ($p_{\text{bar}} = 0$) disk galaxies to these bins, i.e., adding 10 galaxies to the denominator, reduces these p_{bar} values to ~ 0.50 . Our qualitative results and interpretation are unaffected. Therefore, the missing non-barred low mass quiescent disks do not significantly influence our results.

Bar Length Sample

Unlike the GZ2D sample, there is not a concern that the BL sample is missing non-barred disks since, as the sample name implies, the BL (Bar Length) sample only contains barred disks. Nevertheless, we want to ensure that it is not suffering any selection bias.

Fig. 10 shows the completeness of the BL sample relative to the GZ2D sample. The completeness of BL is approximately bimodal with SSFR. In the high SSFR regime ($\log \text{SSFR} > -11 \text{ yr}^{-1}$), the BL sample is $\sim 10\%$ complete, while in the low SSFR regime ($\log \text{SSFR} < -11 \text{ yr}^{-1}$), it is $\sim 20\%$.

This completeness bimodality is reasonable because the BL sample is primarily composed of strong bars, which as illustrated in Fig. 3, strong bars mainly lie in the quiescent population. However, since our analysis splits the BL sample into star-forming and quiescent (i.e., Fig. 4 and Fig. 7), this difference in completeness should be inconsequential to our results and interpretations.

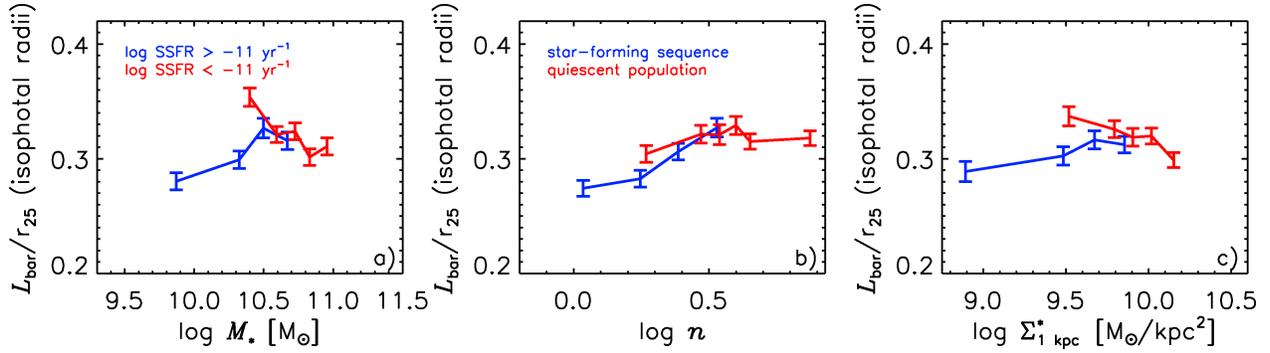


Figure 11. Average bar length scaled by the isophotal radii, L_{bar}/r_{25} , plotted against: a) M_* , b) n , and c) $\Sigma_{1 \text{ kpc}}^*$. Galaxies were split by their star formation state, namely, $\log \text{SSFR} > -11 \text{ yr}^{-1}$ (star-forming; blue) and $\log \text{SSFR} < -11 \text{ yr}^{-1}$ (quiescent; red). Each bin contains ~ 100 galaxies. The error bars are given by σ/\sqrt{N} , where σ is the standard deviation of L_{sbar} per bin, and N is the total number of galaxies per bin.

