

Angular Resolution

ASTR 288C: Lecture 6

Astronomical “Instruments”

Naked Eye



Typical size: 3-9 mm diameter pupil

extremely portable

cheap

subject to blinking

Best for bright, large-field observing

Astronomical “Instruments”

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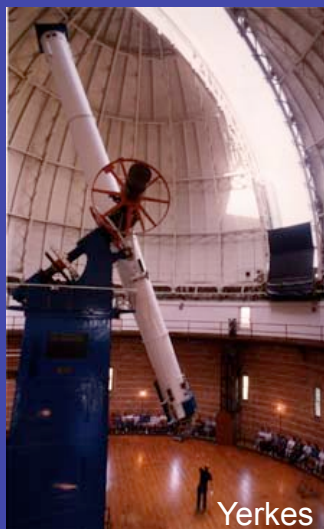
extremely portable

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Best for bright, large-field observing

Refracting Telescopes



Largest: Yerkes 102-cm (40-in) diameter lens

Typical amateur: 60-mm diameter lens

little maintenance

expensive per aperture size

reliable

heavy and bulky – size limit

best image quality

Best for solar system observing

Astronomical “Instruments”

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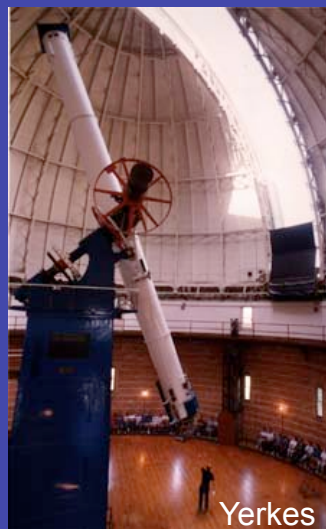
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Reflecting Telescopes



Largest single-mirror: Subaru & VLT 8.2-m diameter mirror

Largest segmented-mirror: GTC 10.4-m diameter “mirror”

cheaper per aperture size

slight light loss

good image quality

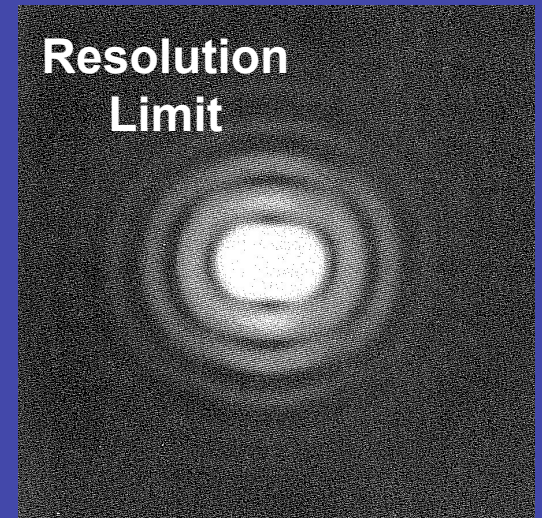
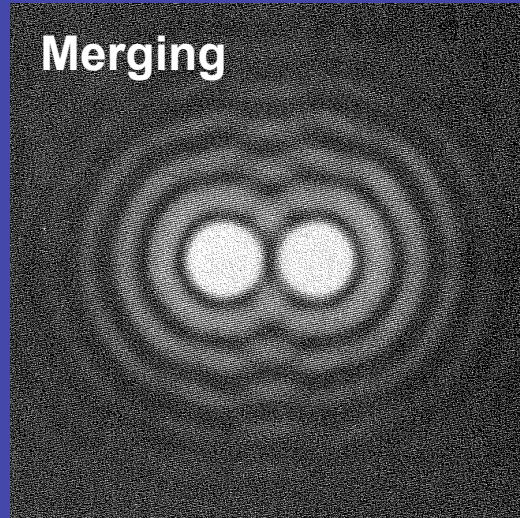
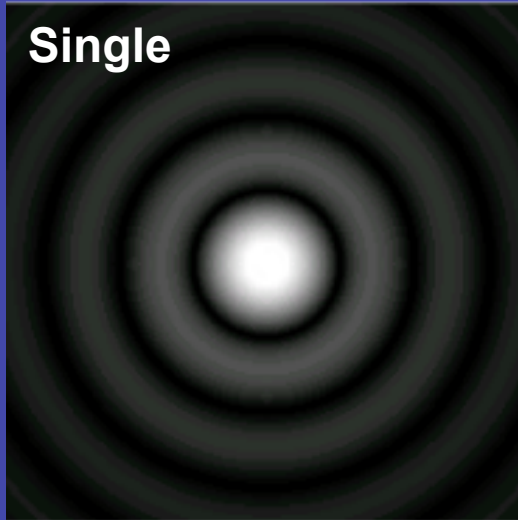
maintenance required