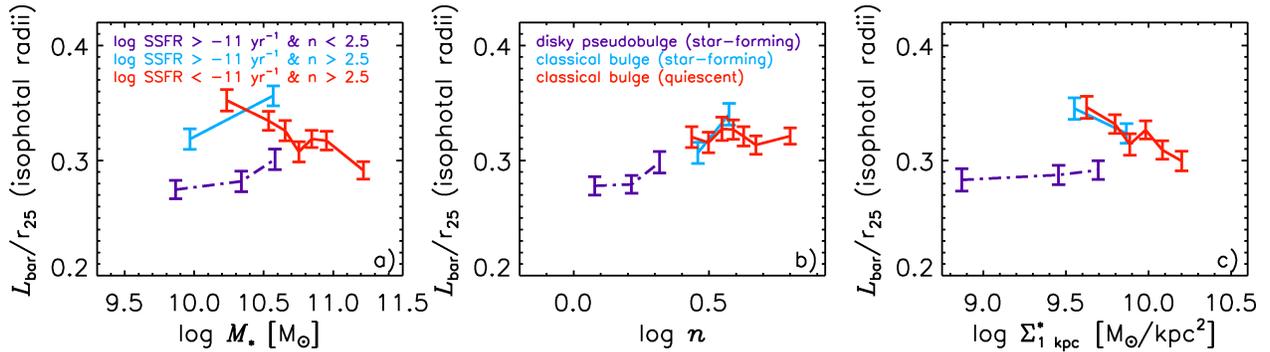


Figure 12. Average L_{bar}/r_{25} plotted against: a) M_* , b) n , and c) $\Sigma_{1 \text{ kpc}}^*$. The details of this figure are identical to that of Fig. 11, with the exception that each bin contains ~ 75 galaxies and also, galaxies are further separated by bulge type, as identified by n . Purple points represent the star-forming disk pseudobulge galaxies, light blue points represent the star-forming classical bulge galaxies, and red points represent the quiescent classical bulge galaxies.

BAR LENGTH SCALED BY ISOPHOTAL RADII

Comparing the trends of bar length scaled by the isophotal radii (Fig. 11 and 12) to those of L_{sbar} (Fig. 4 and 7) shows a good agreement. The only noticeable differences are at the highest n and $\Sigma_{1 \text{ kpc}}^*$, which is hard to interpret and may be due to a number of issues. These GIM2D disk scale lengths may be affected by the prominent bars present in these galaxies. But the better sky background determination and better object deblending of the GIM2D decompositions could also lead to a more accurate measurement of the disk scale length. More work needs to be done to truly understand the differences, but this is outside the scope of this paper. Moreover, this paper does not put a strong emphasis on the bar length trends at the highest n and $\Sigma_{1 \text{ kpc}}^*$, thus it does not affect our major conclusions.

R90/R50

Fig. 13 shows the effects of using the Petrosian concentration index from SDSS, R90/R50, where R90 and R50 are the radii enclosing 90 and 50 % of the galaxy luminosity, respectively. The trends with p_{bar} in Fig. 13a are almost identical to that with Sérsic index (Fig. 3b). Fig. 13b and 13c show that the trends with R90/R50 for the star-forming sequence, star-forming disk pseudobulge galaxies, and the star-forming classical bulge galaxies are the same as with n (Fig. 4b and 7b), i.e., L_{sbar} increases with increasing n or R90/R50.

For the quiescent population (Fig. 13b) and the quiescent classical bulge galaxies (Fig. 13c), however, there is a noticeable difference between the trends of L_{sbar} at the highest values of R90/R50 and n . Namely, while there is a decrease of L_{sbar} at the highest n (Fig. 4b and 7b), there seems to be a steady increase of L_{sbar} with increasing R90/R50. It is unclear why this is the case. It could be due to the improved sky background determination and object deblending in the fits of Simard et al. (2011) compared to the standard SDSS pipeline. However, no matter the reason, this minor difference does not affect the paper since we leave the interpretation of the bar length trends for the highest n values open.

Comparing the trends of bar length scaled by the isophotal radii between n (Fig. 11b and 12b) and R90/R50 (Fig. 13d and 13e) shows general agreement between all populations.

Thus the results from R90/R50 and n are largely similar, and the use of either would not change the main conclusions of the paper.

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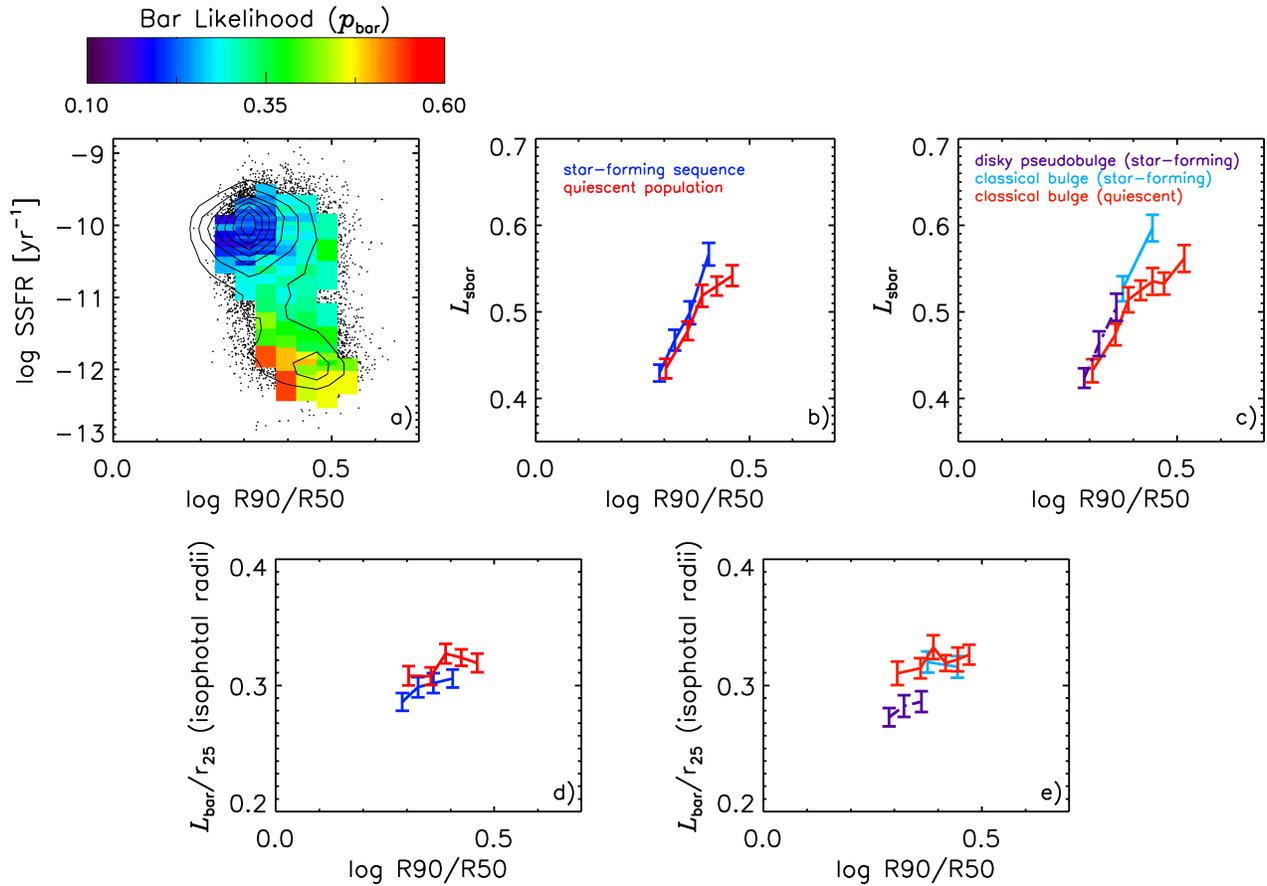


Figure 13. Replacing Sérsic index with R90/R50. *a)* plots average p_{bar} in bins of SSFR and R90/R50. *b) & c)* plot bar length scaled by GIM2D bulge+disk model disk scale length vs. R90/R50. *d) & e)* plot bar length scaled by the isophotal radii vs. R90/R50.

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