lighter – larger sizes

Best for (extra-)galactic observing

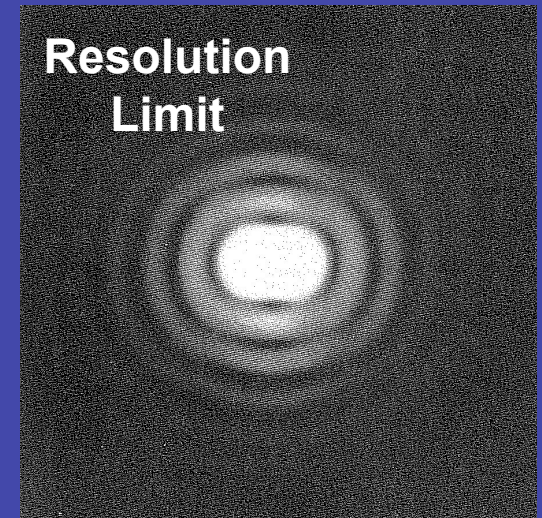
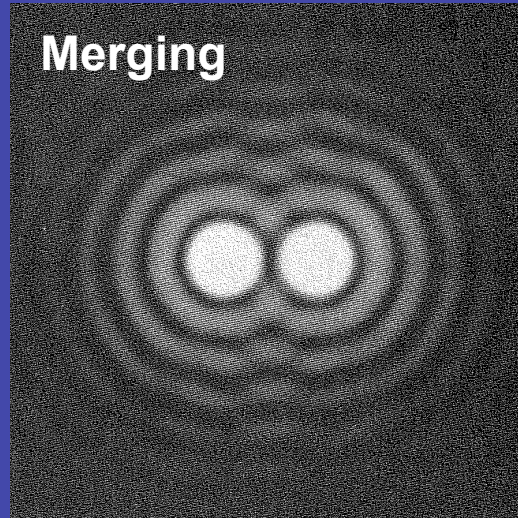
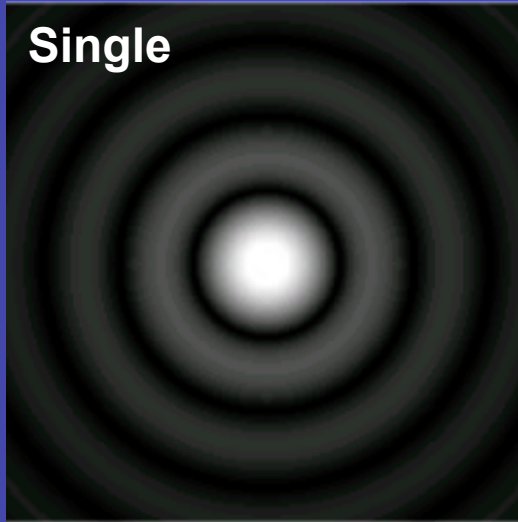
Diffraction and Angular Resolution

Airy Pattern



Diffraction and Angular Resolution

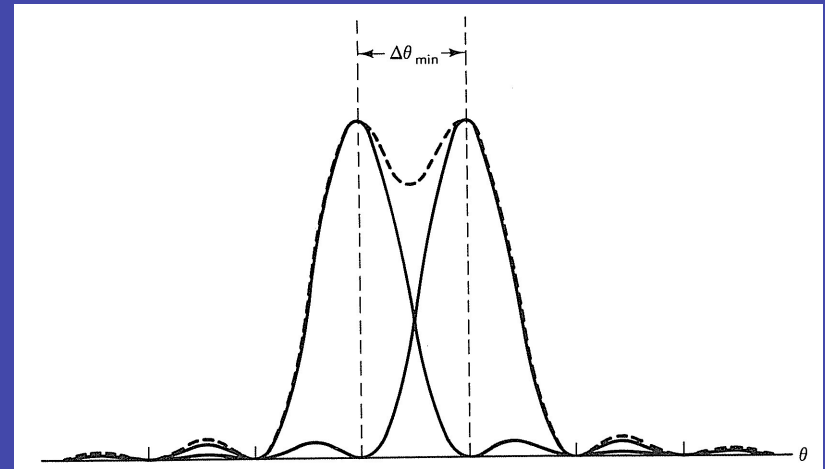
Airy Pattern



Rayleigh's Criterion

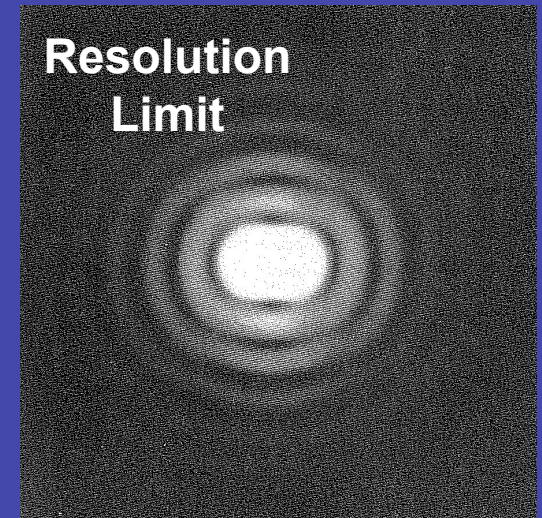
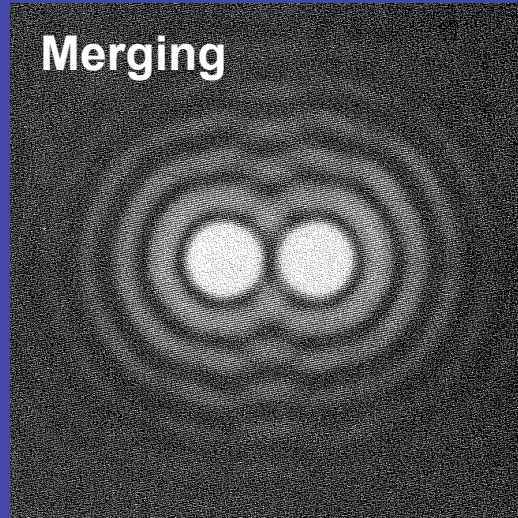
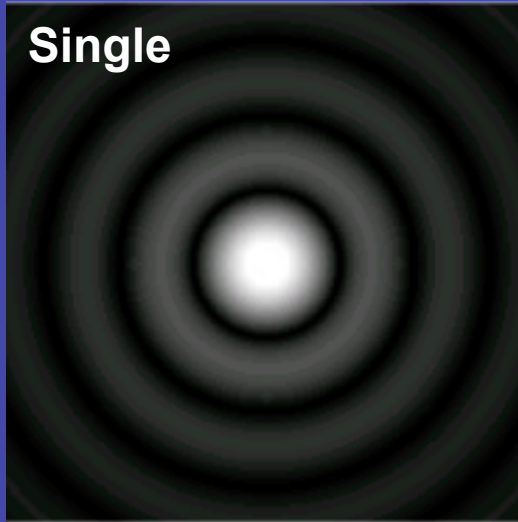
Two “point” (unresolved) sources are resolved from each other when separated by at least the radius of the airy disk.

$$\Theta = 1.22 \frac{\lambda}{D} \text{ rad}$$



Diffraction and Angular Resolution

Airy Pattern



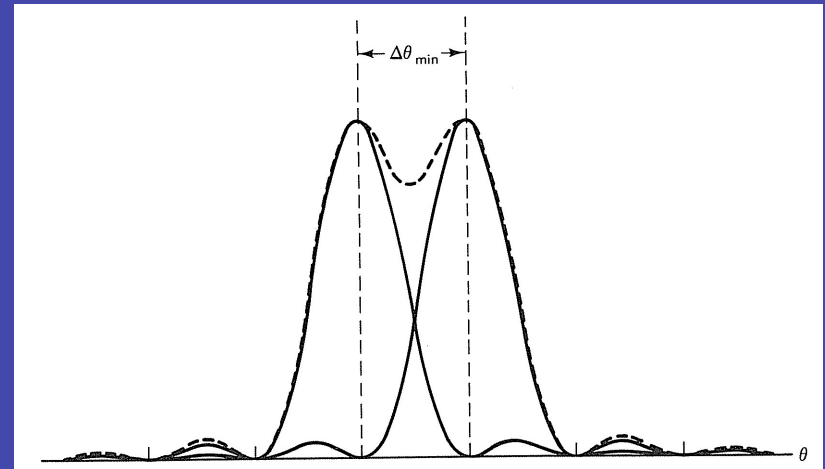
Rayleigh's Criterion

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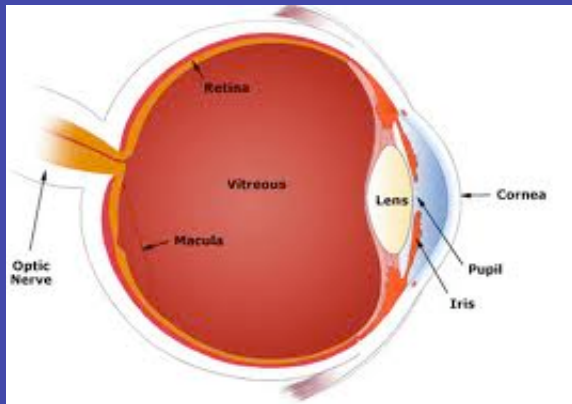
$$\Theta = 1.22 \frac{\lambda}{D} \text{ rad}$$

Careful! λ and D are naturally measured in different units

Also note: $360 \text{ deg} = 2 \pi \text{ rad}$



Angular Resolution: Human Eye

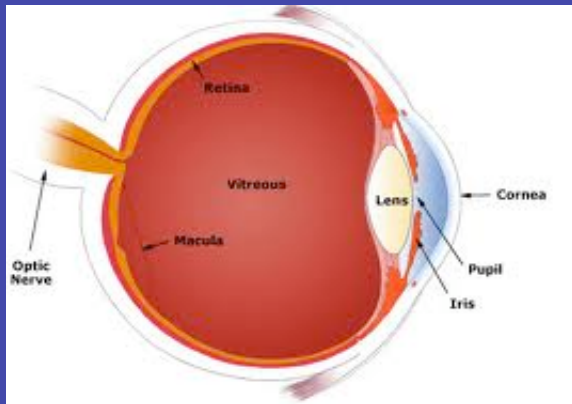


Pupil diameter: 3-4 mm (day)
5-9 mm (night)

Optimal sensitivity: $\sim 0.55 \mu\text{m}$ (V band)

$$\Theta = 1.22 \frac{\lambda}{D} \text{ rad}$$

Angular Resolution: Human Eye

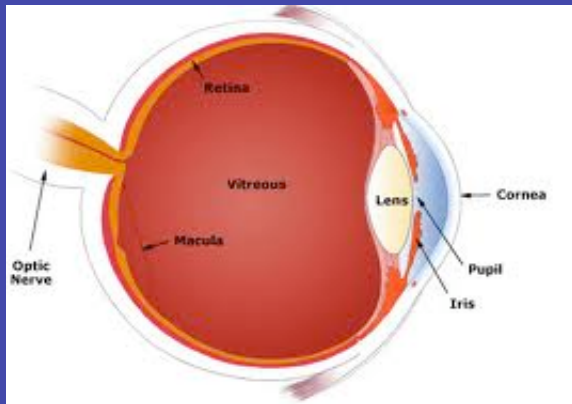


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Angular Resolution: Human Eye

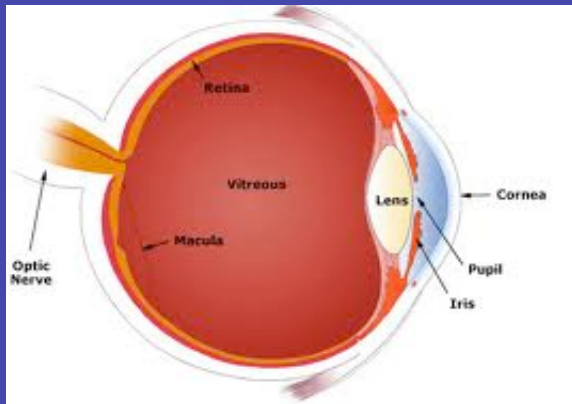


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$$= 0.0128 \text{ deg} \frac{3600''}{1 \text{ deg}}$$

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Moon

3 mm pupil



30'



Moon

9 mm pupil



30'



Moon
telescope



30'